

Volume I

# The Finite Analytic Method And Its Applications

Laminar and Turbulent Flows Past Two Dimensional and Axisymmetric Bodies

> Ching-Jen Chen Seok Ki Choi



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Department of Mechanical Engineering Iowa Institute of Hydraulic Research The University of Iowa Iowa City, Iowa 52242

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#### Laminar and Turbulent Flows Past Two Dimensional and Axisymmetric Bodies

#### **ABSTRACT**

A numerical study of laminar and turbulent flows past two dimensional bodies and axisymmetric bodies is presented. Numerical methods are developed to solve Navier-Stokes equations for two dimensional and axisymmetric flows in the arbitrary geometries. The complex physical geometry is resolved by use of numerically generated, body-fitted coordinates. The governing equations are written in the transformed domain using the orthogonal velocity components as dependent variables for momentum equations. The governing equations are discretized using both the finite analytic method and the finite volume method. Both one velocity staggered grid method and two velocities staggered method are employed for grid arrangements. The velocity and pressure coupling techniques in these grid arrangements are presented. The solution procedure of the SIMPLER numerical algorithm is used with a parabolic marching technique and a global pressure calculation method. For turbulent flow calculations, both the k- $\epsilon$  turbulence model and the two-layer turbulence model are used. ( $\langle \xi, \xi \rangle \rangle = \langle \xi, \xi \rangle^{1/6}$ )

Calculations are performed for laminar and turbulent flows past a finite flat plate and turbulent flow past axisymmetric bodies with different solution domains, numerical methods and turbulence models. Calculations include the development of a wake function method for the prediction of turbulent wake of a flat plate, predictions of turbulent flows past a finite flat plate, predictions of turbulent flow past axisymmetric bodies by the wall function method and by the two-layer turbulence model and predictions of turbulent flow past finite axisymmetric bodies. Comparisons of predictions by finite analytic method with those by finite volume method are made for some calculations. All the predicted results were compared with available experiment measurements. Good agreements between the predicted results and measured data were obtained.

#### **PREFACE**

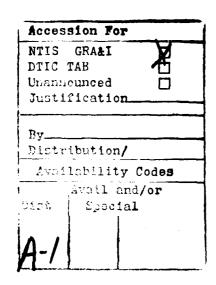
This monograph entitled "The Finite Analytic Method and Its Applications" contains the continuing developments of the numerical method called the "finite analytic" method. The finite analytic method was developed in early 1977 when I and Dr. Peter Li, then a graduate student, had difficulty in obtaining a converged solution from a system of finite difference algebraic equations derived for the Navier-Stokes equations for two-dimensional turbulent flow with a second order turbulence model. I conceived the finite analytic method one night and solved the simple two-dimensional Laplace equation. Dr. Li then carried the finite analytic method to the unsteady diffusion equation and nonlinear ordinary differential equation. The basic idea of the finite analytic method is to derive the approximate algebraic representation of a governing linear or nonlinear differential equation from the local analytic solution. The local analytic solution is obtained for a small element of the total solution domain in which the governing equation, if nonlinear, is linearized. The local analytic solution is then expressed in an algebraic form. The system of local analytic algebraic equations is solved to provide the numerical solution of the problem.

Subsequently, in a span of ten years, many students took interest in the development of the finite analytic method and its applications to fluid mechanics and heat transfer problems. They are Hamid Naseri-Neshat, Hamn-Ching Chen, Kuo-San Ho, Young Hwan Yoon, Che Hsi Yu, Sen-Ming Chang, Wenchung Chen, Zahed Mohammad Sheikholeslami, Tzong-Shyan Wung, Wu Sun Chen, Kemakolam Obasih, Seok Ki Choi, Vahid Talaie, Ramiro Humberto Bravo, and Hakan Aksoy. They all contributed to the further development of the finite analytic method. In 1983 a monograph entitled "The Finite Analytic Method" was published as part of the Iowa Institute of Hydraulic Research Report. There are a total of seven volumes in the monograph entitled "The Finite Analytic Method." The special feature of the finite analytic method is that when it is applied to solve the Navier-Stokes equations, it provides relatively accurate representations of the convection term. The finite analytic method not only provides accurate simulation of the upwinding effect because of its analytic nature of the solutions, but it also provides automatic, gradual shifts of the upwinding. Consequently, the finite analytic numerical solutions of convection diffusion equations minimize the false numerical diffusion that would occur in the upwinding difference used in other numerical methods and provide stable and fast convergency of the solutions.

Six years have passed since the publication of the monograph entitled "Finite Analytic Method." During these years the emphasis has been to apply the finite analytic method to various problems and to develop a more friendly code for users. This monograph thus is developed to document the efforts made in the applications of the finite analytic method along with its further improvements.

I would like to thank my colleagues, V.C. Patel, K.B. Chandran, T.F. Smith, A. T. Chwang, F. Stern, and K. Atkinson for their interest in the development and application of the finite analytic method. I would like to acknowledge the support of Drs. William D. McNally, Peter M Sockol, Gary Johnson, and J.J. Adamczyk of NASA Lewis Center for their support in the early development of the finite analytic method. My thanks also go to Dr. Oscar P. Manley of the U.S. Department of Energy for his support of the application of the finite analytic method in energy related problems. Recent applications of the finite analytic method to ship hydrodynamics problems have been supported by the Navy GHR Grant No. N0014-84-0068, by the Naval Sea System Command GHR Grant No. N00168-86-J-0019 administered by the David Taylor Naval Ship Research and Development Center, and by a recent grant from the Office of Naval Research under the Applied Hydrodynamics Research Grant No. N00167-86-K-0019.

In Volume I of the Finite Analytic Method and Its Application, laminar and turbulent flows past a two-dimensional and axisymmetric body are studied. I would like to thank Dr. Seok Ki Choi for applying the finite analytic method to complex flow problems. Without his participation, the finite analytic method would not have been developed and understood as it is today. I shall be happy to receive any discussion or criticism on the finite analytic method. I attempt to present the finite analytic method and its applications in a systematic documentation. Whenever possible, all the listings of the codes developed associated with the finite analytic method are enclosed so that readers may apply the finite analytic method in their problems.



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#### ABSTRACT

A numerical study of laminar and turbulent flows past two dimensional bodies and axisymmetric bodies is presented. Numerical methods are developed to solve Navier-Stokes equations for two dimensional and axisymmetric flows in the arbitrary geometries. The complex physical geometry is resolved by use of numerically generated, body-fitted coordinates. The governing equations are written in the transformed domain using the orthogonal velocity components as dependent variables for momentum equations. The governing equations are discretized using both the finite analytic method and the finite volume method. Both one velocity staggered grid method and two velocities staggered method are employed for grid arrangements. The velocity and pressure coupling techniques in these grid arrangements are presented. The solution procedure of the SIMPLER numerical algorithm is used with a parabolic marching technique and a global pressure calculation method. For turbulent flow calculations, both the k -  $\epsilon$  turbulence model and the twolayer turbulence model are used.

Calculations are performed for laminar and turbulent flows past a finite flat plate and turbulent flow past

axisymmetric bodies with different solution domains, numerical methods and turbulence models. Calculations include the development of a wake function method for the prediction of turbulent wake of a flat plate, predictions of laminar and turbulent flows past a finite flat plate, predictions of turbulent flow past axisymmetric bodies by the wall function method and by the two-layer turbulence model and predictions of turbulent flow past finite axisymmetric bodies. Comparisions of predictions by finite analytic method with those by finite volume method are made for some calculations. All the predicted results were compared with available experimental measurements. Good agreements between the predicted results and measured data were obtained.

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#### NOMENCLATURE

A, B : convection coefficients in the linerized

transport equation in Eq. (II-63).

 $A_{\varphi'}$   $B_{\varphi'}$   $D_{\varphi'}$   $E_{\varphi}$  : coefficients of the transport equation for

variable  $\phi$  in Eq.(II-60).

 $A_{E}$ ,  $A_{N}$ ,  $A_{N}$  : coefficients of algebraic equations.

As' Ap

 $A_{w}$  : wall surface area.

 $A_{\epsilon'}$   $A_{\mu}$  : constants in turbulence model.

B : constant in the law of the wall (=5.5).

b : half width of wake.

 $b_{\phi}$  : total source term for variable  $\phi$ .

b; : geometric coefficients.

 $C_{f} : friction coefficient ( = \frac{2\tau_{w}}{2} ).$ 

c<sub>nb</sub> : finite analytic coefficients.

 $C_{p} \qquad : \quad \text{pressure coefficient } (= \frac{2(p-p_{\infty})}{2}).$ 

 $c_{\mu'}$   $c_{D'}$   $c_{1'}$  : constants in turbulence model.

c<sub>21</sub>, c<sub>22</sub>,

 $\mathbf{D}_{\mathbf{N}}$  : mass source arised from non-orthogonality

of grid in Eq. (III-33).

mass source in pressure equation in

Eq.(III-40).

equation in Eq. (III-44).

D; : geometric coefficients.

 $D_1^u$ ,  $D_2^u$ ,  $D_1^v$ ,  $D_2^v$ : coefficients of pressure term in momentum

equation in body-fitted coordinates.

 $D_e$ ,  $D_w$ ,  $D_n$ ,  $D_s$ : diffusion terms in finite volume method.

 $d_{e'}$   $d_{w'}$   $d_{n'}$   $d_{s}$  : coefficients of pressure term in momentum

equation in cartesian coordinates.

 $d(\xi)$ : distance from the reference station to the

body surface at  $\xi$ -station.

E<sub>2</sub> : series summation term in Eq.(II-80).

F : source function in Eq. (II-35).

 $F_{e'}$ ,  $F_{w'}$ ,  $F_{n}$ ,  $F_{s}$ : convection terms in finite volume method.

f : grid control functions.

 $F^2$ ,  $F^A$ ,  $F^B$ ,  $F^C$  : grid control functions in  $\eta$ -direction.

G : generation term of turbulent kinetic

energy.

g, g<sup>ij</sup>, g<sub>ij</sub> : geometric coefficients.

h : grid size in local element.

J : Jacobian.

k : 1) turbulent kinetic energy.

2) grid size in local element.

k dimensionless turbulent kinetic energy.

 $\mathbf{k}_{\text{in}}$  : turbulent kinetic energy at inlet station.

 $\mathbf{k}_{\mathbf{w}}$  : turbulent kinetic energy at the wake

function region.

L : body length.

: turbulent length scale at inlet station.

 $l_{m'}$   $l_{t'}$   $l_{\epsilon'}$   $l_{\mu}$  : turbulent length scales.

n : normal distance from the wall.

n : dimensionless normal distance from the

wall.

n1, n2 : components of unit normal vector at wall.

P : pressure.

P : pressure correction.

q : magnitude of velocity vector.

 $q^{\xi}$ : velocity component in  $\xi$ -direction.

R : body radius.

R : maximum body radius.

Re : Reynolds number ( =  $\frac{U_{\infty}L}{v}$  ).

 $R_k$ : turbulent Reynolds number ( = Re n  $k^{1/2}$  ).

 $R_{\phi}$ : effective Reynolds number for variable  $\phi$ .

 $S_{\phi}$ ,  $S_{\phi}^{p}$ ,  $S_{\phi}^{c}$ ,  $S_{\phi}^{b}$  : source functions for variable  $\phi$ .

Tu : turbulent intensity.

 $T_{wx}'$   $T_{wv}$  : wall shear force in x,y directions.

u , v : velocity components.

u\*, v\* : star velocity components.

û, v : pseudovelocity components.

U , V : contravariant velocity components.

U\*, V\* : contravariant star velocity components.

 $\hat{\mathbf{U}}$  ,  $\hat{\mathbf{V}}$  : contravariant pseudovelocity components.

U : free stream velocity.

u : wake centerline velocity.

 $u_{\tau}$ : friction velocity  $\left( = \left( \frac{\tau_{w}}{\rho} \right)^{1/2} \right)$ .

 $\mathbf{u}_{\mathbf{TO}}$  : trailing edge friction velocity.

 $-u_1u_1$ : Reynolds shear stresses.

v : normal velocity component in the wake

function region.

w : velocity defect in the wake.

: centerline velocity defect in the wake.

x , y : Cartesian coordinates.

 $x^{+}$ ,  $y^{+}$ : dimensionless distance in x,y directions.

x , r : cylindrical coordinates.

#### Greek Symbols

 $\alpha_{u'}$ ,  $\alpha_{v'}$ ,  $\alpha_{p}$ , : under-relaxation factors.

 $\alpha_{k'}$   $\alpha_{\epsilon}$ 

 $\Delta_{\mathrm{p}}$  : dimensionless pressure gradient.

 $\Delta t$  : time step.

 $\Delta_{_{\overline{\tau}}}$  : dimensionless stress gradient.

 $\Delta x$ ,  $\Delta y$ : size of control volume in x,y direction.

 $\Delta v$  : volume of control volume.

 $\delta$  : boundary layer thickness.

 $\delta_{ij}$  : Kronecker delta.

 $\delta n$  : normal distance from the wall.

 $\delta x$ ,  $\delta y$ : distance between the pressure calculation

points.

ε : rate of turbulent kinetic energy

dissipation.

 $\epsilon^+$ : dimensionless dissipation rate.

 $\epsilon_{\text{in}}$  :  $\epsilon$  at inlet station.

 $\epsilon_{w}$ :  $\epsilon$  at wake function region.

 $\Gamma_{\!_{f \varphi}}$  : effective diffusion constant for  $\varphi$ .

 $\lambda_{m}$  : eigenvalues.

 $\lambda_{_{\mathbf{W}}}$  : coefficient in wall function.

μ : dynamic viscosity.

v : kinematic viscosity.

 $v_t$ : turbulent eddy viscosity.

 $\xi$ ,  $\eta$  : transformed coordinates.

 $\xi^*$ ,  $\eta^*$  : grid stretching functions.

 $\eta_{\text{ref}}$  : reference station.

θ : momentum thickness.

ρ : density.

τ. : wall shear stress.

transport quantities.

#### Subscripts

E, W, N, S, P : calculation points.

e, w, n, s : control volume surface.

nb : neighbouring nodal points.

x, y, t: first derivative with respect to x, y, t.

xx, yy: second derivative with respect to x, y.

 $\xi$ ,  $\eta$  : first derivative with respect to  $\xi$ ,  $\eta$ .

 $\xi\xi$ ,  $\eta\eta$  : second derivative with respect to  $\xi$ ,  $\eta$ .

to the description of the d

#### Superscripts

e, w, n, s : control volume surface.

P : calculation point.

n-1: (n-1) th time step.

• variables.

#### CHAPTER I

#### INTRODUCTION

#### I.1 Purpose of Study

Recent demands in advanced ship design have prompted many researchers to study flow past ship propulsion systems. Since most ship propellers are located at the downstream end of ship body, the study of flow past ship bodies is important for the design of optimal ship shape and propellers. However, the present state-of-the-art of prediction methods of flow past complex geometries is not yet capable of caculating the entire flow field past ship bodies. The investigations of flows past axisymmetric bodies can provide a fundamental understanding of flow field past more complex ship bodies. Studies of fluid flows past two dimensional bodies such as hydrofoils and appendages are also important for ship design since the understanding of flow field past appendages will provide more realistic simulation of inlet flow conditions for the propeller.

The purpose of the present study is to develop numerical calculation methods for predicting laminar and

turbulent flows past two dimensional and axisymmetric bodies. The present study starts with the prediction of laminar and turbulent flows past a thin flat plate and then turbulent flows past axisymmetric bodies of DTNSRDC (David Taylor Naval Ship Research and Development Center) are investigated in detail. These geometries are chosen not only because their geometries approximately resemble the appendages or ship body but also because of the availability of extensive experimental data to compare with the predicted results. The shapes of these bodies are presented with generated numerical grid in the following chapter.

In the following sections, the theoretical backgroud of present investigation is presented. It includes the review of numerical methods, grid generation techniques, calculation methods for incompressible flow in arbitrary geometry, and turbulence model.

#### I.2 Theoretical Background

Fluid flows past two dimensional or axisymmetric bodies are also encountered in a variety of practical engineering applications, for example, aerodynamics and turbomachineries. The most reliable information may be obtained by direct measurements. However, experimental

investigations are in most case expensive and time consuming. There also exist difficulties of measurement in many situations, and measuring instruments are not free from errors.

On the other hand, with the rapid development of computer technology in computational speed and size of storage, the computational methods became practical to simulate various flow phenomena encountered in many engineering problems. During the past twenty years, the computational methods for incompressible flow have been rapidly developed accompanied with the advances of practical turbulence model. Various computational methods have been proposed, tested and refined to a stage which may significantly impact the design of many engineering problems. Engineers and researchers begin to realize that the CFD (Computational Fluid Dynamics) is perhaps a cost effective and convenient way of analyzing the complex engineering problems.

Two numerical methodologies are the most commonly employed and developed, namely finite difference method and finite element method. Most flows in the engineering problems have rather arbitrary geometries. When the practical usage of calculation methods in arbitrary geometry is considered, the finite element method appears

to be the natural choice. However, the finite element method still has unresolved difficulties in the simulation of fluid flow phenomena although this method is widely used in other areas such as solid mechanics. By its rather simplicity and efficiency, the finite difference method has been the most widely used in the computational fluid dynamics. Among the various finite difference methods, the method developed by Patankar and Spalding [1,2] seems to be the most popular in the calculation of incompressible flows.

In addition to the finite difference method and the finite element method, a finite analytic method has been developed by Chen and Chen [3]. This method has been tested for the several practical engineering problems [4,5,6] and proved to be accurate and stable. In the finite analytic method, the algebraic representation of a certain nodal value with neighbouring nodal values are obtained by a local analytic solution of the governing equation. The novel nature of this method is that the numerical false diffusion problem in solving the Navier-Stokes equations, which is considered as the most serious problem for nearly all the numerical schemes of finite difference method, is satisfactorily minimized by using all the surrounding nodal points. The well developed calculation procedure for the finite difference method in

solving the Naviers-Stokes equations can be readily applied to finite analytic method without any difficulties. Both the finite analytic method and finite difference mothod are used for the several calculations presented in this study. Comparisions of predictions by these two methods are given for certain problems.

Recently, several calculation methods have been developed that employ boundary-fitted, curvilinear coordinate to appropriately handle fluid problems in complex geometries. The technique of generating an appropriate boundary fitted curvilinear coordinate and the development of related calculation procedure associated with using the curvilinear coordinate system have been subjects of numerous studies. Although the calculation methods for incompressible flow in the orthogonal grid system have been well developed and refined, those for non-orthogonal grid system seem to be not yet fully established. Detailed discussion of currently available calculation methods for incompressible flow associated with using the curvilinear coordinate system will be given in the following section.

Due to its importance in the engineering application, several numerical and experimental studies of laminar and turbulent flows past two dimensional or axisymmetric

bodies have been made during the last decade. Since this problem includes the leading edge interaction, boundary layer development on the body, the trailing edge interaction and wake development, it has been subject of testing of several calculation methods and turbulence models. At present, several reliable experimental informations are available which can be used to verify the accuracy of the calculation schemes or turbulence models. Detailed discussion of previous numerical and experimental studies is given in the chapter where each specific problem is mentioned.

Previous numerical and experimental studies indicate that although the first order boundary layer theory adequately describes flow fields over the middle of body, it fails to describe flow fields near the leading and trailing edge of a body and near the tail region of axisymmetric bodies. Two calculation methods have been widely used in order to appropriately handle these flow situations. The first method is the viscous-inviscid interaction method in which boundary layer solutions are matched with the external inviscid flows by interactive means. The second approach is the global numerical solutions of elliptic or partially parabolic form of Navier-Stokes equations. The latter approach is more attractive since it does not require another numerical

solution of inviscid flow and is adopted in the present study.

In many previous numerical studies of flow past ship bodies, calculations are started either at the middle of the body or at the trailing edge of the body with upstream conditions specified by well documented profiles from boundary layer theory or experimental data. Since these calculations do not include the leading edge interaction and initial development of boundary layer over the body, the resulting solutions are dependent on the upstream conditions or the location of upstream solution boundary. A more reliable numerical solution may be obtained by including the leading edge within the solution domain with prescribing uniform flow conditions at the inlet and with the solution domain large enough to capture the whole viscous-inviscid interaction. However, inclusion of leading edge in the solution domain may cause the difficulties of turbulence modelling in the transition region for turbulent flow calculation. In the present study, the upstream solution boundary is made to locate either at the uniform flow region far upstream of body or at the middle of the body according to the objective of the problem considered.

Since the problems considered in the present study have rather arbitrary geometries which require the use of boundary-fitted curvilinear coordinate system, a brief review of methods for the generation of boundary-fitted coordinates and available calculation methods for incompressible flow in arbitrary geometryis is presented. A brief discussion of available turbulence models will be also presented.

#### I.3 Generation of Boundary-Fitted Coordinates

A boundary-fitted coordinate system is defined as a curvilinear coordinate system in which the boundaries of the physical domain concide with a curvilinear coordinate line or surface. The generation of an appropriate computational grid is very important in order to achieve the accuracy and better convergence of numerical solution. Boundary-fitted curvilinear coordinates can be generated orthogonally or non-orthogonally. The orthogonal grid has the advantages that the transformed partial differential equations are simpler as the non-orthogonal terms do not appear. This advantage results in fewer computing time, fast convergence as well as better stability and accuracy of the solution. However, orthogonal coordinates are often difficult to generate and it is sometimes impossible

to generate the orthogonal coordinate for the three dimensional situations. An additional disadvantage for the generation of orthogonal coordinate is the fact that there is no control on the location of the grid points along the boundary which may deteriorate the grid spacing near the solid boundary where the appropriate grid spacing is required. Non-orthogonal coordinates are much easier to generate and can be produced also for three dimensional situations. Further, concentration of grid lines in the regions where good resolution is required is much easier to achieve. However, non-orthogonal coordinate introduce additional terms such as cross derivatives which may reduce both convergence and stability of numerical solution and, thereby, increase the computing time.

There exist several ways of the generating boundaryfitted coordinates. The available grid generation
techniques can be broadly classified into two categories,
algebraic methods and partial differential equation
methods. The multi-surface technique of Eiseman [7] is a
typical method for algebraic method in which simple
functions are combined to generate grids for complex
geometries. In this approach, the grid is generated by
joining corresponding points on the inner and outer
boundaries by polynomial curves. In general, the
algebraic grid generation techniques are very attractive

by the reasons that they do not require a numerical solution of partial differential equations and a precise control over the grid spacing is possible. However, when this method is applied to a complex geometry, non-smoothing grids may be produced.

Boundary-fitted coordinates can also be generated by the solution of partial differential equations in which the dependent variables are the grid coordinates in the physical domain. Conformal mapping is a special case of grid generation technique using the Laplace equation. Much of the works have been done by Thompson and his coworkers [8]. The spacing between the grid lines is strongly dependent on the equations being solved and weakly dependent on the boundary point distributions. The equations can be easily changed by varying the values of the source term or the grid control functions in the Poisson equations. These grid control functions can be selected to appropriately attract the coordinate line toward particular grid points or grid lines or repel the coordinate lines. Thompson et al. [8] have suggested a series of exponential functions as source terms. the selection of grid control function is quite dependent on the problem being solved.

In the present study, all the numerical grids are generated by the solution of the Poisson type of partial differential equations with grid control functions specified properly depending on the physical situations being solved. Details of grid generation techniques adopted in the present study are given in chapter-II.

### I.4 Calculation Methods for Incompressible Flow in Complex Geometries

I.4.1 Calculation Methods for Incompressible Flow in Orthogonal Coordinate System

The computational method for the prediction of fluid flow in the orthogonal grid system is well developed and have been widely used for a variety of problems. The orthogonal grid based calculation method is not much depart from that for Cartesian counterparts. The well developed calculation procedure for Cartesian coordinate system can be easily modified with a proper specification of geometric coefficients and source terms. Most of previous calculations use the staggered grid arrangement and the velocity components normal to the control volume surfaces (contravariant velocity components) are selected as the dependent variables in the momentum equations.

Pope [9] used such a orthogonal based calculation procedure to compute turbulent recirculating flows in diffusers, Gosman and Rapley [10] applied a similiar method to the calculation of fully developed flow in the ducts of arbitrary cross section. Recently, Raithby et al. [11] have presented a new calculation procedure in which the stresses are retained in the discretization equation instead of the usual procedure of substituting them in terms of strain rates.

However, the orthogonal coordinate based methods have limitations in the application due to the difficulty of generating appropriate numerical grid. For the sake of general application, the calculation methods for non-orthogonal coordinate system should be investigated.

## I.4.2 Calculation Methods for Incompressible Flow in Non-orthogonal Coordinate System

Unlike the orthogonal coordinate based methods, several calculation methods for the non-orthogonal coordinate system have been proposed during the late 1970s and during the 1980s. The differences among these methods are the choice of dependent variables in the momentum equations, the grid arrangements and the treatment of pressure and velocity coupling. One interesting fact is that none of these methods have superiority over other

methods to justify its general usage. Each of the methods has its own merits and demerits which should be judged in terms of the problem being considered. As compared with the method based on the orthogonal coordinate system, these methods are still in a developing stage. Among the several calculation methods based on non-orthogoal coordinate system, five typical methods which use different grid arrangements or dependent varibles as shown in Fig.I-1 are discussed below.

#### Non-Staggered Grid Method

In the first grid arrangement, which is shown in the Fig.I-1-a, all the dependent variables are computed and stored at the same location and the Cartesian velocity components are used as dependent variables in the momentum equation. This method has been named differently according to the author's choice. For example,  $P - \Omega$  scheme by Hsu [12]; Momentum Interpolation Method by Majumdar [13]; Pressure Weighted Interpolation Method by Miller and Schmidt [14]; Collocation Method by Peric et al. [15]; and, Non-Staggered Grid Method by Rhie and Chow [16]. Since this method uses Cartesian velocity components as dependent variables for the momentum equation, the governing equation is simple and the curvature terms which are extremely grid dependent can be

avoided. Moreover, a strongly conservative form of transport equation is possible which is a desired characteristics for finite volume method. As is discussed in Patankar [2], this grid arrangement may give rise to a checkerboard pressure oscillation. To overcome this checkerboard splitting of pressure field, a special kind of interpolation method for evaluating velocity components at the control volume cell surface has been devised. All the transport equations are solved at the center point of control volume cell and the cell surface velocities for the derivation of pressure or pressure correction equation are obtained by a linear interpolation using neighbouring nodal values except the pressure gradient term in the momentum equation is evaluated by the method employed in the staggered grid approach to prevent the splitting of the pressure field. Thus, this method indirectly uses the staggering idea and it was questioned that this method can be named as non-staggered method [17]. Since all the variables are calculated at the same point, the coefficients of algebraic equations are the same for all the variables which may reduce the computer storage and computing time, especially for the three dimensional situations. This feature will lead to more cost effective calculation when the multigrid method is employed. earlier method by Rhie and Chow [16] or Peric [18] has

been blamed for the fact that the resulting converged solution is quite relaxation factor or time step dependent. Recently, Majumdar [13,19] and Miller and Schmidt [14] removed this problem by a rigorous derivation. This method has been successfuly applied to a variety of engineering problems by many researchers. However, Miller and Schmidt [14] find that this method may result in a physically unrealistic solution in regions where there is a strong pressure gradient. This method also suffers from the lack of diagonal dominance of pressure correction equation when it is applied to strongly non-orthogonal grid. This method has been applied to a variety of problems; Rhie and Chow [16], Rhie and coworkers [20,21], Peric [18], Han [22], Majumdar [13,19], Majumdar et al. [17], Rodi et al. [23], Miller and Schmidt [14] and Peric et al. [15]. An excellent discussion of this method is given in Majumdar et al. [17].

## One Velocity Staggered Grid Method

Shyy et al. [24] developed a calculation method employing the conventional staggered grid usually adopted in the Cartesian coordinate system. As shown in the Fig.I-1-b, the dependent variables in the momentum equations are the Cartesian velocity components and only

one velocity component is stored at the each cell surface. Since only one velocity component is available at each cell surface, the other unavailable velocity component which is necessary to compute the mass flow rate is usually obtained through the linear interpolation of neighbouring velocity components which are obtained in the previous iteration. In addition to this defficiency, further approximations have to be made, for example neglection of non-orthogonal pressure gradient terms, to provide the diagonal dominant pressure correction equation in strongly non-othorgonal grid. A more serious drawback of this method is that if the flow direction is normal to the direction of velocity component stored at the cell surface, zero convective mass fluxes across the control volume faces may occur and the pressure gradient driving the velocity components will be completely wrong, which may cause undesired pressure splitting. However, use of this method is justified when the flow direction is not much deviated from the direction of velocity components stored at the cell surface. Due to the simplicity of this method, many researchers used this method for the problem to which this method can be applied. For example, Braaten and Shyy [25], Nakayama [26], Ha [27], Chen and Patel [4], Cheng and Chen [5], Obashi and Chen [6], Patel et al. [28] and Choi and Chen [29].

#### Two Velocities Staggered Grid Method

Discussions of the previous method suggest that in order to calculate flow fields around arbitrary geometries, both of the Cartesian velocity components should be stored at each cell surface as shown in Fig. I-1c, while pressure and turbulent quantities are stored at the center point of control volume cell. Maliska and Raithby [30] adopted this configuration in the development of three dimensional parabolic calculation procedure for the fluid flow in the arbitrary cross sectioned ducts. This method is also not free from difficulties. In order to obtain the diagonal dominant pressure correction equation in the strongly non-orthogonal grid, the nonorthogonal pressure gradient term should be neglected. Storing the two velocity components at each control volume surface requires a complex programing and more computer storage and more computing time. These disadvantages became more grave in three dimensional situations. This method is not commonly used due to forementioned disadvantages.

#### Algebraic Manipulation Method

An alternative to the Cartesian velocity components is to use the curvilinear velocity components as the

dependent variables in the momentum equations. contravariant or the covariant velocity components will be the natural choices due to their relationship with the grid lines. Karki and Patankar [31] developed a calculation method using covariant velocity components as the dependent variables in the momentum equations. discretization equations and source terms for covariant velocity components were obtained by the algebraic manipulation of discretization equation and source terms based on the Cartesian velocity components. As shown in the Fig.I-1-e, each covariant velocity component is stored at the control volume cell surface using staggering idea. The usage of covariant velocity components as the dependent variable in the momentum equation enables the strongly diagonal dominant pressure correction equation even in the strongly non-orthogonal grid situations. complicated tensor algebra is avoided through a novel algebraic manipulation of discretization equation and the resulting algebraic equations seem to be cost effective and less grid dependent. The success of this method is largely dependent on the accuracy and grid dependency of the algebraic manipulation of source term of momentum equation which is considered as the most serious problem when the contravariant or covariant velocity components are adopted as a dependent variables. This method should

be tested for complicated three dimensional situations to justify its general usage. This method has been successfully applied to calculation of compressible and incompressible in two dimensional complex geometries [32,33]. Detailed study of this method is provided by Karki [34].

It is worthy to mention the calculation method based on the full transformation of dependent variables for momentum equations using a complicated tensor algabra. Demirdzic et al. [35] developed such a calculation method using contravariant velocity components as dependent variables for momentum equations. Fig.I-1-d shows that the only one contravariant velocity component is stored at the each control volume cell surface and the staggering idea is adopted. This method requires a complicated tensor algebra and more storages for the geometric coefficients. Moreover, the resulting governing equation is extremely complicate and the numerical solution is quite grid dependent. This fact restricts the usage of this method in certain situations. Like all the methods discussed previously, this method also gives a nine point pressure correction equation which lacks diagonal dominance in strongly non-orthogonal grid situations if the non-orthogonal pressure gradient terms are not neglected. The advantage of smaller numerical diffusion

in this approach must be judged against the serious disadvantages mentioned above. This method has been used by few people. For example, Demirdzic et al. [35], Demirdzic [36], Gal-Chen et al. [37], Stern et al. [38] and Richmond [39]. An excellent study of this method is given by Demirdzic [36].

Methods of Vanka et al. [40] and Faghri et al. [41] deserve to receive attention. However, these methods are also not free from many difficulties mentioned in the previous methods and are not commonly used by many researchers.

The one-velocity staggered grid method is adopted for the most of calculations of the present study since this method is very easy to program and the flow direction is not much deviated from the direction of velocity component stored at cell surface with an appropriate grid generation. The two-velocities staggered grid method is also used for some calculations in the present study with some modifications made from the original method of Maliska and Raithby [30].

#### I.5 Turbulence Models

During the last decade, many turbulence models ranging from the Prandtl mixing-length model [42] to the k

- E turbulence model [43] were used for a variety of practical calculations and tested in order to find out their range of applicability. Some progress has been made, but to date no model has been found to be both accurate and general. The models widely used in applications have been based on the Boussinesq (1877) assumption which relates the turbulent stresses to mean rates of strain by

$$-\frac{\partial u_{i}u_{j}}{\partial x_{j}} = v_{t} \left( \frac{\partial u_{i}}{\partial x_{j}} + \frac{\partial u_{j}}{\partial x_{i}} \right) - \frac{2}{3} \delta_{ij} k \qquad (I-1)$$

where  $\mathbf{v}_{\mathsf{t}}$  is turbulent eddy viscosity and k is turbulent kinetic energy.

For a suitable charateristic length scale  $l_{t}$  and velocity scale  $v_{t}$ , dimensional analysis suggests that turbulent eddy viscosity  $v_{t}$  can be evaluated as

$$\mathbf{v}_{+} = \mathbf{v}_{+} \mathbf{1}_{+} \tag{I-2}$$

The difference among the existing models based on the Boussinesq assumption is how velocity scale  $\mathbf{v}_t$  and length scale  $\mathbf{l}_t$  are specified. Experimental evidence indicates that the Boussinesq assumption is reasonably valid in many flow circumtances with exception of some flow situations. Models based on the Boussinesq assumption are frequently called eddy viscosity model.

Turbulence models are often classified according to the number of supplementary partial differential equations that must be solved in order to supply the modelling parameters. Since details of these models are available in the various literatures, for example Chen [44], only a brief discussion of current available turbulence models will be given.

## I.5.1 Zero Equation Turbulence Model

In the zero equation model or algebraic model, such as proposed by Cebeci and Smith [45] or Baldwin and Lomax [46], the eddy viscosity is prescribed from length scale and velocity gradient.

$$v_{t} = (1_{t})^{2} \left| \frac{\partial U}{\partial y} \right| \tag{I-3}$$

The length scale l<sub>t</sub> is usually obtained from the empirical correlations developed for the boundary layers. The algebraic models have proven to be accurate and reliable for relatively simple flows. The disadvantage of this model is the lack of generality that the length scale which is needed for specification of eddy viscosity is function of various parameters and it is not easy to specify an appropriate length scale over the whole flow field, especially for the separated flow region or the wake region. However, these models can be employed all

the way to the wall where the viscosity effect is important and the numerical solutions of partial differential equations are not needed for the specification of length scale.

#### I.5.2 One Equation Turbulence Model

This model is based on the suggestion of Prandtl and Kolomogorov that the turbulent velocity scale is proportional to the square root of turbulent kinetic energy k, implying;

$$v_t = C_{\mu} k^{1/2} l_{\mu}$$
 (I-4)

This model requires the numerical solution of turbulent kinetic energy equation which can be derived from the Navier-Stokes equations. The turbulent kinetic energy equation contains a diffusion term, a generation term and a dissipation term which must be modelled through additional assumptions such as;

$$\varepsilon = c_{D} - \frac{k^{3/2}}{1s}$$
 (I-5)

which requires specification of another length scale  $\mathbf{l}_{\mathbf{E}}.$ 

There exist several one equation models [47,48,49] and the differences among the these models are mainly how the length scales  $l_{\mu}$ ,  $l_{\epsilon}$  are specified. In general, the

predictions of the one equation model have been marginally better than those obtained from zero equation models.

#### I.5.3 k - & Turbulence Model

The k -  $\epsilon$  turbulence model [43] is usually called two equation model. In this model, the eddy viscosity is related to the turbulent kinetic energy k and its dissipation rate  $\epsilon$ ;

$$v_{t} = C_{\mu} \frac{k^{2}}{\epsilon} \tag{I-6}$$

The turbulent dissipation rate  $\epsilon$  is assumed to be related to the length scale through

$$l_{t} = C_{D} \frac{k^{3/2}}{\varepsilon}$$
 (I-7)

The turbulent kinetic energy k and its dissipation rate & are determined from two modelled equations. Thus the eddy viscosity and the length scale are obtained from the numerical solutions of partial differential equations. Since this model does not require algebraic specification of length scale, it can be applied to several flow situations.

The  $k-\epsilon$  turbulence model can only be applied to the fully turbulent region and calculations of the viscosity-affected near wall region is avoided by the use of wall functions. The wall function method [43] has been found

to be quite successful for attached flow, it is not suitable for some flow situations. The wall functions relating the velocity and turbulent quantities at the second grid point to friction velocity heavily lean on the assumptions of a logarithmic velocity distribution and the validity of local equilibrium of turbulence. These assumptions are not valid in the separated flow region. Furthermore, the extension of wall function method to unsteady flow and three dimensional flow requires additional assumptions which are not substantiated by experiment or theory [50]. An alternative to the use of wall function method will be to employ the turbulence model which are valid all the way to the wall.

#### I.5.4 Low Reynolds Number Turbulence Model

Several low Reynolds number extensions of the  $k-\epsilon$  turbulence model [51,52,53] which can be applicable to the viscous affected layer have been proposed. These models introduce damping functions in order to achieve the observed reduction of turbulent transport very near the wall. However, these models have an undesirable feature of requiring very high numerical resolution near the wall region because of the steep gradient of the dissipation rate  $\epsilon$ . It was found that all these models perform rather poorly in adverse pressure gradient boundary layers [54]

and in separated flows [55]. Patel et al. [50] reviewed the several available low Reynolds number  $k-\epsilon$  turbulence models and concluded that none of the these models can be used confidently even in the boundary layer calculations.

#### I.5.5 Two-Layer Turbulence Model

In order to reduce the computational effort and to preserve numerical stability, the well established length scale distribution near the wall region can be introduced to the calculation of the vicosity-affected near wall region instead of using the wall function method while the outer, fully turbulent region is resolved by use of the k - £ turbulence model. This model is named as two-layer model and it is usually used with the combination of the k - £ turbulence model and zero equation or one equation turbulence model. Some successes in the prediction of complex turbulent flows by use of this model is reported [56,57,58,59,60].

In the present study, the  $k-\epsilon$  turbulence model with wall function method will be employed for most of turbulent flow calculations while the two-layer model is applied to some flow situations involving the pressure gradient and body curvature effects to improve the accuracy of the calculations.

## I.6 Outline of Study

In chapter II, mathematical and numerical formulations used in the present study are presented. The governing equations, boundary conditions, methods of generation of boundary-fitted coordinates and dicretization schemes are discussed.

In chapter III, numerical aspects are discussed.

These include the coupling between the continuity equation and momentum equations, numerical algorithm and overall solution procedures.

Chapters IV to VII are devoted to the numerical calculations which include development of the wake function method for the prediction of flat plate wake, prediction of laminar and turbulent flows past a finite flat plate, numerical solutions of turbulent flow past axisymmetric bodies by wall function method and by two layer model, prediction of turbulent flow past finite axisymmetric bodies. Some comparisions of the predictions by finite analytic method with those by finite volume method are presented. All the calculted results are compared with available experimental data to demonstrate the applicability and accuracy of the numerical scheme.

In chapter VIII, a brief summary of the present study is given and some suggestions for future work are discussed.

# CHAPTER II

#### II.1 Introduction

FORMULATION OF PROBLEM

In this chapter, the mathematical and numerical formulation of the present study is presented. This chapter starts with the mathematical formulation of the problem which includes governing equations, boundary conditions and solution domains. Then the grid generation techniques and discretization methods employed in the present study are presented.

The solution domains are made large enough to capture the whole important feature of flow field. The numerical grids are generated through the numerical solutions of Poisson equations in which the dependent variables are the physical coordinate of solution domain. The governing equations are written in the transformed domain using the partial transformation where the original Cartesian or cylindrical velocity components are left as dependent variables for momentum equations. These transformed governing equations are discretized using both finite analytic method and finite volume method.

#### II.2 Governing Equations

The continuity equation and general form of transport equations for the incompressible flow in Cartesian or in cylindrical coordinate system with the  $k-\epsilon$  turbulence model can be written as follow;

$$\frac{\partial}{\partial x}(\rho r u) + \frac{\partial}{\partial y}(\rho r v) = 0$$

$$\frac{\partial}{\partial t}(\rho r \phi) + \frac{\partial}{\partial x}(\rho r u \phi) + \frac{\partial}{\partial y}(\rho r v \phi)$$

$$= \frac{\partial}{\partial x}(r \Gamma_{\phi} \frac{\partial \phi}{\partial x}) + \frac{\partial}{\partial y}(r \Gamma_{\phi} \frac{\partial \phi}{\partial y}) + r S_{\phi}$$
(II-1)

In these equations,  $\phi$  represents the general dependent variables ( u, v, k,  $\epsilon$  ),  $\rho$  is the density of fluid,  $\Gamma_{\phi}$  is the effective diffusion coefficient, ( u, v ) are the velocity components in ( x, y ) directions and  $S_{\phi}$  denotes the source term for the variable  $\phi$ . For two dimensional flow, r = 1 and for axisymmetric flow, y = r. Details of the definition of all the variables are given in Table 1.

#### II.3 Solution Domains and Boundary Conditions

#### II.3.1 Solution Domains

All the calculations presented in the present study can be broadly classified into two cartegories; half body calculations and full body calculations. The difference between these two calculations is the location of the upstream solution boundary as shown in Fig. II-1. In the half body calculations, calculations start at the middle of body with inlet conditions specified by the well documented profiles from the boundary layer theory. the full body calculations, calculations start far upstream of body with inlet conditions specified by uniform flow conditions. The solution domain in the normal direction and in the downstream direction is made large enough to capture the whole viscous-inviscid interaction and wake development. The location of upstream inlet solution boundary in the full body calculations is also made far away from the body to capture the whole leading edge interaction of the solution domains used in the present calculations are given in Tables 2 to 6.

#### II.3.2 Boundary Conditions

The boundary conditions for all the problems considered in the present study can be stated as follows;

Inlet or Upstream Boundary (  $x = x_i$  )

The upstream inlet solution boundary is located either at the middle of the body or at the uniform flow region far upstream of the body. The u-velocity component and turbulent quantities k,  $\epsilon$  are prescribed from the simple flat-plate correlations for the half body calculations and from uniform flow conditions for the full body calculations. For v-velocity component, the condition of  $v_x = 0$  is specified for all the calculations.

Outlet or Downstream Boundary (  $x = x_d$  )

The downstream outlet condition is placed in the wake region far downstream of body. The zero pressure-gradient condition  $p_x = 0$  is specified at the outlet boundary. For the exit boundary conditions for transport quantities ( u, v, k,  $\epsilon$ ),  $u_x = v_x = k_x = \epsilon_x = 0$  conditions are specified.

Body Surface

The no-slip boundary condition ( u = v = 0 ) is specified for all the laminar flow calculations and for

the turbulent flow calculations when the two layer model is employed to calculate the flow field all the way to the wall. For all the other turbulent flow calculations, the wall function method is employed in order to avoid the use of large number of grids to resolve the steep gradient in the near wall region and uncertanties of the turbulence model in the viscous-affected region.

Upper Boundary (  $y = y_{11}$  )

The upper boundary is placed at a large distance from the body where the flow is assumed to be uniform. The uniform boundary condition is;

$$u = 1, p = 0, k_v = \varepsilon_v = 0.$$
 (II-3)

The v-velocity component in this boundary is obtained from the law of conservation of mass within the computational control volume cell during the solution process.

Wake Centerline ( y = 0 )

The boundary conditions along the wake centerline are the symmetry conditions and are specified as

$$v = 0$$
,  $u_y = k_y = \varepsilon_y = 0$ . (II-4)

#### TI.4. Numerical Grid Generation

The boundary-fitted coordinate generation technique proposed by Thompson et al. [8] is employed for the generation of numerical grid in the present study. The complex solution domain in physical coordinates ( x, y) is transformed to a simple rectangular domain in non-orthogonal, body-fitted coordinates (  $\xi$ ,  $\eta$  ) by the solutions of the Poisson equations;

$$\frac{\partial^2 \xi}{\partial x^2} + \frac{a_c}{r} \frac{\partial \xi}{\partial y} + \frac{\partial^2 \xi}{\partial y^2} = f^1(\xi, \eta)$$
 (II-5)

$$\frac{\partial^2 \eta}{\partial x^2} + \frac{a_c}{r} \frac{\partial \eta}{\partial y} + \frac{\partial^2 \eta}{\partial v^2} = f^2(\xi, \eta)$$
 (II-6)

where  $f^1$  and  $f^2$  are the grid control functions which are chosen priori to obtain the desired distribution of grid points in the physical (x, y) domain. In these equations, r = 1,  $a_C = 0$  for a Cartesian coordnate system and y = r and  $a_C = 1$  for a cylindrical coordinate system. The origin of coordinate system is located at the leading edge of body.

The numerical grid is generated by solution of inverted forms of these equations where the dependent variables are the physical coordinates of solution domain.

$$g^{11}\frac{\partial^{2}x}{\partial\xi^{2}} + g^{22}\frac{\partial^{2}x}{\partial\eta^{2}} + 2g^{12}\frac{\partial^{2}x}{\partial\xi\partial\eta} + f^{1}\frac{\partial x}{\partial\xi} + f^{2}\frac{\partial x}{\partial\eta} = 0 \qquad (II-7)$$

$$g^{11}\frac{\partial^{2}y}{\partial\xi^{2}} + g^{22}\frac{\partial^{2}y}{\partial\eta^{2}} + 2g^{12}\frac{\partial^{2}y}{\partial\xi\partial\eta} + f^{1}\frac{\partial y}{\partial\xi} + f^{2}\frac{\partial y}{\partial\eta} = \frac{a_{c}}{r} \quad (II-8)$$

where

$$g g^{11} = r^2 (x_n^2 + y_n^2)$$
 (II-9)

$$g g^{22} = r^2 (x_{\xi}^2 + y_{\xi}^2)$$
 (II-10)

$$g g^{12} = -r^2 (x_{\xi} x_{\eta} + y_{\xi} y_{\eta})$$
 (II-11)

$$g = r^2 (x_{\xi} y_{\eta} - x_{\eta} y_{\xi})^2$$
 (II-12)

The grid generation techniques outlined below are essentially the same as those reported in Chen and Patel [4] or Cheng and Chen [5]. However, some modifications are made for certain problems.

#### II.4.1 Generation of Numerical Grids for Flat Plate

Non-uniform rectangular numerical grids are generated for the calculation of laminar and turbulent flow past a flat plate with a proper grid concentration made near the wall and near the leading and trailing edges. The numerical grid in the normal direction is generated algebraically instead of solving the differential equation. The first few grids near the plate are generated uniformly and next the other grids are generated

non-uniformly with the grid expansion ratio about 1.2 to 1.3. The size of the first grid in the normal direction from the plate is adjusted according to the physical situations being considered. The numerical grid in x-direction is generated by the numerical solution of the following differential equation which is obtained from Eq.(II-7).

$$g^{11} \frac{\partial^2 x}{\partial \xi^2} + f^1 \frac{\partial x}{\partial \xi} = 0$$
 (II-13)

The grid control function f<sup>1</sup> is selected by following equations which is previously used by Chen and Patel [4] or Cheng and Chen [5];

$$f^{1}/2g^{11} = A_{1}$$
  $0.0 \le Z_{1} \le 0.5$ 

$$A_{1} \sin(\pi Z_{1}) \quad 0.5 \le Z_{1} \le 2 \qquad (II-14)$$

$$A_{2} \sin(\pi Z_{2}) \quad 0.0 \le Z_{2} \le 1.5$$

$$-A_{2} \quad 1.5 \le Z_{2}$$

where

$$z_1 = \frac{\xi - 1}{\xi_1 - 1}, \quad z_2 = \frac{\xi - 2\xi_1 + 1}{\xi_2 - 2\xi_1 + 1}$$
 (II-15)

The terms  $\xi_1$  and  $\xi_2$  correspond to the leading and trailing edge stations as shown in Fig.II-2 and A $_1$  and A $_2$ 

are positive constants which can be adjusted to yield the desired grid concentration near the leading and trailing edges.

The partial view of generated numerical grids used for laminar and turbulent flow calculations are shown in Fig.II-3. As shown in the figures, an appropriate grid concentration was made near the wall region and near the leading and trailing edge regions and the desired grid expansion in the wake region is also achieved.

# II.4.2 Generation of Numerical Grids for Axisymmetric Bodies

Body fitted coordinates for axisymmetric bodies are generated by the numerical solutions of Poisson equations, Eq.(II-7) and Eq.(II-8). In the present study, the constant-x lines are chosen as constant- $\xi$  lines to facilitate the comparision of numerical results with experimental data. Then, Eq.(II-7) and Eq.(II-8) can be rewritten as following simplified form.

$$g^{11}\frac{\partial^2 x}{\partial \xi^2} + f^{1}\frac{\partial x}{\partial \xi} = 0$$
 (II-16)

$$g^{11}\frac{\partial^{2}r}{\partial\xi^{2}} + g^{22}\frac{\partial^{2}r}{\partial\eta^{2}} + 2g^{12}\frac{\partial^{2}r}{\partial\xi\partial\eta} + f^{1}\frac{\partial r}{\partial\xi} + F^{2}\frac{\partial r}{\partial\eta} = 0 \quad (II-17)$$

where 
$$F^2 = f^2 - \frac{1}{rr\eta}$$
 (II-18)

The x-coordinates are algebraically generated instead of solving Eq.(II-16). The x-coordinate over the body and in the wake region near the trailing edge of body (x/L < 1.1) is generated uniformly while x-coordinate in the wake region away from the body (x/L > 1.1) is generated nonuniformly with grid expansion ratio about 1.2 to 1.3. The grid control function  $f^1$  is then determined from following equation using the x-coordinate already generated.

$$f^{1} = -g^{11} \frac{x\xi\xi}{x\xi}$$
 (II-19)

With  $f^1$  specified by Eq.(II-19), Eq.(II-17) can be solved with a proper specification of grid control function  $F^2$ . The resulting numerical solution gives the grid distribution in the radial direction.

Along the inlet and outlet boundary where the grid is orthogonal, Eq.(II-17) can be written as following.

$$g^{22}\frac{\partial^{2}r}{\partial\eta^{2}} + F^{2}\frac{\partial r}{\partial\eta} = 0$$
 at  $\xi = 1$  and  $\xi = \xi_{\text{max}}$  (II-20)

Thus the grid control function F<sup>2</sup> along these boundaries can be determined from Eq.(II-20) if the r-coordinate at these boundary is provided.

$$F_{A}(\eta) = F^{2}(1,\eta) = -g^{22} \frac{r_{\eta\eta}}{r_{\eta}} | \xi = 1$$
 (II-21)

$$F_B(\eta) = F^2(\xi_{max}, \eta) = -g^{22} \frac{r_{\eta\eta}}{r_{\eta}} | \xi = \xi_{max}$$
 (II-22)

where  $\xi$  = 1 is the upstream inlet station and  $\xi$  =  $\xi_{max}$  is the downstream outlet station.

The value of  ${\bf F}^2$  inside the solution domain can be obtained by a linear combination of  ${\bf F}_A$  and  ${\bf F}_B$ .

$$F^{2}(\xi,\eta) = F_{A}(\eta) \qquad 1 < \xi < \xi_{A} \qquad (II-23)$$

$$F_{C}(\xi,\eta) \qquad \xi_{A} < \xi < \xi_{B}$$

$$F_{B}(\eta) \qquad \xi_{B} < \xi < \xi_{max}$$

where

$$\begin{aligned} \mathbf{F}_{C}(\xi,\eta) &= \left[ (\mathbf{x}(\xi_{B}) - \mathbf{x}(\xi)) \mathbf{F}_{A}(\eta) + (\mathbf{x}(\xi) - \mathbf{x}(\xi_{A})) \mathbf{F}_{B}(\eta) \right] \\ & / \left[ \mathbf{x}(\xi_{B}) - \mathbf{x}(\xi_{A}) \right] \end{aligned} \tag{II-24}$$

and  $\xi_B$  are determined from the body shape. In the case of half body calculation,  $\xi_A$  is placed at the station where radius of body is initially changed and  $\xi_B$  is placed at the trailing edge of body as shown in Fig.II-2. However, the specification of  $F^2(\xi,\eta)$  is quite problem dependent and can be adjusted to obtain the desired grid distribution depending on the shape of geometry.

With the specification of proper grid control functions  $f^1$  and  $F^2$ , Eq.(II-17) is solved by finite

difference method. Eq.(II-17) is discretized as following using the exponential scheme of Spalding [4].

( 2a g<sup>11</sup> coth a + 2b g<sup>22</sup> coth b )
$$\xi,\eta$$
  $r\xi,\eta$   
= ( 2a g<sup>11</sup> csch a ) $\xi,\eta$  ( e<sup>-a</sup>  $r\xi+1,\eta$  + e<sup>a</sup>  $r\xi-1,\eta$  )  
+ ( 2b g<sup>22</sup> csch b ) $\xi,\eta$  ( e<sup>-b</sup>  $r\xi,\eta+1$  + e<sup>b</sup>  $r\xi,\eta-1$  )  
+ 2 (g<sup>12</sup>) $\xi,\eta$  (  $r\xi+1,\eta+1$  +  $r\xi-1,\eta-1$  -  $r\xi-1,\eta+1$  -  $r\xi+1,\eta-1$  )  
(II-25)

where

$$2a = -\frac{f^{1}}{g^{11}} | \xi, \eta$$
 and  $2b = -\frac{F^{2}}{g^{22}} | \xi, \eta$  (II-26)

The above system of algebraic equation is solved by the tridiagonal-matrix algorithm.

The body fitted coordinate system for full body calculation was obtained with a slightly different specification of grid control function  $F^2(\xi,\eta)$ . In order to attract grid lines toward body surface in the leading edge region of body, the following grid control function  $F^2(\xi,\eta)$  was devised.

$$F^{2}(\xi,\eta) = [(d(\xi_{B})-d(\xi))F_{A}(\eta) + (d(\xi)-d(\xi_{A}))F_{B}(\eta)]$$

$$/ [d(\xi_{B})-d(\xi_{A})] \qquad (II-27)$$

where 
$$d(\xi) = r(\xi, \eta_{ref}) - r(\xi, 1)$$
 (II-28)

In Eq.(II-27), the station  $\xi=\xi_A$  is the station where d( $\xi$ ) is minimum and the station  $\xi=\xi_B$  is the station where d( $\xi$ ) is maximum as shown in Fig.II-2. The grid control functions at these stations,  $F_A(\eta)$ ,  $F_B(\eta)$  are evaluated using Eq.(II-21) and Eq.(II-22) as the same way as done in half body calculation. The normal reference station  $\eta=\eta_{\rm ref}$  which is shown in Fig.II-2 was adjusted to obtain the desired grid concentration toward body and  $\eta_{\rm ref}=\eta_{\rm max}$  - 5 is used for most calculations.

As seen from the Fig.II-4 and Fig.II-5, the boundary-fitted coordinates generated by above method evolve smoothly from the body into the wake and the desired grid expansion in the tail region and in the wake region is obtained.

#### II.5 Finite Analytic Method

The non-dimensionized form of general transport equation in the Cartesian coordinate system can be written as follows;

$$\frac{\partial \phi}{\partial t} + u \frac{\partial \phi}{\partial x} + v \frac{\partial \phi}{\partial y} = \frac{1}{R_{\phi}} \left( \frac{\partial^2 \phi}{\partial x^2} + \frac{\partial^2 \phi}{\partial y^2} \right) + s^{\phi}$$
 (II-29)

where  $S^{f \varphi}$  is source term for variable  $f \varphi$  and  $R_{f \varphi}$  is effective Reynolds number for variable  $f \varphi$  defined as

$$R_u = R_v = \frac{1}{(1/Re + v_+)}$$
 (II-30)

$$R_{k} = \frac{\sigma_{k}}{(\sigma_{k}/Re + v_{t})}$$
 (II-31)

$$R_{\varepsilon} = \frac{\sigma_{\varepsilon}}{(\sigma_{\varepsilon}/Re + v_{+})}$$
 (II-32)

If we locally linearize the convective velocity in the governing equation by the value at calculation point P as shown in Fig.II-6 and neglect the diffusion of transport quantities in the flow direction, the governing equation can be approximately written in a following simplified form:

$$\frac{\partial^2 \phi}{\partial y^2} = 2B \frac{\partial \phi}{\partial y} + F \tag{II-33}$$

where

$$2B = (R_{\phi}v)_{p} \qquad (II-34)$$

$$F = (D_{\phi})_{P} (\phi_{P} - \phi_{W}) + \frac{(E_{\phi})_{P}}{\Delta t} (\phi_{P} - \phi_{P}^{n-1}) - (S_{\phi})_{P}$$
(II-35)

and

$$D_{\phi} = \frac{(R_{\phi}^{u})_{p}}{\Delta x} \tag{II-36}$$

$$E_{\phi} = (R_{\phi})_{P} \tag{II-37}$$

$$S_{\dot{\phi}} = (S^{\dot{\phi}} R_{\dot{\phi}})_{P} \tag{II-38}$$

In these equations, the subscript P denotes the calculation point and the superscript n-1 denotes the previous time step value. The unsteady term and the x-derivative of  $\phi$  are approximated by backward and upwind finite difference respectively. Eq.(II-30) is solved analytically with boundary conditions specified by following equations.

$$\phi(h) = \phi_{N'} \qquad \phi(-k) = \phi_{S} \qquad (II-39)$$

Evaluation of  $\phi$  at calculation point P gives following algebraic equations.

$$\phi_{p} = A_{N} \phi_{N} + A_{S} \phi_{S} - C_{p} F \qquad (II-40)$$

where

$$A_S = \frac{\exp(2Bh) - 1}{\exp(2Bh) - \exp(-2Bk)}$$
 (II-41)

$$A_{N} = \frac{1 - \exp(-2Bk)}{\exp(2Bh) - \exp(-2Bk)}$$
 (II-42)

$$C_{p} = \frac{hk}{2} \left( \frac{A_{N}}{Bk} - \frac{A_{S}}{Bh} \right)$$
 (II-43)

If the node P is placed on the wake centerline where the normal convective velocity component v is equal to zero, then

$$A_{N} = \frac{k}{h + k} \tag{II-44}$$

$$A_{S} = \frac{h}{h+k} \tag{II-45}$$

$$C_{p} = \frac{hk}{2}$$
 (II-46)

With the source term linearized as

$$(S_{\mathbf{\phi}})_{P} = S_{\mathbf{\phi}}^{P} \phi_{P} + S_{\mathbf{\phi}}^{C}$$
 (II-47)

the following four point partially parabolic discretization formula can be obtained by manipulating Eq.(II-40), Eq.(II-35) and Eq.(II-47).

$$A_{p} \phi_{p} = A_{N} \phi_{N} + A_{S} \phi_{S} + A_{W} \phi_{W} + b_{\phi}$$
 (II-48)

where

$$A_{w} = C_{p} (D_{\phi})_{p}$$
 (II-49)

$$A_{p} = 1 + C_{p} ((D_{\phi})_{p} + \frac{(E_{\phi})_{p}}{\Delta t} - S_{\phi}^{p})$$
 (II-50)

$$b_{\phi} = C_{p} \left( \frac{(E_{\phi})_{p}}{\Delta t} \phi_{p}^{n-1} + S_{\phi}^{C} \right)$$
 (II-51)

and  $A_{N}$ ,  $A_{S}$  and  $C_{p}$  are given by Eq.(II-41) through Eq.(II-46).

This partially parabolic form of finite analytic formulation may be interpreted as a combination of the upwind scheme in the flow direction and the exponential scheme in the normal direction.

# 

The non-dimensionized governing equations based on the cylindrical coordinate system can be written in the transformed coordinate system as following using the partial transformation where the original orthogonal velocity components are left as dependent variables;

$$[r(b_1^1 u + b_2^1 v)]_{\xi} + [r(b_1^2 u + b_2^2 v)]_{\eta} = 0$$
 (II-52)

$$g^{11} \phi_{\xi\xi} + g^{22} \phi_{\eta\eta} = 2A_{\phi}\phi_{\xi} + 2B_{\phi}\phi_{\eta} + E_{\phi}\phi_{t} + S_{\phi}$$
 (II-53)

where

$$2A_{\phi} = \frac{R_{\phi}}{J} r (b_1^1 u + b_2^1 v) - f^1$$
 (II-54)

$$2B_{\phi} = \frac{R_{\phi}}{J} r (b_1^2 u + b_2^2 v) - f^2$$
 (II-55)

$$E_{\mathbf{0}} = R_{\mathbf{0}} \tag{II-56}$$

$$S_{\phi} = R_{\phi} S^{\phi} - 2g^{12} \phi_{\xi \eta} \qquad (II-57)$$

and

$$b_1^1 = y_{\eta}, b_2^1 = -x_{\eta}, b_1^2 = -y_{\xi}, b_2^2 = x_{\xi}$$
 (II-58)

$$J = r (x_{\xi} y_{\eta} - x_{\eta} y_{\xi})$$
 (II-59)

If we locally linearize Eq.(II-53) in each numerical element,  $\Delta \xi = \Delta \eta = 1$ , by the value at calculation point P as shown in Fig.II-7 and linearize the source term by Eq.(II-47), one obtains following equation.

$$g_{P}^{11} \phi_{\xi\xi} + g_{P}^{22} \phi_{\eta\eta} = 2(A_{\phi})_{P} \phi_{\xi} + 2(B_{\phi})_{P} \phi_{\eta} + G \quad (II-60)$$

where

$$G = \frac{(E_{\phi})_{P}}{\Lambda_{t}} (\phi_{P} - \phi_{P}^{n-1}) + S_{\phi}^{P} \phi_{P} + S_{\phi}^{C}$$
 (II-61)

If we introduce the grid stretching functions such that

$$\xi^* = \frac{\xi}{\sqrt{g_p^{11}}}, \qquad \eta^* = \frac{\eta}{\sqrt{g_p^{22}}}$$
 (II-62)

then Eq.(II-60) can be written in a standard finite analytic form.

$$\phi_{\xi * \xi *} + \phi_{\eta * \eta *} = 2A \phi_{\xi *} + 2B \phi_{\eta *} + G$$
 (II-63)

where

$$A = \frac{(A_{\phi})_{P}}{\sqrt{g_{P}^{11}}}, \qquad B = \frac{(B_{\phi})_{P}}{\sqrt{g_{P}^{22}}}$$
 (II-64)

and the grid size is stretched to

$$\Delta \xi^* = h = \frac{1}{\sqrt{g_p^{11}}}, \quad \Delta \eta^* = k = \frac{1}{\sqrt{g_p^{22}}}$$
 (II-65)

Equation (II-63) is solved analytically using the method of separation of variable with boundary condition expressed as the combinations of constant, linear and exponential functions involving the nodal values.

Evaluation of the analytic solution at the center node then provides a nine point algebraic discretization formula [3].

$$A_{p} \phi_{p} = \sum_{n=1}^{8} A_{nb} \phi_{nb} + b_{\phi}$$
 (II-66)

where

$$A_{E} = \frac{\exp(-Ah)}{2\cosh(Ah)} * P_{B}$$
 (II-67)

$$A_{W} = \frac{\exp(Ah)}{2\cosh(Ah)} * P_{B}$$
 (II-68)

$$A_{N} = \frac{\exp(-Bk)}{2\cosh(Bk)} * P_{A}$$
 (II-69)

$$A_{S} = \frac{\exp(Bk)}{2\cosh(Bk)} * P_{A}$$
 (II-70)

$$A_{SW} = \frac{\exp(Ah+Bk)}{4\cosh(Ah)\cosh(Bk)} * (1-P_A-P_B)$$
 (II-71)

$$A_{SE} = \frac{\exp(-Ah + Bk)}{4\cosh(Ah)\cosh(Bk)} * (1-P_A - P_B)$$
 (II-72)

$$A_{NW} = \frac{\exp(Ah - Bk)}{4\cosh(Ah)\cosh(Bk)} * (1-P_A - P_B)$$
 (II-73)

$$A_{NE} = \frac{\exp(-Ah - Bk)}{4\cosh(Ah)\cosh(Bk)} * (1-P_A - P_B)$$
 (II-74)

$$A_{p} = 1 + C_{p} \left( \frac{(E_{\phi})_{p}}{\Delta t} - S_{\phi}^{p} \right)$$
 (II-75)

$$b_{\phi} = C_{P} \left( \frac{(E_{\phi})_{P}}{\Delta t} \phi_{P}^{n-1} + S_{\phi}^{C} \right)$$
 (II-76)

$$C_{P} = \frac{h \tanh(Ah)}{2A} * (1-P_{A}) = \frac{k \tanh(Bk)}{2B} * (1-P_{B}) (II-77)$$

and

$$P_A = 4Ah \cosh(Ah) \cosh(Bk) \coth(Ah) E_2$$
 (II-78)

$$P_{B} = 1 + \frac{Bh \cdot coth(Bk)}{Ak \cdot coth(Ah)} * (P_{A}-1)$$
 (II-79)

with

$$E_{2} = \sum_{m=1}^{\infty} \frac{-(-1)^{m} \lambda_{m} h}{[(Ah)^{2} + (\lambda_{m}h)^{2}]^{2} \cosh \sqrt{(A^{2} + B^{2} + \lambda_{m}^{2}) k^{2}}}$$
(II-80)

$$\lambda_{\rm m} h = (m - \frac{1}{2}) \pi \tag{II-81}$$

For large cell Reynolds numbers, the series summation in  $\rm E_2$  can be avoided by the following asymptotic expressions of  $\rm P_A$  and  $\rm P_B$  based on the theory of characteristics.[4]

Ak coth Ah > Bh coth Bk;

$$P_A = 0$$
,  $P_B = 1 - (Bh coth Bk)/(Ak coth Ah).$ 

Ak coth Ah < Bh coth Bk;

$$P_B = 0$$
,  $P_A = 1 - (Ak coth Ah)/(Bh coth Bk)(II-82)$ 

# II.5.3 Partially Parabolic Form of Finite Analytic Method in the Boundary-Fitted Coordinate System

The problems considered in the present study are mostly free from separation and have a predominant flow direction. In these problems, diffusion in the flow direction is much smaller than diffusion in the normal direction. Thus the diffusion term in the flow direction can be neglected without loss of accuracy. This partially parabolic form has advantages over the fully elliptic form in the fact that the computing time for the calculation of finite analytic coefficients can be reduced. situations when the grid ratio and cell peclet number become too large, the nine point finite analytic coefficients requires more computational efforts to be evaluated accurately. The partially parabolic form of finite analytic method can be used without any difficulties. The partially parabolic formulation can also be used for the simulation of small separated flow with FLARE approximation [61].

Eq.(II-60) can be approximated using the partially parabolic assumption (  $\phi_{\xi\xi}$  = 0 ) and the upwind difference for the convection term in the  $\xi$ -direction as the following form;

$$g_{P}^{22} \phi_{\eta \eta} = 2(B_{\phi})_{P} \phi_{\eta} + (D_{\phi})_{P} (\phi_{P} - \phi_{W}) + G$$
 (II-83)

where

$$(D_{\dot{\Phi}})_{P} = 2(A_{\dot{\Phi}})_{P} \tag{II-84}$$

Introduction of the grid stretching functions  $\eta^*$  =  $\sqrt{g_{\rm p}^{22}}$  leads Eq.(II-83) to the standard finite analytic form.

$$\phi_{\eta * \eta *} = 2B \phi_{\eta *} + F \qquad (II-85)$$

where

$$B = \frac{(B_{\phi})_{P}}{\sqrt{g_{P}^{22}}}$$

$$F = (D_{\phi})_{P} (\phi_{P} - \phi_{W}) + G \qquad (II-87)$$

$$F = (D_{\phi})_{p} (\phi_{p} - \phi_{W}) + G$$
 (II-87)

and the grid size is stretched to

$$\Delta \eta * = k = \frac{1}{\sqrt{g_p^{22}}}$$
 (II-88)

Equation (II-85) can be solved analytically using the north and south nodal values as boundary conditions. Evaluation of the analytic solution at the center node then provides a four point algebraic discretization formula.

$$A_{p} \phi_{p} = A_{N} \phi_{N} + A_{S} \phi_{S} + A_{W} \phi_{W} + b_{\phi}$$
 (II-89)

$$A_{N} = \frac{\exp(-Bk)}{2\cosh(Bk)}$$
 (II-90)

$$A_{S} = \frac{\exp(Bk)}{2\cosh(Bk)}$$
 (II-91)

$$A_{w} = C_{p} (D_{\phi})_{p} \qquad (II-92)$$

$$A_{p} = 1 + C_{p} ((D_{\phi})_{p} + \frac{(E_{\phi})_{p}}{\Lambda t} - S_{\phi}^{p})$$
 (II-93)

$$b_{\phi} = C_{P} \left( \frac{(E_{\phi})_{P}}{\Delta t} \phi_{P}^{n-1} + S_{\phi}^{C} \right)$$
 (II-94)

$$C_{p} = \frac{k \tanh(Bk)}{2B}$$
 (II-95)

#### II.6 Finite Volume Method

The strong conservative form of governing equations in the transformed domain can be written as follows;

$$(\rho r U)_{\xi} + (\rho r V)_{\eta} = 0$$
 (II-96)

$$(\rho r U \phi)_{\xi} + (\rho r V \phi)_{\eta} = [\frac{\Gamma_{\phi}}{J} (D_{1}^{1} \phi_{\xi} + D_{2}^{1} \phi_{\eta})]_{\xi}$$

$$+ [\frac{\Gamma_{\phi}}{J} (D_{1}^{2} \phi_{\xi} + D_{2}^{2} \phi_{\eta})]_{\eta} + J S_{\phi}$$
(II-97)

$$U = (b_1^1 u + b_2^1 v) (II-98)$$

$$V = (b_1^2 u + b_2^2 v)$$
 (II-99)

and

$$D_1^1 = r^2 \left( x_n^2 + y_n^2 \right) \tag{II-100}$$

$$D_2^2 = r^2 \left( x_{\xi}^2 + y_{\xi}^2 \right) \tag{II-101}$$

$$D_2^1 = D_1^2 = -r^2 (x_{\xi} x_{\eta} + y_{\xi} y_{\eta})$$
 (II-102)

In the finite volume method [2], the governing differential equations are integrated over a finite number of control volumes with size,  $\Delta \xi = \Delta \eta = 1$ , as shown in Fig.II-8. Using the Gauss theorem, the volume integral of terms under differential operator can be converted into surface integrals over the four faces of a two dimensional control volume. The resulting balance equations for each control volume and variable  $\varphi$  can be expressed as follows.

$$I_e - I_w + I_n - I_s = \int_{AV} J S_{\phi} d\xi d\eta$$
 (II-103)

where

$$I_e = (\rho r U \phi)_e - [\frac{\Gamma_\phi}{J} (D_1^1 \phi_\xi + D_2^1 \phi_\eta)]_e (II-104)$$

$$I_n = (\rho r V \phi)_n - [\frac{I_{\phi}}{J} (D_1^2 \phi_{\xi} + D_2^2 \phi_{\eta})]_n (II-105)$$

The volume integral of the source term may be evaluated as follows;

$$\int_{\Delta V} J S_{\phi} d\xi d\eta = (S_{\phi}^{P} \phi_{P} + S_{\phi}^{C}) \Delta V \qquad (II-106)$$

By putting the non-orthogonal terms into source term, the Eq.(II-103) can be written as as follows.

$$[\rho r U \phi - \frac{\Gamma_{\phi}}{J} D_{1}^{1} \phi_{\xi}]_{e} - [\rho r U \phi - \frac{\Gamma_{\phi}}{J} D_{1}^{1} \phi_{\xi}]_{w}$$

$$+ [\rho r V \phi - \frac{\Gamma_{\phi}}{J} D_{2}^{2} \phi_{\eta}]_{n} - [\rho r V \phi - \frac{\Gamma_{\phi}}{J} D_{2}^{2} \phi_{\eta}]_{s}$$

$$= (s_{\phi}^{P} \phi_{P} + s_{\phi}^{C}) \Delta V + s_{\phi}^{b} \qquad (II-107)$$

where  $S_{\varphi}^{b}$  is the source term arised from the non-orthogonality of numerical grid and defined as;

$$S_{\phi}^{b} = \left(\frac{\Gamma_{\phi}}{J} D_{2}^{1} \phi_{\eta}\right)_{e} - \left(\frac{\Gamma_{\phi}}{J} D_{2}^{1} \phi_{\eta}\right)_{w} + \left(\frac{\Gamma_{\phi}}{J} D_{1}^{2} \phi_{\xi}\right)_{n} - \left(\frac{\Gamma_{\phi}}{J} D_{1}^{2} \phi_{\xi}\right)_{s}$$
(II-108)

The Eq.(II-107) is the standard finite volume formulation and discretization of this equation is well explained in Patankar [2]. Using the hybrid numerical scheme, the discretization equation can be obtained as follows.

$$A_p \phi_P = A_E \phi_E + A_W \phi_W + A_N \phi_N + A_S \phi_S + b_{\phi}$$
 (II-109)

$$A_{E} = MAX [ 0.5*| F_{e} | , D_{e} ] - 0.5*F_{e}$$
 (II-110)

$$A_{W} = MAX [ 0.5* | F_{W} | , D_{W} ] + 0.5*F_{W}$$
 (II-111)

$$A_N = MAX [ 0.5* | F_n | , D_n ] - 0.5*F_n$$
 (II-112)

$$A_S = MAX [ 0.5*| F_S | , D_S ] + 0.5*F_S$$
 (II-113)

$$A_{p} = A_{E} + A_{W} + A_{N} + A_{S} - S_{\phi}^{P} \Delta V$$
 (II-114)

$$b_{\phi} = S_{\phi}^{C} \Delta V + S_{\phi}^{b} \tag{II-115}$$

and

$$F_{e} = (\rho r U)_{e}$$
 (II-116)

$$F_{w} = (\rho r U)_{w}$$
 (II-117)

$$F_{n} = (\rho r V)_{n}$$
 (II-118)

$$F_{s} = (\rho r V)_{s}$$
 (II-119)

with

$$D_{e} = \left(\frac{\Gamma_{\phi}}{J} D_{1}^{1}\right)_{e} \tag{II-120}$$

$$D_{\mathbf{w}} = \left(\begin{array}{c} \frac{\Gamma_{\mathbf{\phi}}}{J} D_{\mathbf{1}}^{1} \right)_{\mathbf{w}} \tag{II-121}$$

$$D_{n} = \left(\frac{\Gamma_{\phi}}{J} D_{2}^{2}\right)_{n} \tag{II-122}$$

$$D_{S} = \left(\frac{\Gamma_{\phi}}{J} D_{2}^{2}\right)_{S} \tag{II-123}$$

In these equations, the notation MAX [ A , B ] means the greater of A and B and  $\mid$  A  $\mid$  means the absolute value of A.

The problems considered in the present study are mostly free of separation. Thus the numerical false

diffusion problem has a negligible effect on the accuracy of solution. In these situations, the choice of numerical scheme is not important. However, the use of different numerical method requires different usage of wall function method in the turbulent flow calculation. The finite analytic method usually uses the two-point wall function method while the wall function method of Launder and Spalding [43] is employed for most of finite volume calculations. The primary numerical scheme for the present study is the finite analytic method. However, the finite volume method is employed when the use of the twopoint wall function method is restricted by a certain problem or when the comparisions of predictions by two different methods are thought to be important. It is noted that the finite analytic method usually employs nondimensionized form of governing equations while finite volume method employes dimensional form. All the derivations follow this common practice. The use of each numerical scheme for a certain problem is explained when a specific problem is mentioned.

# CHAPTER III SOLUTION PROCEDURE

### III.1 Introduction

A difficulty encountered in solving the Navier-Stokes equations for incompressible flow concern the handling of pressure terms. The difficulty arises from the fact that pressure does not have its own equation in the sets of Navier-Stokes equations. The pressure term only appears in the momentum equations which must be considered as the governing equations for velocity components. Thus the continuity equation should be used to solve the pressure variable. However, there is no pressure term in the continuity equation. This difficulty is usually circumvented by deriving the pressure equation by manipulating the continuity equation and momentum equations. It is noted that the algebraic relations obtained in the previous chapter can be used only for the velocity components and turbulent quantities. The way of resolving pressure varible and satisfying mass conservation should be sought. In the present study, the SIMPLER ( Semi-Implicit Method for Pressure Linked Equation - Revised ) numerical algorithm of Patankar [2]

is imployed for this purpose. In this algorithm, a

Poisson like equation which is derived from the

manipulation of continuity equation and momentum equations
is solved to obtain the pressure field and in addition,
the pressure correction equation is again solved to

correct velocity components to satisfy continuity
equation. Following sections are devoted to the
derivation of pressure and pressure correction equation in
the Cartesian coordinate system and in the body-fitted

coordinate system.

## III.2. Pressure and Pressure Correction Equation in Cartesian Coordinate System

From the discretization equations for momentum equations such as Eq.(II-40) or Eq.(II-66), the velocity field ( u , v ) can be decomposed into pseudovelocity components (  $\hat{u}$  ,  $\hat{v}$  ) and the pressure gradient terms contained in the source term as;

$$u_e = \hat{u}_e - d_e (p_E - p_p)$$
 (III-1)

$$v_n = \hat{v}_n - d_n (p_N - p_p)$$
 (III-2)

$$\hat{u}_e = \frac{1}{A_e} \left( \sum_{nb} A_{nb} u_{nb} + b_u \right)_e$$
 (III-3)

$$\hat{v}_n = \frac{1}{A_n} \left( \sum_{nb} A_{nb} v_{nb} + b_v \right)_n$$
 (III-4)

and

$$d_e = [C_e(R_u)_e] / [A_e(\delta x)_e]$$
 (III-5)

$$d_{n} = [C_{n}(R_{y})_{n}] / [A_{n}(\delta y)_{n}]$$
 (III-6)

In these equations, subscripts e and n denote the value evaluated at staggered velocity nodes e and n as shown in Fig.III-1. For example  $A_e$ ,  $C_e$  are algebraic coefficients  $A_p$ ,  $C_p$  evaluated at node e and  $(\delta x)_e$ ,  $(\delta y)_n$  are the distances between pressure calculation points. The variables  $R_u$ ,  $R_v$  are the effective Reynolds number for variable u and v. All the coefficients are based on the finite analytic method in non-dimensional form given in Eq.(II-41) through Eq.(II-43).

The continuity equation within the control volume cell can be written as following;

$$(\Delta y)_e u_e - (\Delta y)_w u_w + (\Delta x)_n v_n - (\Delta x)_s v_s = 0$$
 (III-7)

where  $\Delta x$ ,  $\Delta y$  are the sizes of control volume cell as shown in Fig.III-1.

The pressure equation can be derived by substituting momentum equation, Eq.(III-1) and Eq.(III-2) into continuity equation, Eq.(III-7).

$$A_{p} p_{p} = A_{E} p_{E} + A_{W} p_{W} + A_{N} p_{N} + A_{S} p_{S} - \hat{D}$$
 (III-8)

where

$$A_{E} = (\Delta y)_{e} d_{e}$$
 (III-9)

$$A_{W} = (\Delta y)_{W} d_{W}$$
 (III-10)

$$A_{N} = (\Delta x)_{n} d_{n}$$
 (III-11)

$$A_{S} = (\Delta x)_{S} d_{S}$$
 (III-12)

$$A_{p} = A_{E} + A_{W} + A_{N} + A_{S}$$
 (III-13)

and

$$\hat{D} = (\Delta y)_{e} \hat{u}_{e} - (\Delta y)_{w} \hat{u}_{w} + (\Delta x)_{n} \hat{v}_{n} - (\Delta x)_{s} \hat{v}_{s} \qquad (III-14)$$

The velocity components ( u , v ) obtained from the solution of the momentum equations will generally not satisfy the continuity equation unless the pressure field is correct. We denote these imperfect velocity components as starred velocity components (  $u^*$  ,  $v^*$  ). These starred velocity components must be corrected to satisfy continuity equation.

$$u_e = u_e^* - d_e (P_E' - P_P')$$
 (III-15)

$$v_n = v_n^* - d_n (P_N' - P_P')$$
 (III-16)

where P is the pressure correction.

The pressure correction equation is obtained by substituting these velocity correction equations into continuity equation, Eq.(III-7).

$$A_{p} P_{p} = A_{E} P_{E} + A_{W} P_{W} + A_{N} P_{N} + A_{S} P_{N} - D^{*}$$
 (III-17)

where

$$D^* = (\Delta y)_e u_e^* - (\Delta y)_w u_w^* + (\Delta x)_n v_n^* - (\Delta x)_s v_s^* \quad (III-18)$$

and the coefficients  $A_E$ ,  $A_W$ ,  $A_N$ ,  $A_S$  and  $A_P$  are same as those given in pressure equation and the mass source  $D^*$  is based on starred velocity components which are obtained from the solution of momentum equations.

After the pressure correction equation is solved, the velocity components are corrected through velocity correction equations to satisfy continuity equation.

# III.3 Pressure and Pressure Correction Equation in Boundary-Fitted Coordinate System

# III.3.1 One Velocity Staggered Grid Method

In one velocity staggered grid method, only one velocity component is stored in each staggered node e and n as shown in Fig.III-2. Thus derivation of pressure and pressure correction equation in this grid arrangement is not much depart from those in Cartesian coordinate system.

The discretized momentum equations for  $\mathbf{u}_{\mathbf{e}}$  and  $\mathbf{v}_{\mathbf{n}}$  can be written as follows;

$$u_e = (H_u)_e - (D_1^u)_e (p_E - p_p) - (D_2^u)_e (p_{en} - p_{es})$$
 (III-19)

$$v_n = (H_v)_n - (D_1^v)_n (p_{en} - p_{wn}) - (D_2^v)_n (p_N - p_p)$$
 (III-20)

where

$$(H_u)_e = \frac{1}{A_e} \left( \sum_{nb} A_{nb} u_{nb} + b_u \right)_e$$
 (III-21)

$$(H_v)_n = \frac{1}{A_n} \left( \sum_{nb} A_{nb} v_{nb} + b_v \right)_n$$
 (III-22)

and

$$(D_1^u)_e = [C_e (R_u r b_1^1)_e] / [A_e J_e]$$
 (III-23)

$$(D_2^u)_e = [C_e (R_u r b_1^2)_e] / [A_e J_e]$$
 (III-24)

$$(D_1^{\mathbf{v}})_{\mathbf{n}} = [C_{\mathbf{n}} (R_{\mathbf{v}} r b_2^1)_{\mathbf{n}}] / [A_{\mathbf{n}} J_{\mathbf{n}}]$$
 (III-25)

$$(D_2^{v})_n = [C_n (R_v r b_2^2)_n] / [A_n J_n]$$
 (III-26)

In these equations, the algebraic coefficients are based on the finite analytic method with non-dimensional form given in chapter II-4.

The velocity components ( u , v ) are then decomposed into pseudovelocity components (  $\hat{u}$  ,  $\hat{v}$  ) and the pressure gradient terms.

$$u_e = \hat{u}_e - (D_1^u)_e (P_E - P_P)$$
 (III-27)

$$v_n = \hat{v}_n - (D_2^v)_n (P_N - P_P)$$
 (III-28)

where

$$\hat{u}_e = (H_u)_e - (D_2^u)_e (p_{en} - p_{es})$$
 (III-29)

$$\hat{v}_n = (H_v)_n - (D_1^v)_n (p_{en} - p_{wn})$$
 (III-30)

The cross derivative terms of pressure are contained in the pseudovelocity components to avoid a complicate nine point pressure equation and are explicitly evaluated using the pressure obtained from the previous iteration.

The continuity equation within the control volume cell in non-orthogonal coordinate system can be written as follows.

$$[r(b_1^1 u + b_2^1 v)]_e - [r(b_1^1 u + b_2^1 v)]_w$$

$$+ [r(b_1^2 u + b_2^2 v)]_n - [r(b_1^2 u + b_2^2 v)]_s = 0$$
 (III-31)

The Eq. (III-31) can be rearranged as following form.

$$(rb_1^1u)_e - (rb_1^1u)_w + (rb_2^2v)_n - (rb_2^2v)_s = -D_N (III-32)$$

$$D_{N} = (rb_{2}^{1}v)_{e} - (rb_{2}^{1}v)_{w} + (rb_{1}^{2}u)_{n} - (rb_{1}^{2}u)_{s}$$
 (III-33)

The pressure equation can be derived by substituting Eq.(III-27) and Eq.(III-28) to continuity equation, Eq.(III-32).

$$A_{p} p_{p} = A_{E} p_{E} + A_{W} p_{W} + A_{N} p_{N} + A_{S} p_{S} - \hat{D}$$
 (III-34)

$$A_{E} = (r b_{1}^{1})_{e} (D_{1}^{u})_{e}$$
 (III-35)

$$A_{W} = (r b_{1}^{1})_{w} (D_{1}^{u})_{w}$$
 (III-36)

$$A_N = (r b_2^2)_n (D_2^v)_n$$
 (III-37)

$$A_S = (r b_2^2)_S (D_2^V)_S$$
 (III-38)

$$A_p = A_E + A_W + A_N + A_S$$
 (III-39)

where

$$\hat{D} = (rb_1^1 \hat{u})_e - (rb_1^1 \hat{u})_w + (rb_2^2 \hat{v})_n - (rb_2^2 \hat{v})_s + D_N$$
(III-40)

and the mass source  $\hat{D}$  is based on the pseudovelocity components. The mass source term  $D_N$  expressed in Eq.(III-33) should be evaluated from the continuity-satisfying velocity components from the previous iteration level. It is noted that the velocity components that are needed for evaluation of  $D_N$  are not stored at the staggered nodes and are obtained by averaging neighbouring nodal values.

The imperfect velocity components (  $u^*$ ,  $v^*$ ) which are obtained from the solution of momentum equations are corrected by the pressure correction in order to satisfy the continuity equation.

$$u_e = u_e^* - (D_1^u)_e (P_E^* - P_P^*)$$
 (III-41)

$$v_n = v_n^* - (D_2^v)_n (P_N^' - P_P^')$$
 (III-42)

where P is the pressure correction. The pressure correction terms arised from the cross derivatives are neglected to ensure the diagonal dominant pressure correction equation which is an important parameter to achieve the stability of solution procedure. The neglection of these terms do not effect the accuracy of final converged solution since the pressure correction should be zero at the final converged stage. However, this practice may slow down the convergence when the numerical grid is strongly non-orthogonal.

The pressure correction equation is obtained by substituting velocity correction equations into continuity equation, Eq.(III-32).

$$A_{p} P_{p}' = A_{E} P_{E}' + A_{W} P_{W}' + A_{N} P_{N}' + A_{S} P_{N}' - D^{*}$$
 (III-43)

$$D^* = (rb_1^1 u^*)_e - (rb_1^1 u^*)_w + (rb_2^2 v^*)_n - (rb_2^2 v^*)_s + D_N$$
(III-44)

where the coefficients  $A_E$ ,  $A_W$ ,  $A_N$ ,  $A_S$  and  $A_P$  are the same as those given in pressure equation and  $D^*$  is based on the starred velocities (  $u^*$ ,  $v^*$ ) which only satisfy the momentum equation.

With the updated pressure correction, the velocities are improved through the velocity correction equations to satisfy continuity equation.

It is noted that pressure and velocity coupling technique used in the present study is slightly different from that used by Shyy et al. [24] although same one velocity staggered grid method is employed.

#### III.3.2 Two Velocities Staggered Grid Method

In two velocities staggered method, both velocity components are stored at each staggered node e and n as shown in Fig.III-3. The discretized form of momentum equations for these velocity components can be written as follows with the pressure gradient term expressed explicitly.

$$u_e = (H_u)_e - (D_1^u)_e (p_E - p_p) - (D_2^u)_e (p_{en} - p_{es}) (III - 45)$$

$$v_e = (H_v)_e - (D_1^v)_e (p_E - p_p) - (D_2^v)_e (p_{en} - p_{es}) (III - 46)$$

and

$$u_n = (H_u)_n - (D_1^u)_n (p_{en} - p_{wn}) - (D_2^u)_n (p_N - p_p) (III - 47)$$

$$v_n = (H_v)_n - (D_1^v)_n (p_{en} - p_{wn}) - (D_2^v)_n (p_N - p_p) (III - 48)$$

where

$$H_{u} = \frac{1}{A_{p}} \left( \sum_{nb} A_{nb} u_{nb} + b_{u} \right)$$
 (III-49)

$$H_{v} = \frac{1}{A_{p}} \left( \sum_{nb} A_{nb} v_{nb} + b_{v} \right)$$
 (III-50)

and

$$D_1^u = (r b_1^1) / A_D$$
 (III-51)

$$D_2^u = (r b_1^2) / A_p$$
 (III-52)

$$D_1^V = (r b_2^1) / A_p$$
 (III-53)

$$D_2^V = (r b_2^2) / A_p$$
 (III-54)

In these equations, the algebraic coefficients are based on finite volume method.

The velocity field ( u , v ) can be decomposed into pseudovelocity components (  $\hat{u}$  ,  $\hat{v}$  ) and the pressure gradient terms as follows.

$$u_{p} = \hat{u}_{p} - (D_{1}^{u})_{p} (P_{E} - P_{p})$$
 (III-55)

$$v_e = \hat{v}_e - (D_1^v)_e (P_E - P_P)$$
 (III-56)

and

$$u_n = \hat{u}_n - (D_2^u)_n (P_N - P_P)$$
 (III-57)

$$v_n = \hat{v}_n - (D_2^v)_n (P_N - P_P)$$
 (III-58)

where

$$\hat{u}_{e} = (H_{u})_{e} - (D_{2}^{u})_{e} (p_{en} - p_{es})$$
 (III-59)

$$\hat{v}_{e} = (H_{v})_{e} - (D_{2}^{v})_{e} (p_{en} - p_{wn})$$
 (III-60)

and

$$\hat{u}_n = (H_u)_n - (D_1^u)_n (p_{en} - p_{wn})$$
 (III-61)

$$\hat{v}_n = (H_v)_n - (D_1^v)_n (p_{en} - p_{wn})$$
 (III-62)

The cross derivative terms of pressure are again contained in pseudovelocity components to obtain diagonal dominant five point pressure equations.

The continuity equation for the control volume cell shown in Fig.III-3 can be written as follows;

$$U_{p} - U_{w} + V_{p} - V_{q} = 0 (III-63)$$

where U and V are the contravariant velocity components defined as;

$$U = r (b_1^1 u + b_2^1 v)$$
 (III-64)

$$V = r (b_1^2 u + b_2^2 v)$$
 (III-65)

The pressure equation is then obtained by sustituting Eq.(III-55) through Eq.(III-58) into continuity equation, Eq.(III-63).

$$A_{p} p_{p} = A_{E} p_{E} + A_{W} p_{W} + A_{N} p_{N} + A_{S} p_{S} - \hat{D}$$
 (III-66)

where

$$A_{E} = r_{e} \left( b_{1}^{1} D_{1}^{u} + b_{2}^{1} D_{1}^{v} \right)_{e}$$
 (III-67)

$$A_{W} = r_{W} \left( b_{1}^{1} D_{1}^{u} + b_{2}^{1} D_{1}^{v} \right)_{W}$$
 (III-68)

$$A_N = r_n (b_1^2 D_2^u + b_2^2 D_2^v)_n$$
 (III-69)

$$A_S = r_s (b_1^2 D_2^u + b_2^2 D_2^v)_s$$
 (III-70)

$$A_{p} = A_{E} + A_{W} + A_{N} + A_{S}$$
 (III-71)

$$\hat{D} = \hat{U}_e - \hat{U}_w + \hat{V}_n - \hat{V}_s$$
 (III-72)

and  $\hat{\mathbb{U}}$  and  $\hat{\mathbb{V}}$  are based on the pseudovelocity components and defined as;

$$\hat{U} = r \left( b_1^1 \hat{u} + b_2^1 \hat{v} \right)$$
 (III-73)

$$\hat{V} = r \left( b_1^2 \hat{u} + b_2^2 \hat{v} \right)$$
 (III-74)

Since the velocity components obtained from the solution of momentum equations with imperfect pressure field generally do not satisfy continuity equation. These starred velocity components ( $u^*$ ,  $v^*$ ) are corrected through the pressure correction in order to satisfy mass conservation during the iteration process.

$$u_e = u_e^* - (D_1^u)_e (P_E^! - P_P^!) - (D_2^u)_e (P_e^! - P_e^!)$$
 (III-75)

$$v_e = v_e^* - (D_1^v)_e (P_E^{-P_P}) - (D_2^v)_e (P_{en}^{-P_{es}})$$
 (III-76)

and

$$u_n = u_n^* - (D_1^u)_n (P_{en}^{'} - P_{wn}^{'}) - (D_2^u)_n (P_N^{'} - P_P^{'})$$
 (III-77)

$$v_n = v_n^* - (D_1^v)_n (P_{en}^* - P_{wn}^*) - (D_2^v)_n (P_N^* - P_P^*)$$
 (III-78)

where P is the pressure correction

In order to facilitate the velocity correction procedure, following contravariant velocity correction equations are derived using Eq.(III-75)-Eq.(III-78) and Eq.(III-64)-Eq.(III-65).

$$U_e = U_e^* - (D_U)_e (P_E^* - P_P^*)$$
 (III-79)

$$v_n = v_n^* - (D_V)_n (P_N^{'} - P_P^{'})$$
 (III-80)

$$U_{e}^{*} = r_{e} (b_{1}^{1} u^{*} + b_{2}^{1} v^{*})_{e}$$
 (III-81)

$$v_n^* = r_n (b_1^2 u^* + b_2^2 v^*)_n$$
 (III-82)

and

$$(D_U)_e = r_e (b_1^1 D_1^u + b_2^1 D_1^v)_e$$
 (III-83)

$$(D_{V})_{n} = r_{n} (b_{1}^{2} D_{2}^{u} + b_{2}^{2} D_{2}^{v})_{n}$$
 (III-84)

The pressure correction terms arised from the nonorthogonality of numerical grids are neglected to avoid the complicated nine point pressure correction equation and to ensure diagonal dominant pressure correction equation.

The pressure correction equation is obtained by substituting these contravariant velocity correction equations into continuity equation, Eq.(III-63).

$$A_{p} P_{p}' = A_{E} P_{E}' + A_{W} P_{W}' + A_{N} P_{N}' + A_{S} P_{N}' - D^{*}$$
 (III-85)

where

$$D^* = U_p^* - U_w^* + V_n^* - V_s^*$$
 (III-86)

where the coefficients  $A_E$ ,  $A_W$ ,  $A_N$ ,  $A_S$  and  $A_P$  are the same as those in pressure equation and  $D^*$  is based on the starred velocities which are obtained from the solutions of the momentum equations.

From the updated pressure correction, the contravariant velocity components are corrected to satisfy mass conservation. The other contravariant velocity components,  $\mathbf{U}_{n}$  and  $\mathbf{V}_{e}$  which lie parallel to the control volume surfaces are obtained from linear interpolation of newly computed neighbouring nodal values.

Then the corrected velocities are obtained from these continuity-satisfying, corrected contravariant velocity components.

$$u = (b_2^2 U - b_2^1 V) / J$$
 (III-87)

$$v = - (b_1^2 U - b_1^1 V) / J$$
 (III-88)

where

$$J = r \left( b_1^1 b_2^2 - b_2^1 b_1^2 \right) \tag{III-89}$$

It is noted that the conitinuity-satisfying, corrected contravariant velocity components are stored and used for the evaluation of algebraic coefficients  $A_E$ ,  $A_W$ ,  $A_N$ ,  $A_S$  and  $A_P$  for transport quantities.

Maliska and Raithby [30] used the same procedure as outlined above in the calculation of three dimensional parabolic flow of arbitrary cross sectioned ducts.

However, they used exact nine-point pressure and pressure

correction equations which may deteriorate the stabillity of solution process when the numerical grids are strongly non-orthogonal.

#### III.4 Overall Solution Procedure

The solution procedure of SIMPLER algorithm is adopted for all the calculations in the present study. The momentum equations and turbulent transport equations are first solved by parabolic marching technique in the flow direction using the pressure obtained from the previous iteration. After the marching of calculations for turbulent quantities is completed, the pressure field is solved elliptically with several global iterations. The advantage of this global, elliptic pressure calculation technique is a monotonic and rapid convergence of pressure due to a proper consideration of the elliptic nature of the pressure field, especially near the leading and trailing edges.

The detailed overall solution procedure can be outlined as following.

1) Generate the numerical grids using the methods outlined in chapter II-3 and save the geometric data, such as  $b_1^j$ , J,  $f^i$ ,  $g^{ij}$  etc.

- 2) Specify the inlet boundary conditions for transport quantities, the velocity components and turbulent quantities.
- 3) Set pressure and pressure correction equal to zero everywhere in the solution domain.
- 4) Calculate the algebraic coefficients and source terms for momentum equations, such as those given in Eq.(II-67) through Eq.(II-81), at downstream station using the transport quantities obtained from the previous iteration level. This step includes the calculation of coefficients of pressure and pressure correction equation such as those given in Eq.(III-35) through Eq.(III-39).
- 5) Solve the momentum equations, such as Eq.(III-19) and Eq.(III-20), using the pressure from the previous iteration level to obtain starred velocity field, ( $u^*$ ,  $v^*$ ).
- 6) Using this starred velocity components, calculate the mass source for the pressure correction equation,  $^{\star}$ .
- 7) Solve the pressure correction equation, such as Eq.(III-43) and update the velocity field using Eq.(III-41) and Eq.(III-42) to satisfy continuity equation.

- 8) Calculate the pseudovelocity field, ( $\hat{u}$ ,  $\hat{v}$ ) from Eq.(III-29) and Eq.(III-30) using the corrected velocity components.
- 9) Calculate the mass source for pressure equation,  $\hat{D}$ , and store for later use.
- 10) Calculate the algebraic coefficients and source terms for the turbulent transport equations using the updated velocity field and turbulent quantities from the previous iteration level.
  - 11) Solve the turbulent transport equations.
- 12) March to the next downstream station and repeat the procedure 4) to 11).
- 13) After the marching is completed at the last downstream station, the pressure equation such as Eq.(III-34) is solved elliptically with several global iterations (typically 20 sweeps) from downstream to upstream to update new pressure field.
  - 14) Return to step 4) for the next iteration level.
- 15) Steps 4) through 14) are repeated until convergence or steady state solution is reached.

All the algebraic equations are solved by line by line technique using tridiagonal matrix algorithm. It is noted that although parabolic marching technique is employed for the calculation of transport quantities, all the transport quantities are stored in two dimensional array. Thus the present solution procedure has potential for the calculation of separated flow.

#### CHAPTER IV

# CALCULATION OF TURBULENT WAKE PAST A FLAT PLATE BY WAKE FUNCTION METHOD

#### IV.1 Introduction

The turbulent flow past a finite flat plate has been studied by many researchers because it provides a fundamental understanding of wake development and the basic feature of viscous-inviscid interaction at the trailing edge of the body. According to Alber [62], the wake region can be divided into three fundamental regions; laminar wake region where the laminar sublayer on the plate is destroyed, turbulent inner near wake region where the logarithmic remnant of the trailing edge boundary layer is destroyed, the far wake region where the flow field loses the memory of the turbulent boundary layer on the flat plate and attains the self preserving form. experimental data of Chevray and Kovasznay [63], Ramaprian et al. [64], Pot [65], Andreopoulous and Bradshaw [66] confirm such a wake behaviour behind a flat plate. Some comparisions and reviews of these data can be seen in Ramaprian et al. [64].

The earlier calculations by Rodi [67], Launder et al.[68] had placed more emphasis on the test of turbulence model. More extensive calculations were carried out by Patel and Scheuerer [69] for symmetric and asymmetric turbulent wake of a flat plate. The results were compared with several available experimental data. In these works, the authors used the boundary layer calculation method with zero pressure gradient and calculations were started at the trailing edge of the flat plate with initial conditions provided by experimental data. Thus, the boundary layer on the flat plate and viscous-inviscid interaction at the trailing edge of flat plate were not considered. A detailed large domain solution surrounding the trailing edge of the flat plate was obtained recently by Patel and Chen [70]. The two-layer model was adopted for the boundary layer calculation on the flat plate and the  $k - \varepsilon$  turbulence model was adopted for the wake calculation. The boundary layer on the flat plate was accurately calculated to the laminar sublayer (  $y^+ \sim 0.4$  ) by the two-layer model in which the turbulent kinetic energy and turbulent kinetic energy dissipation rate in the laminar sublayer and the buffer layer and a part of logarithmic layer are specified by universal functions based on the experimental data curve-fitting and eddy viscosity in these regions is calculated by the Van Driest

formula. Comparisons of calculated results with experimental data and results from the previous calculations were made. However, a detailed destruction of laminar sublayer and buffer layer in the wake was not calculated since the k -  $\epsilon$  turbulence model was adopted in the wake calculation. For example, the destruction of turbulent kinetic energy peak at  $y^+ \sim 15$  on the trailing edge of turbulent boundary layer and the development of wake centerline velocity in the laminar wake region were not calculated. While the two layer model predicted a reasonably accurate result, it requires many computational nodes in the near wall region over the plate. It is quite questionable that the present low Reynolds number turbulence model can be used confidently for the prediction of rapid mixing in the laminar wake region although it has been successful in the various calculations of boundary layer type flow.

The purpose of the present study is to develop a calculation method in which the concept of a wall function method is adopted and extended to the wake calculation.

In this approach, the laminar wake region is excluded from the calculation domain and wake functions are introduced to accurately account for the large streamwise velocity gradient along the wake centerline in the same spirit that wall functions are used in the near wall calculation. It

is shown that the application of the combination of wall and wake function may satisfactorily predict the turbulent boundary layer on the plate, the trailing edge interaction and the development of turbulent wake.

# IV.2 Numerical Grids and Solution Domains

The solution domain shown in Fig.IV-1 consists of wall function region, wake function region, and calculation region. The wall function region is one computational control volume over the plate which extends from  $y^+ = 0$  to  $y^+ \sim 150$ . The wake function region is one computational control volume just downstream of the trailing edge of flat plate extending approximately from  $x^+ = 0$  to  $x^+ \sim 500$  in the wake region.

Non-uniform 57x31 grids are generated numerically by the grid generation technique outlined in chapter II-4-1 with exponential distribution along the y-direction and sinusoidal distribution along the x-direction so that an appropriate grid concentration can be made close to the wall and near the trailing edge of flat plate as shown in Fig.II-3. The details of informations on grid and sizes of solution domains are given in Table 2. The numerically generated coordinate lines are treated as control volume lines and grid lines are placed at the center of control

volume lines as suggested by Patankar [2]. Of the 31 grid points in the y-direction, 10 grid points are placed within the boundary layer on the body. The origin of coordinate system is placed at the trailing edge of plate.

## IV.3 Boundary Conditions

The upstream inlet condition for u-velocity is specified by the following simple flat-plate correlations [71].

$$u = \left(\frac{Y}{\delta}\right)^{1/7} \tag{IV-1}$$

$$\delta(x) = 0.37 \times (R_e \times)$$
 (IV-2)

where  $\delta$  (x) denotes the boundary layer thickness at distance x from the leading edge and  $R_{\rm e}$  is the Reynolds number based on the free stream velocity and plate length.

The upstream inlet condition for turbulent kinetic energy and the rate of turbulent kinetic energy dissipation are specified by following simple relations.

$$k = c_{\mu}^{-1/2} u_{\tau}^{2} (1 - \frac{y}{\delta})$$
 (IV-3)

$$\varepsilon = c_{\mu}^{3/4} k^{3/2} / 1_{m}$$
 (IV-4)

where  $u_{\tau} = (\tau_w/\rho)^{1/2}$  is the friction velocity,  $c_{\mu} = 0.09$  and the length scale  $l_m$  is calculated by Escudier formula [72].

$$y/\delta < c_{\mu}/\kappa$$
 ,  $l_m = \kappa y$  (IV-5)

$$y/\delta > c_{\mu}/\kappa$$
 ,  $l_m = c_{\mu}\delta$  (IV-6)

In the wall function region, u, k, and  $\epsilon$  are calculated by the following conventional relations [43].

$$\frac{\mathbf{u}}{\mathbf{u}_{\tau}} = \frac{1}{\kappa} \ln \mathbf{y}^{+} + \mathbf{B} \tag{IV-7}$$

$$k = c_{\mu}^{-1/2} u_{\tau}^{2}$$
 (IV-8)

$$\varepsilon = u_{\tau}^{3} / \kappa y \tag{IV-9}$$

where  $y^+ = R_e u_{\overline{t}} y$ ,  $\kappa$  is von-Karman constant,  $\kappa = 0.42$  and B = 5.5.

The two point wall function method used in the present study is a slightly different from the wall function method generally used in the control volume method. It is assumed that at least two u calculation nodes are placed in the logarithmic region. The friction velocity  $\mathbf{u}_{\tau}$  is first determined by iterative method using the u value in the third node (  $\mathbf{y}^{+}$  ~ 150 ) and Eq.(IV-7). Then the  $\mathbf{u}$ ,  $\mathbf{k}$ ,  $\mathbf{\epsilon}$  values in the second node (  $\mathbf{y}^{+}$  ~ 60 ) are

evaluated using this friction velocity and Eqs.(IV-7)-(IV-9).

In the wake function region, the wake centerline velocity  $\mathbf{u}_{\mathbf{C}}$ , and other variables,  $\mathbf{v}_{\mathbf{w}}$ ,  $\mathbf{k}_{\mathbf{w}}$ , and  $\boldsymbol{\varepsilon}_{\mathbf{w}}$  are specified at the locations as shown in the Fig.IV-2. Detailed specification and explanation of these wake functions will be given later.

The other boundary conditions are sama as those reported in chapter II-3-2.

#### IV.4. Wake Function Method

IV.4.1. Significance of Wake Function Method.

One of the difficulties that arises in the prediction of wake flow is that when the turbulent boundary layer leaves the trailing edge of flat plate, the turbulent structure of flow changes rapidly because the no slip condition on the plate abruptly changes to the symmetry condition in the wake. There is a rapid mixing near the wake centerline and the turbulent boundary layer on the plate breaks down and developes into the wake. The flow development in the wake can be divided into three fundamental regions as mentioned before. The practical difficulty encountered in the calculation of turbulent

wake is that none of the present turbulence models can be used confidently for the calculation of the laminar wake and far wake. On the other hand, it is not easy to capture numerically the rapid variation of turbulent structure near the wake centerline unless large number of nodes are placed near the trailing edge. The same difficulties are also encountered in the calculation of flow near the wall. The wall function is introduced to circumvent these two difficulties. In the present study, we introduce wake functions which may account for the development of velocity along the wake centerline while laminar wake region is excluded from the calculation The detailed calculation in the laminar wake region and the uncertainty of the turbulence model in the laminar wake calculation can be removed by this approach. If there is no separation near the trailing edge of the body like present problem, the downstream near wake calculation is strongly depends on the flow condition immediately downstream of the trailing edge. proper imposition of the wake function may reduce the error initiated by the wake inlet condition.

One of the difficulties in the calculation of a symmetric wake when the wall function method is used in the calculation of boundary layer of body is the imposition of symmetry condition for the u-velocity along

the wake centerline in the turbulent inner near wake region. In the initial phase of this study, an interpolation function which satisfies the symmetry condition along the wake centerline was used for the evaluation of quantities of the first control volume in the wake and along wake centerline while calculations were carried out from the second control volume. The square interpolation function,  $Ay^2 + B$ , was used for the evaluation of u, k,  $\varepsilon$  and linear interpolation function, Ay, was used for the evaluation of v. However, these interpolation functions do not accurately account for the physical behaviour of the flow. The errors generated by these interpolation functions thus affect the solution in the normal direction by diffusion and in the downstream direction by convection. As a result, the downstream calculation, particularly in the turbulent near wake region, suffers from these errors.

According to the theory of Alber [62], the mean x-directional velocity component has the logarithmic behaviour of the turbulent boundary layer in the turbulent inner near wake region although it breaks down as the flow moves downstream. In the present study, the first x-directional computational grid in the wake region is placed at the starting point of turbulent inner wake region ( $x^+ \sim 250$ ) and the first three y-directional u-

velocity calculation nodes are placed at the logarithmic layer ( $y^+ \sim 60$ , 150, 250). Thus, the computational nodes used in the interpolation function for the initial portion of turbulent inner near wake region are placed in the logarithmic layer. The discrepancies between the physical behaviour and interpolation functions result in a considerable error, especially in the evaluation of uvelocity. If the square interpolation function is used in the evaluation of u-velocity, it gives a higher uvelocity values for the second node and the wake centerline. Consequently, this higher u-velocity influences the generation term of kinetic energy in the third node. Thus, the turbulent kinetic energy is underpredicted. These errors can be reduced if many finer grids are placed near the wake centerline. However, there is a limit because the wall function used in the boundary layer calculation can only be applied to the region 60 <  $y^+ < 400$ . On the other hand, only the laminar sublayer,  $y^+ < 10$ , from the boundary layer flow is destroyed in the starting portion of turbulent inner wake region. In other words, the wake symmetry condition satisfies only about a laminar sublayer thickness above the wake centerline. Thus, an accurate resolution of the symmetry condition along the wake centerline by a simple interpolation function is impossible, and more importantly, the solution

will be quite grid dependent. It is quite apparent that a direct imposition of the symmetry condition  $\phi(i,2)=\phi(i,1)$  over a distance of  $\Delta y^+$  in the order of 60 should cause severe error.

One possible way of avoiding these errors will be a direct calculation along the wake centerline with the inlet condition provided properly. If we consider the calculation of asymmetric wake, the whole domain should be calculated. Rhie and Chow [16] performed the whole domain calculation even in the symmetric wake calculation to avoid numerical error from interpolation along the line of symmetry. However, details of the inlet conditions of transport quantities for the wake calculation immediately downstream of the plate were not explained in their paper.

Since the k - E turbulence model is used in this study, the control volume which contains the laminar wake region should be excluded from the wake calculation.

Since the laminar sublayer and buffer layer and a part of the logarithmic layer in the boundary layer on the body are not calculated in the wall function method, the detailed destruction of these layers in the wake can not be calculated. Thus a universal function which can resolve the large streamwise velocity gradient caused by the destruction of these layers should be used in the wake

function region. The idea of creating the wake function is the same as that the wall function is introduced in the calculation of boundary layer on the body.

## IV.4.2. Proposed Wake Functions.

In order to adopt a wake function, we note that Alber [62] obtained the mean velocity profile in the turbulent inner near wake region using the boundary layer approximation and similarity transformation under the assumption of a linear distribution of eddy viscosity in the normal direction. The wake centerline velocity and velocity components near the wake centerline in the turbulent inner near wake region are

$$\frac{u_{C}}{u_{\tau o}} = \frac{1}{\kappa} [\ln g(x^{+}) - \gamma] + B$$
 (IV-10)

$$\frac{u}{u_{\tau 0}} = \frac{1}{\kappa} [\ln y^{+} + E_{1}(\zeta)] + B$$
 (IV-11)

$$\frac{v}{u_{to}} = \kappa \left[ 1 - \exp(-\zeta) \right] / \ln g(x^{+})$$
 (IV-12)

where

$$x^{+} = R_{e} u_{to} x$$
,  $y^{+} = R_{e} u_{to} y$ ,  $\zeta = y^{+}/g(x^{+})$   
 $\infty$   
 $E_{1}(\zeta) = \int \exp(-t)/t dt$ 

and

$$g(\alpha) [ ln g(\alpha) - 1 ] = \kappa^2 \alpha$$
 (IV-13)

and  $u_{TO}$  is the trailing edge friction velocity and  $\gamma$  ( = 0.5772157 ) is the Euler constant. The constants  $\kappa$ , B in these equations were taken as  $\kappa$  = 0.42, B = 5.5 for the consistency with the wall function. Eq.(IV-12) was obtained from Eq.(IV-11) and continuity equation.

One may alternatively use the centerline velocity formula given in Eq.(IV-10) with the correlation obtained from experiment by Andreopoulos and Bradshaw [66];

$$\frac{u_{C}}{u_{70}} = 2.02 \ln x^{+} + 0.7$$
 (IV-14)

Alber's solution, Eq.(IV-10), is used as the inlet condition for the downstream wake centerline u-velocity calculation in this study.

For the proper introduction of wake functions for the turbulent quantities in the wake function region, we may consider Chevray and Kovasnay's data [63]. They show that the turbulent structure in the logarithmic layer from the trailing edge of the flat plate to the starting point of turbulent inner near wake region remains the same although the structure of laminar sublayer and buffer layer evolve rapidly by means of mixing in the laminar wake region. Therefore, we may use the second y-directional nodal values of the k and  $\varepsilon$  at the trailing edge of plate as the second y-directional nodal values of k and  $\varepsilon$  in the first

control volume in the wake, as shown in Fig.IV-2, without loss of accuracy. Obviously, a direct calculation of these quantities is impossible since the calculation point for  $k_W$  and  $\epsilon_W$  is located immediately downstream of the the trailing edge where the centerline u-velocity can not be calculated. We thus adopt

$$k_{w} = c_{u}^{-1/2} u_{\tau o}^{2}$$
 (IV-15)

$$\varepsilon_{\rm w} = u_{\rm TO}^3 / \kappa y$$
 (IV-16)

as the second nodal values of the turbulent kinetic energy and the rate of its dissipation in the first control volume in the wake. Here,  $\mathbf{u}_{to}$  is the trailing edge friction velocity.

There is no detailed experimental observation made for the variation of k and  $\epsilon$  along the wake centerline within our knowledge. This lack of inlet conditions for k and  $\epsilon$  along the wake centerline lead us to use the interpolation function ( $\phi = Ay^2 + B$ ) in the subsequent calculation of k,  $\epsilon$  along the wake centerline. However, this does not create error in the calculation of k,  $\epsilon$  in the second node in the wake because the value of k and  $\epsilon$  in the second node in the wake are more dependent on the generation term of the turbulent kinetic energy than the k,  $\epsilon$  values along the wake centerline. In other words,

accurate resolution of the wake centerline velocity is more important for the accurate prediction of second nodal turbulent kinetic energy than the specification of k and  $\epsilon$  along the wake centerline.

# IV.4.3 Enforcing the Conservation of Mass

An important problem in the calculation of wake by the wall and wake function method is the calculation of the second nodal v-velocity component in the wake region. The difficulty arises from the fact that the detailed destruction ( mixing ) of laminar sublayer and buffer layer and logarithmic layer in the first y-directional control volume in the wake can not be properly described in the wall function method due to the lack of computational nodes near the wake centerline. Obviously, this is more severe in the calculation of the intial portion of turbulent inner near wake. To avoid these numerical difficulties, we adopt PSL ( Parabolic Sublayer ) like treatment [73]. In this study, the second nodal vvelocity in the wake which is denoted as  $v_2$  in Fig.IV-2 is calculated by the mass conservation of the first control volume using the following simple integration formula.

$$\Delta x_c v_2 = \int_0^{\Delta y_c} u_1 dy - \int_0^{\Delta y_c} u_2 dy \qquad (IV-17)$$

where

$$\int_{0}^{\Delta y_{C}} u \, dy = \left( \frac{1}{3} u(i,1) + \frac{13}{24} u(i,2) + \frac{1}{8} u(i,3) \right) \Delta y_{C}$$
(IV-18)

The accuracy of the integration formula is very significant in the wake calculation since a small error in mass conservation may lead to a large error in the prediction of the pressure field in the weak interaction like present problem. It is not easy to find a good integration formula which can accurately resolve the mass flux of laminar sublayer, buffer layer and a part of logarithmic layer at the trailing edge of body ( x = 0 ) so that  $v_w$  in Fig.IV-2 can be calculated by Eq.(IV-17). Thus the Eq. (IV-12) is used only for the specification of the v-velocity component in the wake function region ( v., in Fig. IV-2 ) for simplicity and accuracy. The pressure in the wake is calculated from the third node in the ydirection using these v-velocity components as velocity boundary condition. The u-velocity component in the second node is calculated using the pressure in the third The starting point of calculation in the ydirection in the wake region is shown in Fig. IV-2.

## IV.5. Results and Discussions

Calculations were performed using the partially parabolic form of finite analytic method which is derived in chapter II-5-1 and SIMPLER numerical algorithm outlined in chapter III-4. The derivation of pressure and pressure correction equation is given in chapter III-2. The time marching technique is employed for the iteration process and satisfactory convergence were obtained after 100 time marching with time step  $\Delta t = 1$ .

The calculation is made for Reynolds number  $2.48 \times 10^6$  based on the plate length and free stream velocity. The predicted results are presented and compared with available experimental data of Ramaprian et al. [64] who measured the mean velocity and turbulent quantities in the turbulent inner near wake region.

The converged pressure distribution near the trailing edge of the flat plate along  $y^+ \sim 150$  over the plate and wake centerline is shown in the Fig.IV-3. Fig.IV-3 shows the pressure near the trailing edge, either upstream or downstream, is lower than the free stream pressure which is set equal to zero. The minimum pressure is located at the trailing edge where the fluid experiences the maximum acceleration and deceleration. According to Alber [62],

the pressure gradient effect is mainly confined to a small laminar wake region close to the trailing edge where  $x^+ < 100$ . Obviously, the present wall and wake function method together with the  $k-\epsilon$  turbulence model can not predict the detailed interaction in this laminar wake region. However, the sharp reduction followed by a rapid increase of pressure near the trailing edge and its slow recovery in the wake is predicted by the present method as shown in Fig.IV-3. The prediction of pressure distribution by Patel and Chen [70] by two-layer model is given in Fig.IV-4. There exists a small difference between the present prediction and the calculation by Patel and Chen [70] in the region of plate. However, both predictions give nearly the same magnitude of trailing edge interaction.

The calculated result of the skin friction coefficient is shown in Fig.IV-5 and compared with the conventional flat-plate correlation. In general, Fig.IV-5 shows a good agreement between the predicted value and simple flat plate correlation. Since the pressure on the plate drops rapidly near the trailing edge causing the boundary layer to accelerate, the skin friction coefficient near the trailing edge is expected to increase. This increase, even though it is small, is well predicted in the present calculation.

Fig.IV-6 shows the comparison of the predicted wake centerline velocity distribution with experimental data by Ramaprian et al.[64] The first computational node along the centerline is located approximately at x<sup>+</sup> ~ 250. An excellent agreement is obtained by the application of wall and wake function method. As compared with the predicted wake centerline velocity distribution by Patel and Chen [70], which is shown in Fig.IV-7, the present wake function method accurately predicts the wake development without the detailed calculation of the laminar sublayer on the plate and the laminar wake.

Figs.IV-8, IV-9, and IV-10 show the detail of the predicted u-velocity component, Reynolds shear stress and turbulent kinetic energy. The comparison of the predicted results with experimental data is excellent. As mentioned before, the direct imposition of symmetry condition or the use of interpolation function as the symmetry condition for u-velocity along the centerline may lead to predictions of a higher u-velocity and lower turbulent kinetic energy due to the inadequate grid concentration near the wake centerline when the wall function method is adopted in the calculation of boundary layer on the body. On the other hand, the present method of combining the wall and wake function clearly removes these difficulties.

It should be mentioned that while the selection of appropriate wake functions is important, an accurate evaluation of the second nodal v-velocity component is also important in achieving the accurate prediction of the near wake turbulent structure. We note that the turbulent kinetic energy and turbulent shear stress measurements of Ramaprian et al. [64] give slightly higher values than those of Pot [65] in the initial portion of turbulent inner near wake region which can be seen at the locations x = 25.4 mm and x = 127 mm.

A proper prediction of the v-velocity component in the turbulent near wake region is very significant for the accurate prediction of the flow structure since the amount of mixing in this region is more or less related to the v-velocity component. The second nodal v-velocity in the wake region calculated from the present PSL (parabolic sublayer) like treatment can not be confirmed due to the lack of experimental data. A comparison with Alber theory [62] is made. Two calculations are performed with a different grid distribution near the wake centerline,  $\Delta y_c^+$  120 (grid 1),  $\Delta y_c^+$  200 (grid 2) where  $\Delta y_c^-$  is the size of the first y-directional control volume in the wake as shown in Fig.IV-2. Fig.IV-11 shows the comparison of the present prediction with Alber theory [62] in the turbulent inner near wake region. Good agreement is

obtained but the integral formula gives a little grid dependency.

Fig. IV-12 and Fig. IV-13 indicate the prediction of velocity defect and Reynolds shear stress in the far wake region where the velocity defect w ( = 1 - u ) becomes small compared with u-velocity component. The assumption of similarity of velocity and shear stress profiles leads the half power law for the decay of the centerline velocity defect  $w_0$  ( = 1 -  $u_c$ ) and the growth of the half width b (  $y_h$  = b/2 where w/w<sub>0</sub> = 1/2 ). According to asymptotic theory [71],

$$b \sim x^{1/2}$$
,  $w_0 \sim x^{-1/2}$  (IV-19)

A simple velocity defect and shear stress distribution can be obtained [69] when one introduces a constant eddy viscosity across the wake in the normal direction for the momentum equation.

$$w/w_{0} = \exp(-4 \ln 2 \eta^{2})$$
 (IV-20)  
$$-\overline{uv}/w_{0}^{2} = 4 (\pi \ln 2)^{1/2} (v_{t}/u\theta) \eta \exp(-4 \ln 2 \eta^{2})$$
 (IV-21)

where  $\eta$  = y/b, and  $v_t/u\theta$  = 0.032 which has been confirmed by Rodi [74] from a survey of several sets of experimental data. Fig.IV-12 and Fig.IV-13 show the

comparison between present prediction and asymptotic theory, Eq.(IV-20) and Eq.(IV-21). The velocity defect, in general, is predicted well except near the edge of the wake where the computed profile underpredicted the asymptotic value. This may be due to the fact that the turbulence model can not properly simulate the high intermittance of turbulent and laminar flow occurring at the edge of the wake. On the other hand, the turbulent shear stress is underpredicted. This is a well known defect of the current  $k - \epsilon$  turbulence model which was already observed in the previous calculations [67], [69], and [70]. An improvement in the turbulence modelling is required in order to achieve a better agreement in the prediction of turbulent structure in the far wake region with the experiment. For example, Chen and Singh [75] showed a better prediction can be achieved with the k -  $\epsilon$ model based on the two turbulence scale concept where the first scale is based on the turbulent kinetic energy, k, and its dissipation rate,  $\varepsilon$ , to characterize the large, energy-containing eddies while the second scale, the Kolmogorov scale, is based on the dissipation reate, £, and the kinematic viscosity, V, to characterize the small, energy-dissipating eddies.

A more sophisticated analysis of wake functions and related calculation method is needed for the application

of the present method to the calculation of wakes behind bodies of streamline curvature for which the pressure gradient effect are important.

## IV.6. Conclusion

A new calculation method is presented in the present study for an accurate prediction of turbulent wake flow behind a flat plate. The method proposes a wake function that models the laminar and turbuent wake immediately downstream of the trailing edge of the plate from  $\mathbf{x}^+ = 0$  to approximately  $\mathbf{x}^+ = 250$ . The combination of the wake function for the near wake region and the wall function for the near wall region on the plate provides a means for accurate prediction of turbulent wake flow and eliminates excess computational grids required near the wall and the trailing edge and the uncertainty of the turbulence model.

#### CHAPTER V

#### LAMINAR AND TURBULENT FLOW PAST A FINITE FLAT PLATE

# V.1 Introduction

The classical problem of incompressible laminar and turbulent flow past a finite flat plate has been studied by numerous investigators. It is a problem that not only provides much fundamental understanding of basic feature of leading and trailing edge interaction, boundary layer on the plate and wake development, but also of considerable importance in diverse engineering applications such as thin airfoil theory.

When the Reynolds number based on the plate length and the free stream velocity is large, the laminar boundary layer on the plate is described by the well-known Blasius solution. However, the Blasius solution, which is based on the boundary layer theory of Prandtl, does not properly describe the flow field near the leading and trailing edges of plate due to the breakdown of assumptions made in the boundary layer theory.

Due to its geometric simplicity, the laminar flow near the trailing edge of plate has been subject of

various numerical and theoretical investigations. The study of this problem provides us the basic understanding of inviscid-viscous interaction at the trailing edge and near wake development. According to the triple deck theory of Stewartson [76] or Messiter [77], for infinite Reynolds number flow, the laminar boundary layer on the plate develops into Goldstein's near-wake through a small transition region around the trailing edge which is known as the triple-deck region. This triple deck region which is embedded inside the boundary layer near the trailing edge arises in order to avoid the singularity of the boundary layer equations at the trailing edge. Melnik and Chow [78] and Veldmen and van de Vooren [79] have obtained the numerical solutions of the triple deck equations.

The breakdown of boundary layer theory for describing the flow field near the trailing edge of plate leads many investigators to use alternative approaches. Two approaches are commonly used: the inviscid-viscous interaction method [80]; and the numerical solutions of fully elliptic or partially parabolic form of equations [81,82]. Recently, Chen and Patel [81] have obtained the numerical solutions of this problem using the elliptic form of finite analytic numerical scheme. The grid dependence and convergence tests, the influence of the size of solution domain on the solution were investigated

in detail. The predicted results were compared with previous results by interacting boundary layer theory and by partially parabolic numerical solution. One valuable observation made in this study is that the solution domain should be larger than that used in the previous studies in order to capture the whole inviscid-viscous interaction and far wake development and to obtain domain independent solution. The same observation is also reported in Rhie [83] in the calculation of laminar flow past a thin airfoil.

However, most of the previous studies are confined to the analysis of the flow field near the trailing edge.

Thus the leading edge interaction and the initial development of boundary layer near the leading edge were not considered. In order to remove the dependency of the solution on the location of inlet solution boundary and to obtain whole flow field past a plate, the calculations should be started at the upstream of the plate with inlet conditions provided by uniform flow conditions. The earlier numerical solutions of the full Navier-Stokes equations obtained by Dennis and Dunwoody [84] are limited to relatively low Reynolds number flow. Xu and Chen [82] has recently obtained a numerical solution of complete laminar flow field past a finite flat plate using a novel nine-point finite analytic numerical scheme. The

predicted results of pressure distribution on the plate and along the wake centerline, the wake centerline velocity development and the friction coefficient distribution near the trailing edge were presented with comparision with previous studies.

In the present study, the classical problem of laminar and turbulent flow past a finite plate is reconsidered. The laminar flow past a finite flat plate is first solved using both partially parabolic form of finite analytic numerical method given in chapter II-5-1 and elliptic form of finite volume method with modified TEACH code. This practice will not only give a critial evaluation of suitability of the partially parabolic form of Navier-Stokes equations in the prediction of the strong leading edge interaction but also provide us the comparisions of results by both methods which has not been made before. Then the numerical solutions of turbulent flow past a finite flat plate is obtained by solving the Reynolds averaged Navier-Stokes equations with the k -  $\epsilon$ turbulence model and the wall function method. The finite volume method is used in this calculation. This practice will show how the introduction of turbulence model influences the overall solution. The predicted results are compared with available experimental data of Ramaprian et al. [64].

#### V.2. Numerical Grids and Solution Domains

The numerical grids are generated using the method outlined in chapter II-4-1 and the partial view of generated grids are shown in Fig.II-3 for both laminar and turbulent calculations. Table-3 shows the details of solution domain and number of computational grids used in the present calculations. The solution domain in normal direction for laminar flow calculation is chosen to be  $y_u \sim 12L$  in which Chen and Patel [81] obtained the domain independent solution. The solution domain in the other directions is also made large enough to capture the whole leading and trailing edge interactions. The generated numerical grids are treated as control volume lines and the computational grid lines are placed at the center of control volume lines.

# V.3 Boundary Conditions

The upstream boundary conditions are specified by following uniform flow conditions;

$$u = 1$$
,  $v_x = 0$ ,  $k = k_{in}$ ,  $\varepsilon = \varepsilon_{in}$  (V-1)

where  $k_{in}$  and  $\epsilon_{in}$  is specified as follows

$$k_{in} = 1.5 (Tu)^2$$
 (V-2)

$$\varepsilon_{in} = c_{\mu} k_{in}^{3/2} / l_{in}$$
 (V-3)

and the turbulent intensity, Tu = 0.5% and length scale,  $l_{in} = 0.03L$  are used in the present calculations.

For laminar flow calculations, the no-slip condition is specified on the plate. The wall function approach of Launder and Spalding [43] is used for turbulent flow calculation. The other boundary conditions are same as those reported in chapter II-3-2.

### V.4 Numerical Method

The finite analytic computer code used in the previous chapter is modified for the laminar flow calculation. The well-known TEACH code [86] is used for finite volume calculations with subtantial modification. The solution procedures outlined in chapter III-4 are implemented to TEACH code which includes the change of numerical algorithm, from SIMPLE to SIMPLER and the usage of parabolic marching technique with global pressure calculation procedure instead of fully elliptic calculation procedure. Details of TEACH code are well-documented in reference [86] and are not explained here.

#### V.5 Results and Discussions

# V.5.1 Laminar Flow Past A Finite Flat Plate

Calculations are performed for  $Re = 10^5$  using both partially parabolic finite analytic method outlined in chapter II-5-1 and elliptic finite volume method given in reference [86]. The same numerical grids are employed for both calculations. Of 135 x-directional numerical grids, 35 grids are placed upstream of plate, 60 grids are placed on the plate and 40 grids are placed in the wake region. The first y-directional u-calculation point over the plate is made  $\Delta y = 0.35 \times 10^{-3}$  and the minimum grid size at the leading edge is made  $(\Delta x)_1 = 0.897 \times 10^{-4}$  and the minimum grid size at the trailing edge is made  $(\Delta x)_{+} = 0.2 \times 10^{-2}$ . Time marching technique is employed for finite analytic calculation with time step  $\Delta t = 1$ . The relaxation factors used in the finite volume calculation are  $\alpha_{ij} = \alpha_{ij} = 0.7$ and  $\alpha_{p} = 0.5$ . Satisfactory convergence was obtained after 500 iterations for the calculation by finite volume method ( RES =  $0.6617 \times 10^{-3}$  ) and 1000 iterations for the calculation by partially parabolic finite analytic method ( RES =  $0.2891 \times 10^{-3}$  ) where RES denotes sum of mass residuals in pressure correction equation divided by inlet flow rate. It was observed that the velocity components

and pressure field are settled down within 200 iterations and the rest computational efforts are devoted to reduction of the mass residuals to a certain degree.

The predicted pressure distribution on the plate and along the wake centerline is shown in Fig.V-1. As shown in the figure, the magnitude of leading edge interaction is lager than the magnitude of trailing edge interaction. However, the interacting region near the leading edge is smaller than the interacting region near the trailing edge. The comparision of predicted pressure distributions by two different numerical schemes shows that both methods predicted nearly same pressure distribution except near the leading edge. The supurious pressure drop near the leading edge predicted by the present partially parabolic numerical scheme is not observed in the present elliptic calculation or in the nine-point elliptic calculation by Xu and Chen [82]. This fact shows that the partially parabolic assumption may not be appropriate for the simulation of strong leading edge interaction. However, it is also shown that the partially parabolic assumption is valid for the prediction of most of the boundary layer on the plate, the trailing edge interaction and wake development.

The enlarged view of pressure distribution near the trailing edge is shown in Fig.V-2. The magnitude of trailing iteraction predicted by finite volume method (~-0.01563) is slightly higher than that predicted by partially parabolic finite analytic method (~-0.01474). The origin of this difference is not clearly understood. For reference, the trailing edge pressure predicted by Chen and Patel [81] using elliptic finite analytic method is reported as ~0.0152.

Fig.V-3 shows the distribution of friction coefficient near the trailing edge by both methods. The difference in friction coefficient near the trailing edge by both methods is consistent with the predicted pressure distribution in this region. The stronger interaction cause stronger acceleration near the trailing edge and larger penetration to the upstream of the plate. This figure also clearly shows that the Blasius solution which is based on the boundary layer theory is not adequate for describing the flow field near the trailing edge.

The development of wake centerline velocity is also affected by the trailing edge interaction when the accelerated boundary layer at the trailing edge is destroyed in the wake with adverse pressure gradient.

Fig.V-4 shows the predicted wake centerline velocity

profiles in the wake region by two different numerical methods. Little difference is evident, which is consistent with the pressure distribution in this region. There may exist some effects which are caused by using different numerical treatments near the wake centerline. In the finite volume method, the wake centerline velocity do not affect the second nodal velocity in the wake by placing the control volume surface along the wake centerline and applying the symmetry condition and zero normal velocity condition. In finite analytic method, the wake centerline velocity affects the second nodal velocity. These practice may result in smaller wake centerline velocity prediction by finite analytic method. However, this effect seems to be very small since the wake centerline velocity prediction by the present elliptic finite volume method more agree well with those reported in Chen and Patel [81] who used elliptic finite analytic method. It is also noted that these two elliptic calculations have nearly same magnitude of trailing edge interaction. Although there may exist some numerical errors, it may be concluded that the fully elliptic form of discretization equation should be used in order to accurately capture the leading and trailing edge interactions and thereby accurately predict the wake development.

However, the differences of predictions by two different methods are very small and are confined to a relatively small region. These effects are not significant in the practical calculations when the interaction is not weak as in the present problem.

# V.5.2 Turbulent Flow Past A Finite Flat Plate

Calculations are performed for Re =  $2.48 \times 10^6$ , corresponding to experiments of Ramaprian et al. [64], using finite volume method with the standard k -  $\epsilon$  turbulence model and the conventional wall function method. Of 120 x-directional numerical grids, 30 grids are placed upstream of plate, 55 grids are placed on the plate and next 35 grids are placed in the wake region. The first y-directional u-calculation point over the plate is made  $\Delta y = 0.164 \times 10^{-2}$  which correspondins to  $y^+ \sim 15$  at the trailing edge. The minimum grid size at the leading edge is made  $(\Delta x)_1 = 0.323 \times 10^{-4}$  and the minimum grid size at the trailing edge is made  $(\Delta x)_1 = 0.4 \times 10^{-2}$ . The relaxation factors used in this calculation are  $\alpha_u = \alpha_v = \alpha_k = \alpha_\epsilon = 0.8$  and  $\alpha_p = 0.5$ . Satisfactory convergence was obtained after 500 iterations. (RES =  $0.4203 \times 10^{-3}$ )

Fig.V-5 and Fig.V-6 show the predicted pressure distribution on the plate and along the wake centerline.

There exists a sharp peak at the leading edge and a sharp drop at the trailing edge followed by slower recovery in the wake region. The predicted leading and trailing edge interactions in turbulent flow are much weaker than those in laminar flow by the introduction of turbulence model and insufficient grid refinement in these regions. The grid refinement in these regions is restricted since the k - £ turbulence model can only be applied to fully turbulent region. Thus the detailed interactions near the leading edge and in the laminar wake region near the trailing edge can not be captured. Patel and Chen [70] explained that the slower recovery of wake centerline pressure to ambient value is related to the isotropic eddy viscosity assumption in the k - £ turbulence model;

$$\frac{\partial p}{\partial x} \sim -\frac{2}{3} \frac{\partial k}{\partial x}$$
 (v-4)

The predicted friction velocity distribution on the plate is shown in Fig.V-7 with a comparision of the simple flat plate correlation given in Reference [87]. The strange transition near the leading edge region is due to the improper modelling of transition by  $k-\epsilon$  turbulence model which is also observed in Rhie [83] in the calculation of turbulent flow past a thin airfoil. There exist a substantial difference between the prediction and correlation even in fully turbulent region. It was found

that the underprediction of friction velocity originates from use of the wall function method. The first uvelocity calculation point over the plate is placed around  $y^{T} \sim 15$  at the trailing edge to provide proper calculation in the wake region. Thus all the first calculation points on the plate are placed in the buffer layer. However, the wall function region employed in the actual calculation is divided into only two regions, laminar flow region ( $v^{\dagger}$  < 11.63 ) and fully turbulent region (  $y^+ > 11.63$  ). Thus the wall shear stress on the plate is calculated by way of logarithmic law even though the first u-calculation point is placed in the buffer layer. As a result, the friction velocity is underpredicted even though the velocity is overpredicted. The friction velocity in the turbulent region is corrected using the third nodal u-velocity component which lie in logarithmic layer and the law of the wall. The corrected skin friction velocity is consistent with the overprediction of velocity at the trailing edge which is shown in Fig.V-9. The amount of overprediction in friction velocity is not so serious as shown in the figure. It may be suggested that the predictions will be improved if the wall shear stress in the wall function method is evaluated using the third nodal velocity component in the practical calculation. It was also found that the prediction of friction velocity

was slightly improved when the first grid over the plate was slightly increased to  $y^{+} \sim 30$ . However, this practice was abandoned due to the very poor prediction in the wake region which was explained in detail in the previous chapter. It was also observed that the prediction was extremely sensitive to the numerical grid distribution near the wall region which was not observed in the calculation of previous chapter in which two point wall function method was adopted. This sensitivity of prediction to the location of the first grid point is due to the Couette-flow type wall function method usually used in the finite volume calculations. It is noted that the two-point wall function method can not be used in the laminar flow region near the leading edge. The poor prediction of friction velocity can be improved with more advanced turbulence model which can properly describe the flow field near the viscosity-affected near wall region.

Figs.V-8, V-9 and V-10 show the predicted wake centerline velocity, mean velocity ditribution and turbulent kinetic energy distribution in the near wake region. The predicted results are only fairly good due to the improper calculation of the boundary layer on the plate. The overprediction of velocity profile at the trailing edge results in higher velocity profiles and smaller kinetic energy distribution in the near wake

region. However, these predictions are not much deviated from the experimental data as shown in these figures. It is shown that as the flow approaches downstream, the flow becomes to lose the memory of boundary layer on the plate and the predictions agree better with the experimental data.

Although only fairly good predictions were achived due to improper modelling of transition and near wall turbulence, the present study achieves the prediction of whole turbulent flow past a finite flat plate. The predictions can be improved if a suitable turbulence model is used. However, there does not exist a general turbulence model which can properly describe the transition of laminar to turbulent and the flow field in the viscosity-affected near wall region.

#### CHAPTER VI

#### TURBULENT FLOW PAST AXISYMMETRIC BODIES

# VI.1 Introduction

In order to design an optimal ship body and ship propelling system, it is very important to have a fundamental understanding and to be able to make an accurate prediction of fluid flow past various ship. bodies. The accurate prediction of turbulent flow near the ship stern region is particularly important since many propellors and appendages are located inside the ship stern boundary layers. The flow evolution in this ship stern region is characterized by a rapid growth of boundary layer, a strong viscous-inviscid interaction and a general reduction in the level of turbulence by streamline curvature and pressure gradient [88] which is quite different from that in the hull region. These flow features show that the thin boundary layer approximation is not adequate for describing the flow field around the ship stern region although it may be suitable for describing the flow field around the ship hull region.

A review of the state-of-the-art of available experimental and numerical investigations of turbulent flow past axisymmetric bodies was recently made by Patel and Chen [89]. According to this detailed survey, many reliable experimental informations are available at present which can be used to verify the accuracy of numerical calculations. Chevry [90] made measurements of mean flow and turbulent quantities in the wake of 6 to 1 spheroid. These data provide quite detailed informations on the near wake evolved from the a separated flow just ahead of the tail region of spheroid. The experiment of Patel et al. [88] was conducted on the same model but the separation was eliminated by means of a short conical tail attachment. They measured the development of thick boundary layer on this modified spheroid. Patel and Lee [91] made extensive measurements on the boundary layer and near wake development of turbulent flow past a low-drag body (F-57 body). Since above two measurements are made normal to the body surface using boundary layer coordinates, it is difficult to use these data to compare with practical calculation if numerical grids are not generated in the same manner. The extensive experimental data measured by Huang et al. [92,93,94] for four different afterbodies, afterbody-1, afterbody-2, afterbody-3, afterbody-5, provide the detailed

informations on the thick boundary layer and the near wake development. These four bodies have the same streamlined forebody and parallel middle body, but have different afterbodies. All of these bodies have an inflection point and quite dramatic changes in surface curvature which induce a strong favorable and adverse pressure gradient over the stern region and propellor hub region. In the case of afterbody-3, experimental data indicate that there is a small separation bubble around the inflection point. These data have been widely used in the previous studies [89,95,96,97,98,99] for the evaluation of calculation methods and turbulence models. These data are also used in the present study to compare with the calculated results.

Many numerical efforts have been made in the past decade to compute this complex flows near the tail region of the axisymmetric bodies. These efforts have involved with different approximations made in the governing equations, with different turbulence models and with different calculation methods. According to the survey by Patel and Chen [89], the previous calculation methods can be broadly classified into three categories, the non-interactive numerical solution of thin layer or boundary layer equation with the pressure field given by experimental data [91], the viscous-inviscid interaction

method [100,101,102] and the global numerical solutions of partially parabolic or elliptic equations [89,98]. Among these methods, the global numerical solution method is the most attractive since this method does not require the experimental informations of pressure field or another numerical solution of inviscid flow. It is interesting to note that the recently developed calculation methods outlined in chapter-I have not been applied to this problem except the works of Patel and Chen [89]. The calculation methods used by Muraoka [97,103] or Markatos [98] are not general and can only be applicable when the numerical grids are generated in a special algebraic manner. It is also noted that most of previous calculations start at the middle of body to avoid the numerical difficulties associated with the calculation near the leading edge.

In the present study, numerical solutions of partially parabolic or fully elliptic form of Reynolds-averaged Navier-Stokes equations in numerically generated, nonorthogonal coordinates are obtained through the calculation procedure outlined in chapter-II and chapter-III. The complex, physical geometry is resolved by the use of nonorthogonal, body-fitted coordinates which are generated through the solutions of Poisson equations with appropriate grid control functions. The governing

equations are written in the transformed coordinates by the partial transformation where the original orthogonal velocity components are left as dependent variables. These transformed governing equations are discretized using the finite analytic method by Chen and Chen [3] which was already explained in chapter-II. The finite volume method is also applied to some problems in order to provide comparisions of two different numerical schemes in the prediction of turbulent boundary layer and wake of axisymmetric bodies. The one-velocity staggered grid technique is employed for all the calculations presented in this chapter. The derivation of pressure and pressure correction equations in this grid configuration is given in chapter III-3-1.

Since there are strong pressure gradient and streamline curvature effects on the flow near the stern region, some considerations should be made for the selection of turbulence model. The zero equation models of Cebeci-Smith model or Baldwin-Lomax model and the one equation model have been used in the earlier calculations [91,95,96,101] with some modifications. However, the  $k-\epsilon$  turbulence model with wall function method has been the most widely employed in the recent calculations [89,97,102,103]. The defect of the  $k-\epsilon$  turbulence model in the calculation of flow involving pressure gradient

effect is well explained by Rodi and Scheuerer [54]. poor performance of the current  $k - \epsilon$  turbulence model is caused by inaccurate modelling of the  $\varepsilon$  - equation. For example, the length scale determined using the  $\epsilon$  - equation rises steeper near the wall region in the adverse pressure gradient region while the experimental data shows that the length scale is virtually independent of the presure gradient. By this reason, the turbulence models using the empirical length scale specification near the wall region yield much better predictions for the adverse pressure gradient boundary layers than does the current  $k - \epsilon$ turbulence model. Rodi and Scheuerer [54] suggest use of Hanjaliac and Launder's model [104]. On the other hand, Chen and Patel [56] developed a two-layer turbulence model to consider the pressure gradient and streamline curvature effects and flow separation. Their model has been successfully applied to the prediction of turbulent flow past axisymmetric bodies.

In the present study, some calculations are performed using the conventional  $k-\epsilon$  turbulence model and wall function method in which the pressure gradient effect is embodied in the wall function while some calculations are performed using the two-layer turbulence model of Chen and Patel [56].

## VI.2 Two-Laver Model

In the two-layer model, the calculation region is divided into two regions; a near wall region and an outer region, as shown in the Fig.VI-1. The boundary between the near wall region and the outer region is placed around  $y^+ \sim 100$ . The near wall region includes the laminar sublayer, buffer layer and a part of logarithmic layer ajacient to the body. In this region, calculations are carried all the way to the wall using the one equation turbulence model where the rate of turbulent kinetic energy dissipation  $\epsilon$  and the turbulent eddy viscosity  $\nu_t$  is specified by algebraic relations to consider the wall proximity viscous effects. The outer region is the upper region of the near wall region over the body and the whole wake region. The standard  $k - \epsilon$  turbulence model is used to simulate this fully turbulent region.

Three one equation turbulence models such as Hassid and Poreh's model [48], Norris and Reynolds's model [49], Wolfshtein's model [47] were tested in the course of present investigation. However, the Wolfshtein model is chosen in the present study by the simple reason that the other two models slightly overpredict the wall shear stress compared with the Wolfshtein model.

In the Wolfshtein model, the turbulent eddy viscosity  $v_t$  and the rate of turbulent kinetic energy dissipation  $\epsilon$  is specified by a simple algebraic form as following;

$$\varepsilon = \frac{k^{3/2}}{l_{\varepsilon}}$$
 (VI-1)

$$v_t = c_{\mu} k^{1/2} l_{\mu}$$
 (VI-2)

where the length scales  $\mathbf{1}_{\epsilon'}$   $\mathbf{1}_{\mu}$  contain the viscosity damping effect in the near wall region in terms of turbulent Reynolds number  $\mathbf{R}_{k}$  .

$$l_{\mu} = c_1 n [1 - exp(-R_k / A_{\mu})]$$
 (VI-3)

$$1_{\varepsilon} = c_1 n \left[ 1 - \exp(-R_k / A_{\varepsilon}) \right]$$
 (VI-4)

where

$$R_k = \text{Re n } k^{1/2}$$
,  $c_{\mu} = 0.09$ ,  $c_1 = \kappa c_{\mu}^{-3/4}$ ,

$$A_{\epsilon} = 2 c_{1}, A_{\mu} = 70.$$

and n is the normal distance from the wall.

These constants are evaluated by Chen and Patel [56] and somewhat different from those reported in Wolfshtein [47] or Yap [58].

### VI.3. Numerical grids and Solution Domains

The numerical grids are generated using the grid generation technique outlined in chapter II-4-2. The generated numerical grids for four different afterbodies are shown in Fig.II-4. The detailed informations on the solution domains are given in Table 4 and Table 5. These solution domains are large enough to capture the whole viscous-inviscid interactions and wake development.

# VI.4 Boundary Conditions

In the half body calculations using the wall function method, the upstream inlet conditions were specified by following simple correlations.

$$\frac{u}{u_{\tau}} = \frac{1}{\kappa} \ln y^{+} + B \qquad (VI-5)$$

$$k = c_{\mu}^{-1/2} u_{\tau}^{2} (1 - \frac{y}{\delta})$$
 (VI-6)

$$\varepsilon = c_{\mu}^{3/4} k^{3/2} / \kappa y \qquad (VI-7)$$

where y<sup>+</sup> = R<sub>e</sub> u<sub> $\tau$ </sub>y,  $\kappa$  is von-Karman constant,  $\kappa$  = 0.42 and B = 5.5. The boundary layer thickness  $\delta$  and friction velocity u<sub> $\tau$ </sub> =  $(\tau_w/\rho)^{1/2}$  are provided by experimental data.

The wall function method employed in the present study is a little different from the conventional wall

function method usually used in the control volume method. In the present study, it is assumed that at least two ucalculation nodes are located in the logarithmic region. The friction velocity  $\mathbf{u_t}$  is first determined by iterative method using the velocity components in the third node which is obtained from the previous iteration and following the generalized form of the law of the wall [4] in which the pressure gradient effects on the flow in the wall region are taken into consideration.

$$\frac{q}{u_{\tau}} = \frac{1}{\kappa} \left\{ \ln \left[ \frac{4}{\Delta_{\tau}} \frac{(1 + \Delta_{\tau} n^{+})^{1/2} - 1}{(1 + \Delta_{\tau} n^{+})^{1/2} + 1} \right] + 2 \left[ (1 + \Delta_{\tau} n^{+})^{1/2} - 1 \right] \right\} + B + 3.7 \Delta_{p} \text{ (VI-8)}$$

where n<sup>+</sup> = Re u<sub>t</sub>n is dimensionless, normal distance from the surface,  $\Delta_{\rm p} = -\Delta {\rm p}$  / (Re u<sub>t</sub>) is the dimensionless pressure gradient on the body surface,  $\Delta_{\rm t}$  is the dimensionless shear stress gradient and is assumed to be  $\frac{1}{2}$   $\Delta_{\rm p}$ , q is the magnitude of velocity or q = (u<sup>2</sup> + v<sup>2</sup>)  $^{1/2}$ ,  $\kappa$  = 0.418 is the von-Karman constant, and B = 5.45.

Then the magnitude of velocity in the second node  $q_2$  can be calculated using this friction velocity and Eq.(VI-8) while the velocity components parallel to  $\xi$  - grid line are calculated by the following relations.

$$q_3^{\xi} = \frac{\sqrt{g_{11}}}{J} r (b_1^1 u_3 + b_2^1 v_3)$$
 (VI-9)

$$q_2^{\xi} = \frac{q_2}{q_3} q_3^{\xi}$$
 (VI-10)

where the geometric coefficients J and  $b_{i}^{i}$  are given in Eqs. (II-58) and (II-59) and  $g_{11} = x_{\xi}^2 + y_{\xi}^2$ .

The u, v, k,  $\varepsilon$  values at the second node are evaluated using the friction velocity and following relations.

$$u_{2} = \frac{x_{\xi}}{\sqrt{g_{11}}} q_{2}^{\xi}$$

$$v_{2} = \frac{y_{\xi}}{\sqrt{g_{11}}} q_{2}^{\xi}$$
(VI-11)
$$(VI-12)$$

$$v_2 = \frac{y_\xi}{\sqrt{g_{11}}} q_2^{\xi}$$
 (VI-12)

$$k_2 = c_{\mu}^{-1/2} u_{\tau}^2$$
 (VI-13)

$$\varepsilon_2 = u_{\tau}^3 / \kappa y$$
 (VI-14)

The details of this two-point wall function method is given in Chen and Patel [4]. The advantage of this twopoint wall function method is that the sensitivity of the solution to the location of the first grid point, which is found in other Couette-flow type wall function method usually used in the control volume method, is removed.

In the two-layer calculations, the upstream uvelocity boundary condition near the wall is specified by following Spalding's velocity law:

$$y^{+} = u^{+} + e^{-\kappa B} [e^{-\kappa u^{+}} - 1 - \kappa u^{+} - (\kappa u^{+})^{2}/2$$

$$- (\kappa u^{+})^{3}/6] \qquad (VI-15)$$

The inlet boundary conditions for turbulent quantities in the inner layer are specified by following correlations given in Patel and Chen [70] while turbulent quantities in the outer layer is specified by Eq.(IV-6) and Eq.(IV-7).

$$k^{+} = 0.05 (y^{+})^{2}$$
 $y^{+} < 5 (VI-16)$ 
 $= 1.25 + 0.325 (y^{+} - 5)$ 
 $= 4.5 + (y^{+} - 15) / 37.5$ 
 $15 < y^{+} < 60$ 
 $= 3.3$ 
 $60 < y^{+} < 120$ 

and

$$\epsilon^{+} = 0.1 \text{ y}^{+} / 120$$
  $\text{y}^{+} < 12 \text{ (VII-17)}$ 

$$= 1 / \kappa \text{y}^{+}$$
  $\text{y}^{+} > 12$ 

The dimensionless quantities in these equations are defined as  $\mathbf{k}^+ = \mathbf{k} \ / \ \mathbf{u_T}^2$  ,  $\epsilon^+ = \epsilon \ / \ (\ \mathrm{Re}\ \mathbf{u_T}^4\ )$  ,  $\mathbf{y}^+ = \mathrm{Re}\ \mathbf{u_T}$  y and  $\mathbf{u}^+ = \mathbf{u}\ / \ \mathbf{u_T}$  .

The other boundary conditions are same as those reported in chapter II-3-2.

### VI.5 Results and Discussions

VI.5.1 Prediction of Turbulent Flow Past Axisymmetric Bodies using Wall Function Method

Calculations are performed for three different axisymmetric bodies of DTNSRDC, afterbody-1, afterbody-2 and afterbody-5. Both finite analytic method and finite volume method are used to solve Reynolds-averaged Navier-Stokes equations with the k - £ turbulence model and two-point wall function method. The same numerical grids and boundary conditions are employed for both calculations. The time marching technique is employed for finite analytic calculations with time step  $\Delta t = 1$  and pressure relaxation factor  $\alpha_p = 0.2$ . The relaxation factors used in the finite volume calculations are  $\alpha_u = \alpha_v = 0.7$ ,  $\alpha_k = \alpha_{\hat{\epsilon}} = 0.8$  and  $\alpha_p = 0.5$ .

Figure VI-2 shows the convergence history of both calculations for the afterbody-1. The calculation by finite volume method converges faster than that by finite analytic method in the earlier stage. However, the calculation by finite volume method has a limit in convergence. This limited convergence originates from use of one velocity staggered grid method which is also reported in Shyy et al. [24]. As will be shown in the

next chapter, use of two velocities staggered grid method eliminates this deficiency. The calculation by finite analytic method monotonically converges without a limit although the same one velocity staggered method is used. Satisfactory convergence, RES  $< 2 \times 10^{-3}$ , was obtained within 100 iterations for both calculations where RES denotes the sum of mass residuals in the pressure correction equation divided by the inlet flow rate. However, the pressure and velocity fields are settled down within 50 iterations as shown in Figs.VI-3 to VI-8. figures show that convergences of boundary layer and wake development by finite analytic method are a little faster than those by finite volume method. This is due to the fact that the relaxation factors in the finite volume method is same in the whole computational domain while relaxation factors in the finite analytic method are changed according to the size of numerical grid and the magnitude of convecting velocity components which is another novel nature of the finite analytic method.

Figs.VI-9 to VI-11 show the converged pressure  $\frac{2}{2}$  distributions,  $Cp = 2(p-p_{\infty})/(\rho U_{\infty})$ , on the body surface and along the wake centerline for afterbody-1, afterbody-2, and afterbody-5. As shown in the figures, the agreement between the predictions and measured data is excellent. The differences in the prediction by two

different methods are small and are confined to only the region of inlet, propellor hub and trailing edge. The dramatic change of pressure in the stern and propeller hub region is well predicted. The pressure is recovered in the wake at a distance roughly 0.3L from the trailing edge of the body. Since the solution domain of the present study extends far beyond this distance, the whole viscous-inviscid interaction is completely captured.

Figs.VI-12 to VI-14 show the comparision between predicted and measured friction velocity. Fairly good agreement between predictions and measurments was obtained in the stern region. The slight disagreement in the upstream region may due to the simple imposition of inlet conditions. The results can be improved if the accurate inlet conditions of velocity and turbulent quantities are provided by experimental data. The finite volume method consistently overpredicts the friction velocity in all calcultions. As shown in the figures, there is steep drop of friction velocity in the adverse pressure gradient region and the flow is very near to separate at x = 0.93L for afterbody-5, x = 0.97L for afterbody-2 but no flow separation is predicted.

Figs.VI-15 to VI-17 show the radial pressure distribution in the stern and near wake region.

Satisfactory agreements between the prediction and measurements are made although they are not as good as those of pressure distribution on the body surface. The small discrepancies may be partly due to the difficultities in the measurements. The differences in prediction between two methods are small and are again confined to the regions of propellor hub and trailing edge. We note that the viscous-inviscid interaction extends radially to 0.35L from the surface of the body near the trailing edge. This fact shows the failure of thin boundary layer approximation for the present problem and some careful considerations should be made for the selection of radial direction solution domain. In the present study, the computational domain extends radially to  $y_{11} \sim 1.1L$  as shown in Table 4.

Comparisions of the predictions with the measured data for both axial and radial velocity components is seen in Figs.VI-18 to VI-20. The agreements between measured data and the predictions by finite analytic method is excellent. The finite volume method slightly overpredicts the axial velocity component, especially near the tail region and in the near wake region. One may notice the thickening of boundary layer in the tail and in the near wake region which is consistent with the pressure variation in these regions.

The turbulent kinetic energy in the tail region and in the near wake region is overpredicted as shown in the Figs.VI-21 to VI-23. The amount of overprediction is more severe in the prediction of afterbody-5 and afterbody-2 than that in the afterbody-1. The differences in prediction by two methods are small and consistent with the predicted velocity profiles. It is noted that the predictions of turbulent kinetic energy made by Huang and Chang [99] agrees quite well with experimental data. They used a different near wall treatment instead of the wall function method. As will be shown in the next section, the use of two-layer model slightly improve the prediction. From these observations, the overprediction of turbulent kinetic energy in the tail and near wake regions seems to be originated from the inadequacy of k -  $\epsilon$ turbulence model in the prediction of fluid flow involving pressure gradient and streamline curvature effects. other predictions made by Patel and Chen [89], Muraoka [97,103] using the  $k - \varepsilon$  turbulence model and the wall function method show the similiar trend as in the present prediction.

Overall agreements between measurements and predictions made using both methods are encouraging. For most of the stern region and near wake region, the

pressure and velocity components are accurately predicted. But some considerations must be made on the selection of turbulence model especially on the near wall treatment in order to accuately predict the turbulent quantities for the flow involving pressure gradient and streamline curvature effects. Although predictions by finite analytic method are in favor for all the calculations, the differences in the predictions by two different numerical schemes are small. It shows that the selection of numerical scheme is not important for calculating of boundary layer type flow where the numerical false diffusion effects are very small. The overall success of present calculations are mainly due to the use of twopoint wall function method. However, the use of two-point wall function method is limited and can not be confidently applied to the flow involving separation. Calculations are also made using the partially parabolic form of finite analytic method although it is not presented here. differences in predictions between partially parabolic calculations and elliptic calculations were found to be negligible. This fact shows that partially parabolic assumption is a good approximation if there is no flow separation.

# VI.5.2 Prediction of Turbulent Flow Past Axisymmetric Bodies by Two-Layer Model

Calculations are performed for four different axisymmetric bodies of DTNSRDC, afterbody-1, afterbody-2, afterbody-3 and afterbody-5. The partially parabolic form of finite analytic method explained in chapter II-5-3 is employed to solve Reynolds-averaged Navier-Stokes equations with two-layer model. The FLARE approximation where the  $\xi$ -directional convecting velocity (  $D_h$  in Eq.(II-84) ) is zero if it is less than zero is employed in order to properly handle the flow separation ocurring during the iteration process. The introduction of FLARE scheme is come from the observation made by Ramakrishnan and Rubin [105]. They found that the FLARE scheme was the most stable for the calculation of small separated, high Reynolds number flow. The time marching technique is employed for iteration process with time step  $\Delta t = 0.002$ . Satisfactory convergence was obtained after 1000 time marching.

Figs.IV-24 to IV-27 show the converged pressure  $\frac{2}{2}$  distributions,  $Cp = 2(p-p_{\infty})/(\rho U_{\infty})$ , on the body surface and along the wake centerline. As shown in the figures, the agreements between the measured data and the predicted results are fairly good. The pressure is a little

sensitive to the shape of the body surface as compared with predictions using the wall function method. It is due to the fact that pressure is calculated all the way to the wall in the two-layer calculations while pressure on the body surface is extrapolated from the wall function region to the body surface using a simple linear function in the calculations using the wall function method. It is noted that the predictions for afterbody-3 are possible by use of the two-layer model.

Figs.IV-28 to VI-31 show the comparisions between the predicted and measured friction velocity. Athough fairly good agreements are made in the hull region, systematic overpredictions are made in the tail region. overprediction of friction velocity in the tail region may be partly due to the numerical difficulties in the generation of fine numerical grid near the wall in the tail region of the body and may be partly due to the fact that even the one equation turbulence model tends to overestimate the velocity in the near wall region indicating a reduction of turbulence length scale in the tail region. It is noted that flow separation was not predicted in the present calculation for afterbody-3 in which experimental data indicate there exist a small separation bubble around the inflection point. Figs.VI-32 to VI-33 show the predicted friction velocity for

afterbody-3 and afterbody-5 by Chen and Patel [56] using the same two-layer model and the nine-point finite analytic method. There exist substantial differences between two predictions. The origin of these differences can not be clearly explained since the details of pressure-velocity coupling technique are not reported in Chen and Patel [56]. However, the present predictions does not show the strange overshoots which is observed in the predictions by Chen and Patel [56].

Fairly good agreements between the predictions and the measured data were obtained for both the axial and radial velocity components which can be seen in Figs.VI-34 to VI-37 except the axial velocity component is slightly overpredicted in the tail region as explained before.

The overprediction of turbulent kinetic energy in the tail region and in the near wake region in the calculations using the wall function method is slightly improved by using the two-layer model as shown in the Figs.VI-38 to VI-40. This observation shows that the defect of the  $k-\epsilon$  turbulence model in the calculation of turbulent boundary layer and wake involving pressure gradient and curvature effects is a little relieved by the introduction of one equation turbulence model for the calculation of flow near the wall region.

Overall agreements between measurements and predictions made by the present finite analytic method with both wall function method and two-layer model are satisfactory. For most of the stern region and the near wake region, velocity components and turbulent quantities are accurately predicted except that the axial velocity component is overpredicted in the two-layer calculation in the tail region of body. The origin of this overprediction should be clearly investigated. found that the inlet condition severely influence the overall solution. Thus the proper ways of specifying the inlet condition should be sought. When it is considered the fact that the two-layer calculation not only provides the numerical solutions of laminar sublayer, buffer layer and a part of logarithmic layer without excessive numerical efforts but also the two-layer model can be applied to separated flow region to which the wall function method can not be confidently applied, the use of two-layer model is highly recommended.

#### CHAPTER VII

#### TURBULENT FLOW PAST FINITE AXISYMMETRIC BODIES

#### VII.1 Introduction

Incompressible turbulent flow past axisymmetric bodies of finite length has been the subject of numerous investigations, as it is of major importance in aerodynamics and hydrodynamics. In most of previous studies, the calculations start at the middle of body with inlet conditions provided by curve fits of experimental data [97], simple flat plate correlations [56,89] or numerical solutions of boundary layer equation up to the inlet location [103]. However, these calculations do not provide the solution of leading edge interaction and initial development of boundary layer near the leading edge. The resulting solutions are dependent on the inlet conditions as shown in the previous chapter or the location of inlet boundary [81].

In order to avoid above deficiencies in the half body calculations and to obtain the solution of the whole flow field, the calculation should start far upstream of the body with inlet conditions provided by unform flow

condition. However, numerical solutions of incompressible turbulent flow past axisymmetric bodies, including the leading edge interaction, boundary layer development on the body, the trailing edge interaction and the wake development, is rarely seen in the literature. For two dimensional flow situations, Rhie and Chow [16] obtained the numerical solutions of turbulent flow past airfoils with or without angle of attack using the  $k - \varepsilon$  turbulence model and the wall function method. The C-type, bodyfitted coordinates were introduced to handle the complex physical geometry and the SIMPLE numerical algorithm was employed with non-staggered grid arrangement. Detailed numerical solutions of laminar and turbulent flow past a cicular cylinder were obtained by Majumdar and Rodi [55]. They used an orthogonal coordinate system with staggered grid arrangement. The k -  $\epsilon$  turbulence model was also employed in this study. An improvement of prediction by using the zero equation turbulence model in the near wall region instead of the wall function method is reported.

Since the physical solution domain has a complex geometry which requires the use of nonorthogonal, body-fitted coordinate system, some considerations should be made about the choice of calculation methods in this coordinate system. Among the several calculations methods outlined in chapter I, the two velocities staggered grid

method developed by Maliska and Raithby [30] keeps the novel nature of staggered grid arrangement without any numerical problems encountered in the use of one velocity staggered grid method although the use of this grid configuration requires a little more computer storage and computing time by storing both velocity components at each control volume surface. It is reported in Maliska and Raithby [30] that the computational efforts using this two velocities staggered grid method is not so grave as it looks by its relatively earlier convergence. This grid configuration allows to use H-type grid as well as C-type grid to which the one velocity staggered grid method may not be applicable. Therefore the two velocities staggered grid method is employed for all the calculation presented in this chapter with some modifications made from the original method by Maliska and Raithby [30].

In the initial phase of present study, some computational experiments were made using the finite analytic method and the two-point wall function method outlined in the previous chapter. However, this practice was abandoned since the two-point wall function method did not properly describe the laminar flow near the leading edge even in the simple flat plate calculation. It was also found that the general law of the wall, Eq.(VI-8), had singularity in the region of favorable pressure

gradient giving a negative argument in the logarithmic function. Although this two-point wall function method has a salient feature of removing the sensitivity of the first grid location on the solution, the application of this method to general flow situation is limited. After testing other possibilities, it was decided to use the same numerical scheme and the near wall treatment as those reported in Rhie and Chow [16] or Majumdar and Rodi [55]. These authors used the finite volume method and the Couette flow type wall function method by Launder and Spalding [43]. However, the numerical solutions using this wall function method usually suffer the sensitivity of the solution on the numerical grid and the overprediction of the axial velocity component in the adverse pressure gradient region due to the neglection of the pressure gradient effect in the wall function.

In the present study, numerical solutions of incompressible turbulent flow past axisymmetric bodies are obtained using the  $k-\epsilon$  turbulence model and the wall function method. The complex, physical solution domain is resolved by the use of numerically generated, nonorthogonal, body-fitted coordinates. The governing equations are written in the transformed domain with the cylindrical veolcity components as the dependent variables. The transformed governing equations are

discretized using the finite volume method with hybrid numerical scheme as outlined in chapter II-6. As mentioned before, the two velocities staggered grid method is adopted and the derivation of pressure and pressure correction equations in this grid configuration is given in chapter III-3-2.

Calculation are performed for four axisymmetric bodies of DTNSRDC using the calculation procedure outlined in chapter III-4. The numerical results are compared with the experimental data.

#### VII.2. Numerical Grids and Solution Domains

In the initial phase of present study, use of C-type numerical grid was seriously considered due to the roundness of forebody shape. The introduction of two velocity staggered grid method should be understood within this context since the use of one velocity staggered grid method in C-type grid may cause numerical instability. However, the use of C-type grid was abandoned due to the difficulties in the specification of boundary conditions. The numerical difficulties related with the use of C-type grid are well reported in Rhie [83] and Chen and Patel [106]. For example, Chen and Patel [106] first performed calculation using H-type grid. Then the boundary

conditions for calculation by C-type grid are specified by these calculated results. In order to avoid these difficulties, it was decided to change the forebody shape up to  $\mathbf{x_i} = 0.3L$  and to use H-type grid. The forebody shape was changed to orgive shape using following simple equations;

$$R = R_{\text{max}} - R_{i} + (R_{i}^{2} - (x - x_{i})^{2})^{1/2}$$
 (VII-1)

where  $\mathbf{R}_{\text{max}}$  is the maximum radius of body and  $\mathbf{R}_{\text{i}}$  is defined as following relation.

$$R_i = (R_{max}^2 + x_i^2) / (2 R_{max})$$
 (VII-2)

As will be seen later, the change of forebody shape does not seriously influence the develoment of boundary layer in the region of middle body and tail since these DTNSRDC bodies have long parallel middle bodies.

The numerical grids are generated using the method outlined in chapter II-4-2. The partial view of generated numerical grids are shown in Fig.II-5. The x-directional numerical grids on the body are distributed uniformly while those in the upstream of body and in the wake region are stretched with expansion ratio 1.2 ~ 1.3. Table 6 shows the detailed information on the flow condition, grid and solution domains used in the present calculation. These solution domains are large enough to capture the

whole leading and trailing edge interactions. Of the 151 x-directional numerical nodes, 20 nodes are placed upstream of body, 101 nodes are placed on the body and the rest 30 nodes are placed in the wake.

#### VII.3 Boundary conditions

The inlet boundary conditions are specified by following uniform flow conditions.

$$u = 1$$
,  $v_x = 0$ ,  $k = k_{in}$ ,  $\varepsilon = \varepsilon_{in}$  (VII-3)

where  $\mathbf{k}_{\text{in}}$  and  $\boldsymbol{\epsilon}_{\text{in}}$  is specified as follows

$$k_{in} = 1.5 (Tu)^2$$
 (VII-4)

$$\varepsilon_{\rm in} = c_{\mu} k_{\rm in}^{3/2} / l_{\rm in}$$
 (VII-5)

and the turbulent intensity, Tu = 0.5% and length scale,  $l_{in} = 0.001L$  are used in the present calculations.

In the wall function region, the wall function approach of Launder and Spalding [43] is used. It is based on the one-dimensional Couette flow analysis. The wall shear stress,  $\tilde{\tau}_w$  is expressed as a function of the second nodal velocity component parallel to the wall,  $\tilde{\mathbf{U}}_p$  as follows;

$$\tilde{\tau}_{w} = -\lambda_{w} \tilde{U}_{p}$$
 (VII-6)

where the coefficient,  $\lambda_{_{\mathbf{W}}}$  is determined from the two-part universal velocity profile.

$$\lambda_{w} = \mu / \delta n$$
 if  $y_{p}^{+} < 11.63$  (VII-7)

$$\lambda_{w} = \rho c_{\mu}^{1/4} k_{p}^{1/2} \kappa / \ln(E y_{p}^{+}) \text{ if } y_{p}^{+} > 11.63 \text{ (VII-8)}$$

In these equations,  $\kappa$  = 0.418 is the von-karman constant and E = 0.9793 is the roughness parameter,  $\delta$ n is the normal distance from the wall and  $y_p^+$  is defined as follows;

$$y_p^+ = \rho c_\mu^{1/4} k_p^{1/2} \delta_n / \mu$$
 (VII-9)

Since the dependent variables of momentum equations are cylindrical velocity components, the shear force,  $\tilde{T}_w = A_w \tilde{\tau}_w$  should be expressed in terms of its cylindrical components. The shear force,  $\tilde{T}_w$  acting along  $\tilde{U}_p$  direction is decomposed into two components  $T_{wx}$  and  $T_{wy}$  along x and y directions repectively as follows;

$$T_{wx} = -\lambda_w A_w [ (1 - n1 n1) u_p - n1 n2 v_p ] (VII-10)$$

$$T_{wy} = -\lambda_w A_w [ (1 - n2 n2) v_p - n1 n2 u_p ] (VII-11)$$

where n1 and n2 are the components of the unit vector normal to the wall along the x and y directions repectively.

$$n1 = - \left( y_{\xi} / \sqrt{\gamma} \right)_{w} \tag{VII-12}$$

$$n2 = (x_{\xi} / \sqrt{\gamma})_{w} \qquad (VII-13)$$

and the geometric coefficient  $\gamma = x_{\xi}^2 + y_{\xi}^2$ .

The equations for turbulent kinetic energy, k and its dissipation rate,  $\epsilon$  also need a special treatment for the near wall cell. In the equations for k, the diffusion flux through the wall surface is set equal to zero while the source terms are modified as follows.

The generation and dissipation term of turbulent kinetic energy equation is approximated as follows using the Couette flow assumption;

$$\int_{\Delta V} G dV \cong |\tilde{\tau}_{w}| |\tilde{U}_{p}| \Delta V / \delta n \qquad (VII-14)$$

$$\int_{\Lambda V} \epsilon \, dV \cong c_{\mu}^{3/4} k_{p}^{3/2} U_{p}^{+} \Delta V / \delta n \qquad (VII-15)$$

where  $U_p^+$  is given by

$$U_p^+ = y_p^+$$
 if  $y_p^+ < 11.63$  (VII-16)

$$U_p^+ = \frac{1}{\kappa} \ln(E y_p^+)$$
 if  $y_p^+ > 11.63$  (VII-17)

The value of  $\varepsilon$  in the near wall cell is obtained from the local value of k using the concept of local equilibrium between production and dissipation of turbulent kinetic energy as follows;

$$\varepsilon_{\rm p} = c_{\rm \mu}^{3/4} k_{\rm p}^{3/2} / (\kappa \delta n) \qquad (VII-18)$$

Since the details of this wall function method is well-documented in Launder and Spalding [43] or Peric [18], only a brief description of this method is given in the present study.

The other boundary conditions are same as those reported in chapter II-3 and not explained here.

## VII.4 Results and Discussions

Calculations are performed for four axisymmetric bodies using the finite volume method outlined in chapter II-6. The relaxation factors used in the present calculations are  $\alpha_u = \alpha_v = 0.7$ ,  $\alpha_k = \alpha_\epsilon = 0.8$  and  $\alpha_p = 0.5$ .

Fig.VII-1 shows the convergence history of calculations for afterbody-1. The total mass residual decreases rapidly for the first fifty iterations. However, the rate of convergence slows down after fifty iterations. It is also noted that the calculation using the coarse grid gives a faster convergence. Satisfactory convergence, RES  $< 2 \times 10^{-4}$ , was obtained within 300 iterations although computations are continued to 500 iterations where RES denotes sum of mass residuals in the

pressure correction equation divided by inlet flow rate. In general, the velocity components and pressure field were settled down within 100 iterations and the rest computational efforts are devoted to the development of far wake.

Figs.VII-2 and VII-3 show the grid dependence tests for pressure and friction velocity. They show that present calculations are generally grid independent except for a small region near the leading and trailing edges. It should be noted that the first three y-directional computational grids near the wall were fixed for both calculations to avoid errors caused by the near wall treatment.

Figs.VII-4 to VII-7 show the converged pressure  $\frac{2}{2}$  distributions,  $Cp = 2(p-p_{\infty})/(\rho U_{\infty})$ , on the body surface and along the wake centerline for four different afterbodies. The leading and trailing edge interactions as well as the dramatic change of pressure in the regions of stern and propellor hub are well predicted. The agreement between the predictions and measured data is also fairly good except pressure is overpredicted in the tail region of afterbody-3. This overprediction is the result of the inadequacy of the present  $k-\epsilon$  turbulence model with the present wall function method for describing the flow field

in this region. It is noted that although the magnitude of leading edge interaction is large, the interacting zone is confined to a small region. The pressure is recovered in the wake in a distance roughly 0.3L from the trailing edge of the body. Since the solution domain of the present study extends far beyond this distance, the whole viscous-inviscid interaction is completely captured.

Figs.VII-8 to VII-11 show the predicted friction velocity distribution with comparision with measured data. There exist a strange transition near the leading edge which is originated from inproper modelling of transition by present  $k - \varepsilon$  turbulence model. The friction velocity is underpredicted in the region of middle body in spite of velocity components in this region are somewhat well predicted as will be shown in the next figures. As well explained in chapter V, the origin of this discrepancy is come from the usage of the wall function method in the fact that although the first normal calculation point is placed in the buffer layer ( $y^+ \sim 20$ ), the friction velocity is calculated by the logarithmic law. increase of the size of the first grid would improve the prediction of friction velocity. However, this practice was abandoned due to the very poor overall predictions especially in tail region of the body. From these observations, it is suggested that the wall function

region should be at least divided into three regions, laminar sublayer, buffer layer and logarithmic layer as reported in Lee [107]. The use of more elaborated wall functions by Launder and Chieng [108] will also improve the predictions. However, these practices are not performed in the present investigation. A subtantial overprediction of friction velocity is observed in the tail region of body, especially in the predictions for afterbody-3 and afterbody-5. These overprediction is due to the neglection of pressure gradient effect both in the turbulence model and in the wall functions. However, as mentioned before, the use of general law of the wall, Eq. (VI-8), leads to singularity in the region of favorable pressure gradient. It is noted that flow separation is not predicted for afterbody-3 although experimental data indicate that there exist a small separation bubble around the inflection point. It is believed that the use of more advanced turbulence model, for example the two-layer turbulence model, will remove all the defeciencies arised from using wall function method.

Comparisions of the predictions with the measured data for both axial and radial velocity components are shown in Figs.VII-12 to VII-15. The agreements between measured data and the predictions are fairly good except the velocity components are a little overpredicted in the

tail region and in the near wake region due to the neglection of pressure gradient effect in the turbulence model and in the wall functions. However, the thickening of boundary layer in the tail and in the near wake region is well predicted. It is noted that as shown in these figures, the change of forebody shape does not seriously influence the boundary layer development in the region of middle body, thereby, that in the stern and wake region.

As shown in Fig.VII-16 to VII-18, the predictions of turbulent kinetic energy agree fairly well with experimental measurements. However, when the overprediction of velocity components in the regions of tail and near wake is considered, the agreements of predictions with experimental data are not improved results over the predictions presented in the chapter VI. If the velocity components are accurately predicted, it is anticipated that the turbulent kinetic energy in the regions of tail and near wake will be overpredicted.

Overall agreements between measurements and predictions made by the present numerical method are encouraging. For the most of body and near wake region, the pressure and velocity components are fairly well predicted. However, some considerations must be made on the selection of turbulence model especially on the the

near wall treatment in order to accuately predict the turbulent quantities for the flow involving pressure gradient and streamline curvature effects. The use of more elaborated wall functions or introduction of more advanced turbulence model is indeed needed to properly simulate the flow field in these situations. improvements on turbulence model are remained for future study and are not pursued further in the present study. However, the present calculation method provides the predictions of whole turbulent flow field past axisymmetric bodies which are not yet reported in the literature. The present calculations also gives an example of the successful use of two velocity staggered grid method in the calculation of fluid flow in complex geometry which has not been reported in the literature since the original works of Maliska and Raithby [30].

#### CHAPTER VIII

#### CONCLUSIONS AND RECOMMENDATIONS

A numerical study of laminar and turbulent flow past finite two dimensional and axisymmetric bodies is presented. The available calculation methods for incompressible flow in a complex geometry, grid generation techniques and turbulence models are discussed. The numerical formulations and grid generation techniques and solution procedures employed in the present study are presented. Calculations are performed for laminar and turbulent flow past a thin flat plate, turbulent flow past axisymmetric bodies with changing body shapes, solution domains, turbulence models and numerical methods. Major contributions and findings of present study may be summarized as follows;

- (1) Wake function method for the prediction of turbulent flow past a flat plate is developed. An accurate prediction of wake flow past a flat plate is made without the detailed calculations of the near wall region and the laminar wake region.
- (2) Numerical solutions of a complete flow field past a finite flat plate and axisymmetric bodies which

include the leading edge interaction, the boundary layer development on the body, the traling edge interaction and the wake development, are obtained. The influence of inlet boundary conditions and the location of inlet solution boundary on the solution which is observed in the half body calculations is removed in the full body calculation. It is observed that the magnitude of the leading edge interaction is large, but the interacting zone is confined to a relatively small region. It is also found that the partially parabolic form of Navier-Stokes equations is not appropriate for the simulation of the strong leading edge interaction although it is suitable for the simulation of the boundary layer on the body, the trailing edge interaction and the wake development.

(3) Comparisions of predictions by the finite analytic method and by the finite volume method are made. Although the finite analytic method gives better convergence histories and more accurate predictions, the differences are found to be quantitatively very small. Both methods well predict the important features of flow field. It is observed that the finite volume method always slightly overpredicts the velocity components on the boundary layer as well as in the wake region.

- (4) It is found that use of one velocity staggered grid method with finite volume method gives a limit in convergence. The introduction of two velocities staggered method removes this deficiency. However, the two velocity staggered grid method requires more storage, more computing time and complicated programing.
- The defect of the  $k \varepsilon$  turbulence model with the Couette flow type wall function method for the prediction of transition of laminar flow to turbulent flow, turbulent boundary layer involving pressure gradient and streamline curvature effects is addressed. A strange transition near the leading edge was predicted and the velocity components are overpredicted in the adverse pressure gradient boundary layer region. As compared with the Couette flow type wall function method, the two-point wall function method well predicts the velocity components in the adverse pressure gradient boundary layer region by use of the general law of the wall in which the pressure gradient effect on the flow in the wall region are taken into consideration. However, the use of the general law of the wall is limited and can not be confidently applied to the laminar flow region near the leading edge and the favorable pressure gradient region. It is observed that the turbulent kinetic energy are overpredicted in the tail

region of axisymmetric bodies. This fact shows the the defect k -  $\epsilon$  turbulence model in the simulation of flow field involving pressure gradient and streamline curvature effects.

of two-layer turbulence model are observed. The predictions by the two-layer model not only provide the numerical solutions of viscous-affected near wall region without excessive computational efforts, but also the two-layer model can be applied to separated flow region where the wall function method can not be confidently applied. The use of two-layer model is highly recommended. However, it is found that the two-layer model slightly overpredicts the velocity components in the tail region of axisymmetric bodies.

Although present calculation methods are successfully applied to the simulation of various flow situations, there exist much rooms for further investigations which may be summarized as follows;

(1) The one velocity staggered grid method used in chapter VI has limitations in the general applications. The two velocities staggered grid method employed in the chapter VII removes the difficulties encountered in the use of one velocity staggered method. However, this

method requires a complicated programing, more storages and a more computing time. An introduction of newly developed calculation methods like algebraic manipulation method by Karki and Patankar [36] or the momentum interpolation method by Majumdar [19] will be alternative choices for removing these deficiencies. The introduction of these methods are straightfoward. The use of multigrid method will improve the convergence.

- (2) The origin of overprediction of velocity components in the tail region of axisymmetric bodies in the two-layer calculations should be clearly investigated in order to confidently apply this turbulence model to general flow situations.
- (3) The introduction of more advanced turbulence model, or at least more elaborated wall functions is needed for the proper prediction of complete turbulent flows past two dimensional or axisymmetric bodies. The use of two-layer model in this purpose may be an appropriate choice although it is questionable whether this model may properly simulate the transition of laminar flow to turbulent flow.
- (4) The present calculation methods can be easily applied to three dimensional situations with minor modifications.

Table 1. Definition of Variables

ф	$\Gamma_{\!oldsymbol{\phi}}$	S <sub><b>\phi</b></sub>
u	μ + μ <sub>t</sub>	$-\frac{\partial p}{\partial x} + \frac{\partial}{\partial x}(\mu_{ef}\frac{\partial u}{\partial x}) + \frac{1}{r}\frac{\partial}{\partial y}(r\mu_{ef}\frac{\partial v}{\partial y}) - \frac{2\partial k}{3\partial x}$

$$\mathbf{v} \qquad \mu + \mu_{\mathsf{t}} - \frac{\partial p}{\partial y} + \frac{\partial}{\partial \mathbf{x}} (\mu_{\mathsf{ef}} \frac{\partial \mathbf{u}}{\partial y}) + \frac{1}{\mathsf{r} \partial y} (\mathsf{r} \mu_{\mathsf{ef}} \frac{\partial \mathbf{v}}{\partial y}) - 2 \mathtt{a}_{\mathsf{C}} \mu_{\mathsf{ef}} \frac{\mathtt{v}}{\mathsf{r} 2} - \frac{2 \partial \mathtt{k}}{3 \partial y}$$

$$k \mu + \frac{\mu_t}{\sigma_k}$$
  $G - \rho \epsilon$ 

$$\varepsilon = \mu + \frac{\mu_t}{\sigma_e}$$
 $c_{\varepsilon 1}G \frac{\varepsilon}{k} - \rho c_{\varepsilon 2} \frac{\varepsilon^2}{k}$ 

$$G = \mu_{ef} \left[ 2 \left( \frac{\partial u}{\partial x} \right)^2 + 2 \left( \frac{\partial v}{\partial y} \right)^2 + 2 a_{c} \left( \frac{v}{r} \right)^2 + \left( \frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right)^2 \right]$$

$$\mu_{\text{ef}} = \mu + \mu_{\text{t}}$$
,  $\mu_{\text{t}} = c_{\mu} \rho \frac{k^2}{\epsilon}$ 

$$c_{\mu} = \text{0.09, } \sigma_{k} = \text{1.0, } \sigma_{\epsilon} = \text{1.3, } c_{\epsilon 1} = \text{1.44, } c_{\epsilon 2} = \text{1.92.}$$

 $a_{\rm C}$  = 0, r = 1 for Cartesian coordinate system.

 $a_{C} = 1$ , y = r for cylindrical coordinate system.

Table 2. Solution Domains for Calculations in Chapter-IV

Type of Flow	ı Re	Grid	x <sub>i</sub>	x <sub>d</sub> <sup>a</sup>	Y <sub>u</sub> a
Turbulent	2.48×10 <sup>6</sup>	57x31	-0.6	8.57	1.0

Re = Reynolds number based on the free stream velocity and body length.

 $X_i$  = location of upstream boundary.

 $X_d$  = location of downstream boundary.

 $Y_u$  = location of upper boundary.

<sup>a</sup>The origin of coordinate system is located at the trailing edge of plate.

Table 3. Solution Domains for Calculations in Chapter-Va

Type of Flow	Re	Grid	$x_{i}$	$x_d$	Yu
Laminar	105	135x35	-1.25	14.6	12.7
Turbulent	2.48x106	120x41	-1.15	12.3	3.9

aVariables defined in Table 2 and text.

Table 4. Solution Domains for Calculations in Chapter-VI $^{a}$  ( Wall Function Method )

Type of Body	Re	Grid	xi	x <sub>d</sub>	Yu
Afterbody-1	6.6x10 <sup>6</sup>	96x35	0.5	10.9	1.60
Afterbody-2	6.8x10 <sup>6</sup>	96x35	0.6	10.9	1.55
Afterbody-5	9.3x10 <sup>6</sup>	96x35	0.6	10.9	1.15

aVariables defined in Table 2 and text.

Table 5. Solution Domains for Calculations in Chapter-VI<sup>a</sup> ( Two Layer Model )

Type of Body	Re	Grid	$x_{i}$	$\mathbf{x}_{d}$	Yu
Afterbody-1	6.6x10 <sup>6</sup>	85x53	0.5	6.75	3.64
Afterbody-2	6.8x10 <sup>6</sup>	85×53	0.6	5.60	3.71
Afterbody-3	6.0x10 <sup>6</sup>	90x53	0.6	12.4	4.20
Afterbody-5	9.3x10 <sup>6</sup>	85x53	0.6	5.60	2.73

aVariables defined in Table 2 and text.

Table 6. Solution Domains for Calculations in Chapter-VII<sup>a</sup>

Type of Body	Re	Grid	xi	x <sub>d</sub>	Yu
Afterbody-1	6.6x10 <sup>6</sup>	151x36	-2.23	9.29	1.77
Afterbody-2	6.8x10 <sup>6</sup>	151x36	-2.23	9.29	1.80
Afterbody-3	6.0x10 <sup>6</sup>	151×36	-2.23	9.29	2.04
Afterbody-5	9.3x10 <sup>6</sup>	151x36	-2.23	9.29	1.33

<sup>&</sup>lt;sup>a</sup>Variables defined in Table 2 and text.

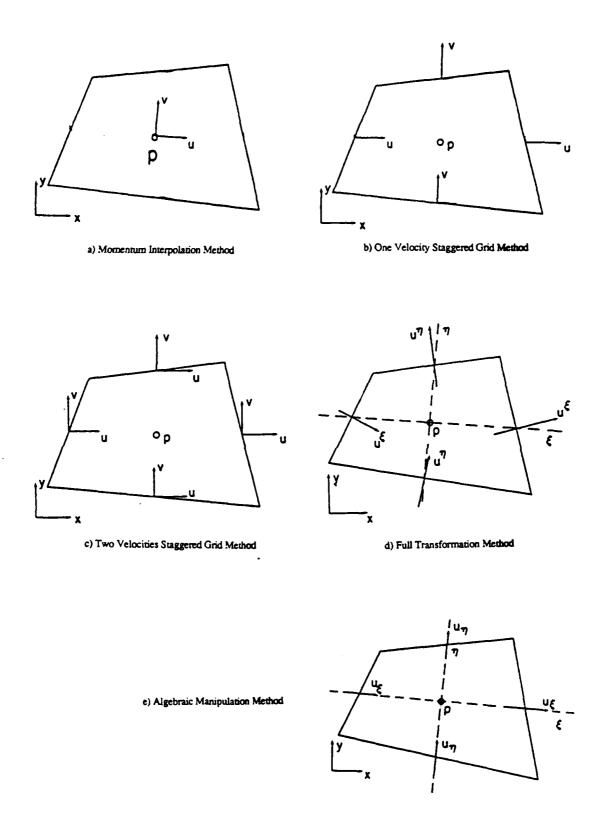
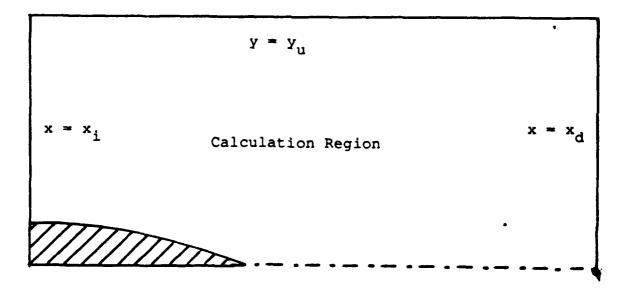


Fig.I-1. Grid Configurations.

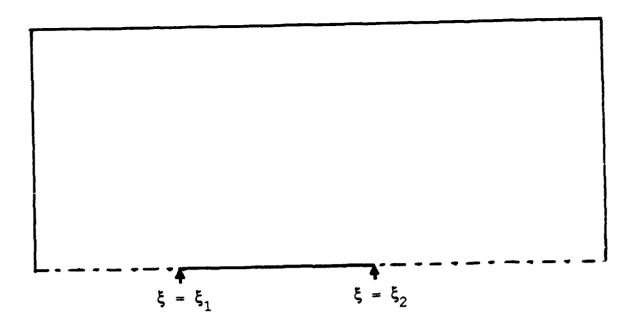
$$y = y_u$$
 $x = x_i$  Calculation Region  $x = x_d$ 

a) Full Body Calculation

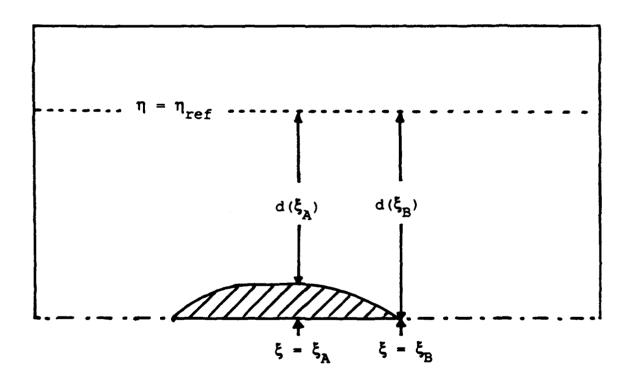


b) Half Body Calculation

Fig.II-1. Solution Domains.

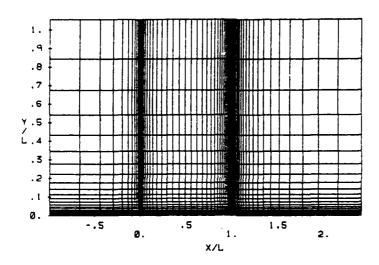


a) Flat Plate

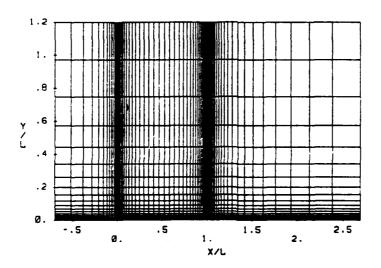


b) Axisymmetric Body

Fig.II-2. Notations for Grid Generation.

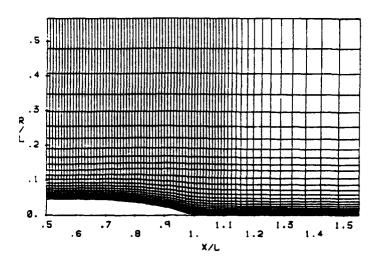


a) Laminar Flow.

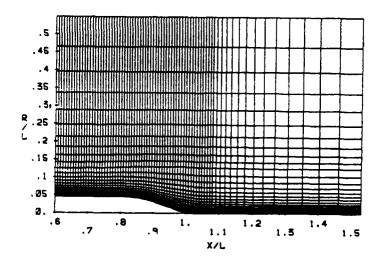


b) Turbulent Flow.

Fig.II-3. Numerical Grids for A Flat Plate.

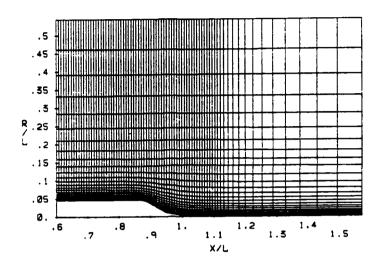


a) Afterbody-1

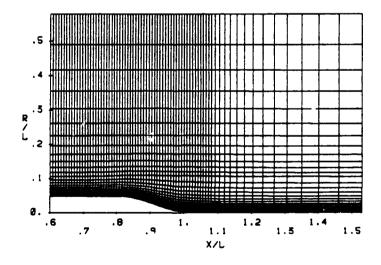


b) Afterbody-2

Fig.II-4. Numerical Grids for Axisymmetric Bodies ( Half Body Calculation )

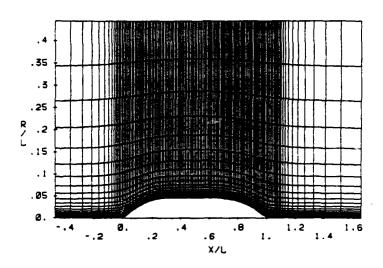


## c) Afterbody-3

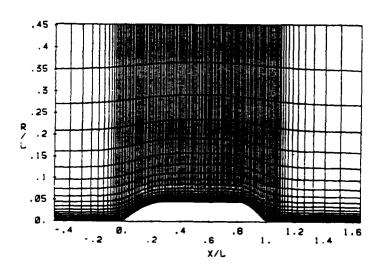


## d) Afterbody-5

Fig.II-4. Numerical Grids for Axisymmetric Bodies ( Half Body Calculation )

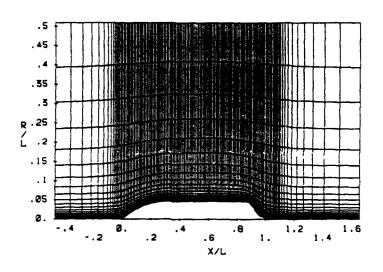


a) Afterbody-1

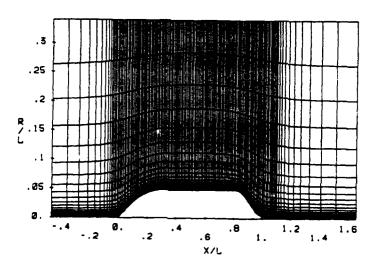


b) Afterbody-2

Fig.II-5. Numerical Grids for Axisymmetric Bodies (Full Body Calculation)



c) Afterbody-3



d) Afterbody-5

Fig.II-5. Numerical Grids for Axisymmetric Bodies (Full Body Calculation)

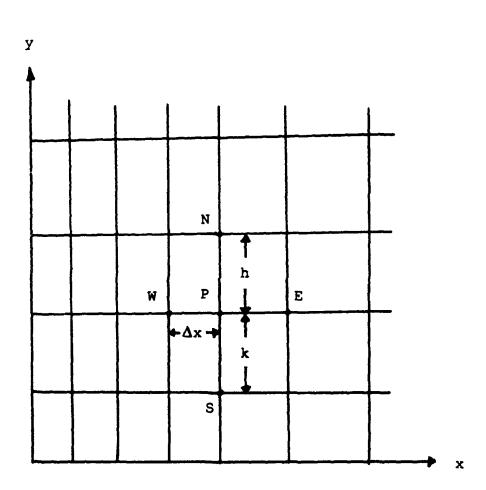
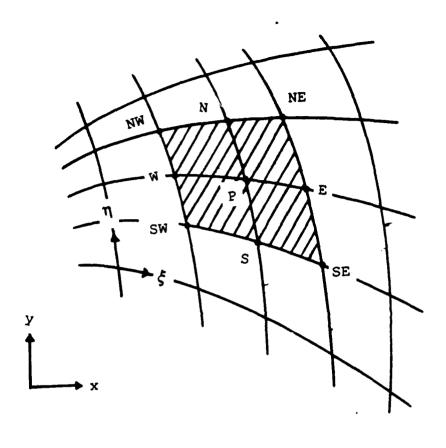


Fig.II-6. A Local Element for Finite Analytic Method in Catesian Coordinate System



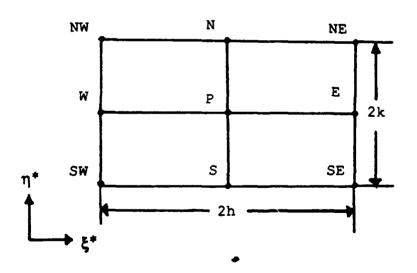


Fig.II-7. A Local Element for Finite Analytic Method in Boundary-Fitted Coordinate System

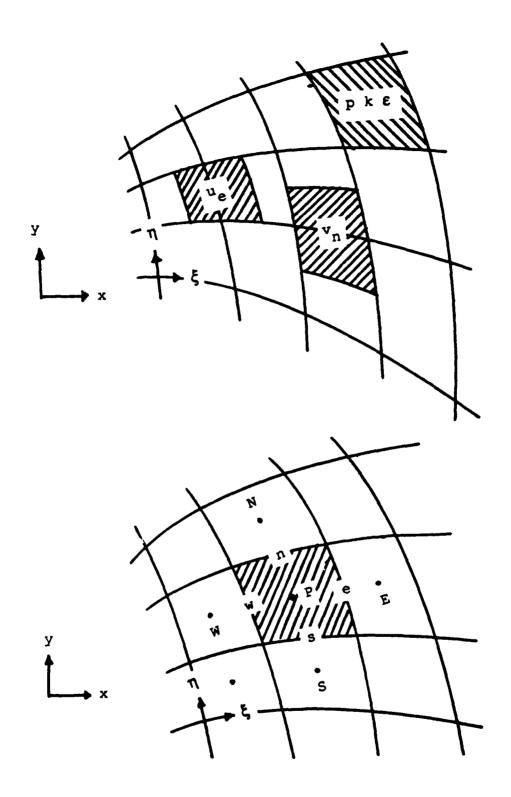


Fig.II-8. A Local Element for Finite Volume Method in Boundary-Fitted Coordinate System

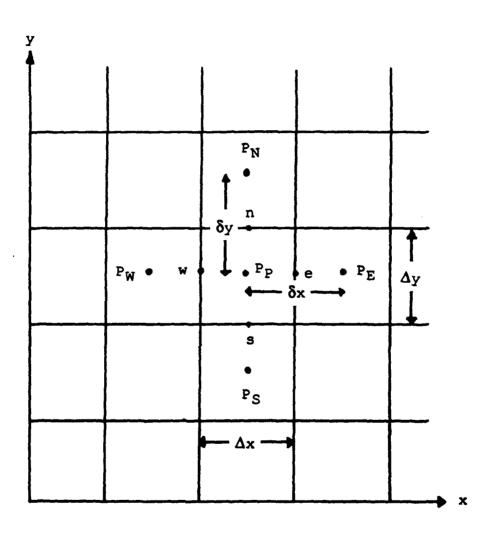


Fig.III-1. Control Volume for Pressure Variable in Cartesian Coordinate System

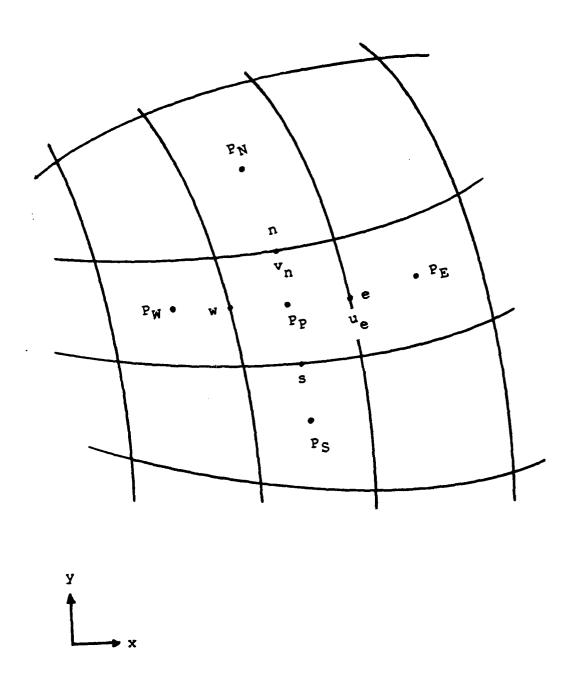


Fig.III-2. One Velocity Staggered Grid System.

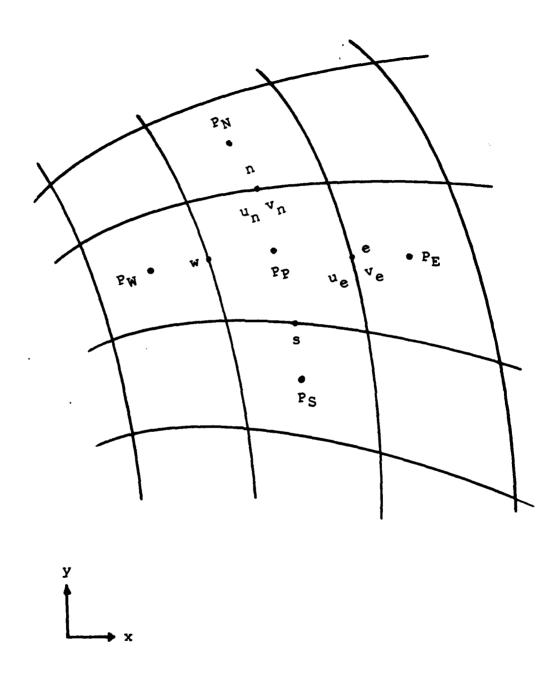


Fig.III-3. Two Velocities Staggered Grid System.

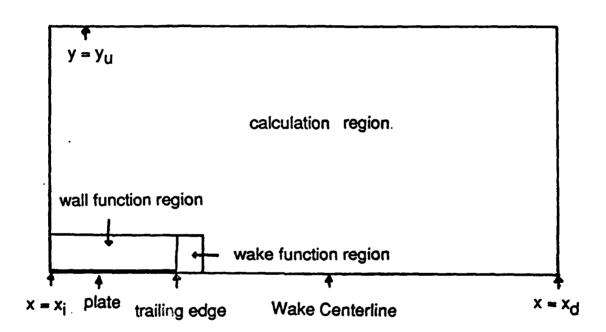


Fig. IV-1. Computational Domain.

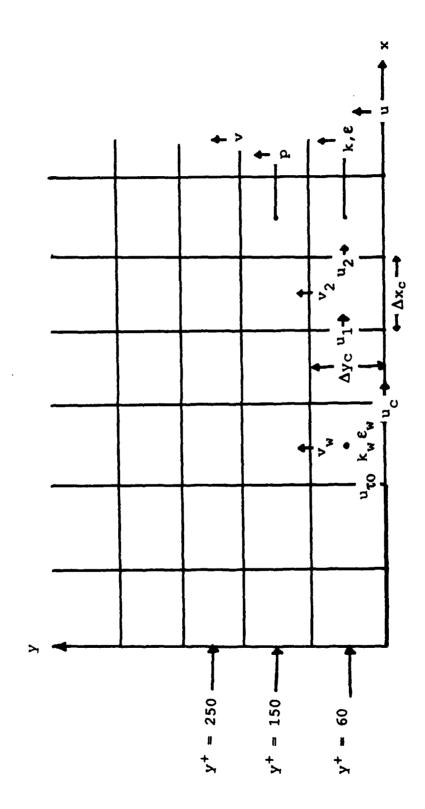


Fig.IV-2. Notation for Wake Function Method.

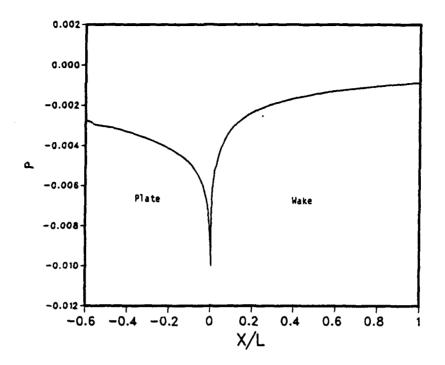


Fig.IV-3. Pressure Distribution on the Plate and along the Wake Centerline (  $y^+ \sim 150$  )

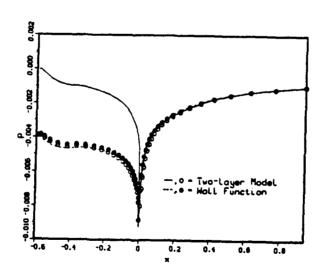


Fig. IV-4. Pressure Distribution Given in Ref. [70]

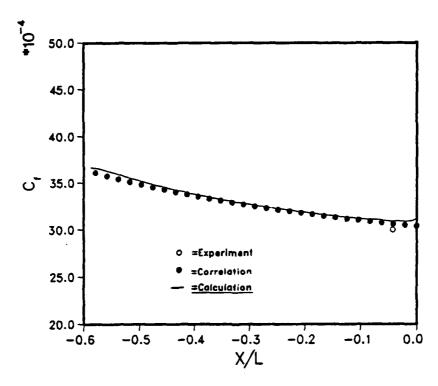


Fig. IV-5. Skin Friction Coefficient

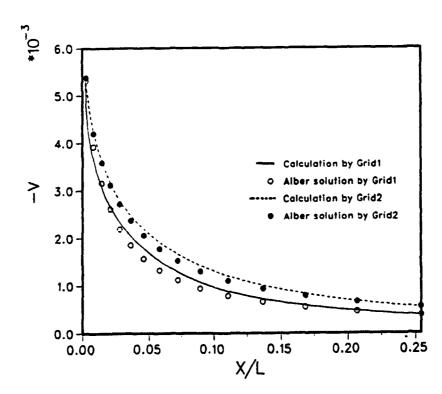


Fig.IV-11. Near-Wake Normal Velocity Distributions

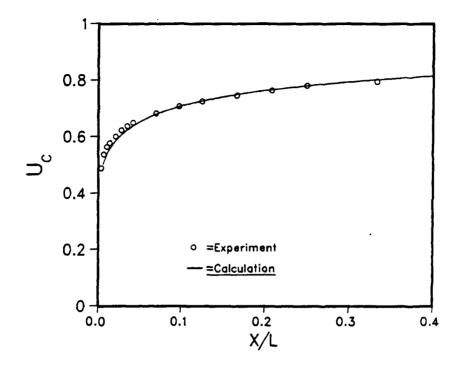


Fig. IV-6. Wake Centerline Velocity Distribution

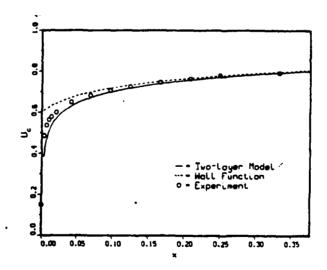


Fig.IV-7. Wake Centerline Velocity Distribution Given in Ref.[70]

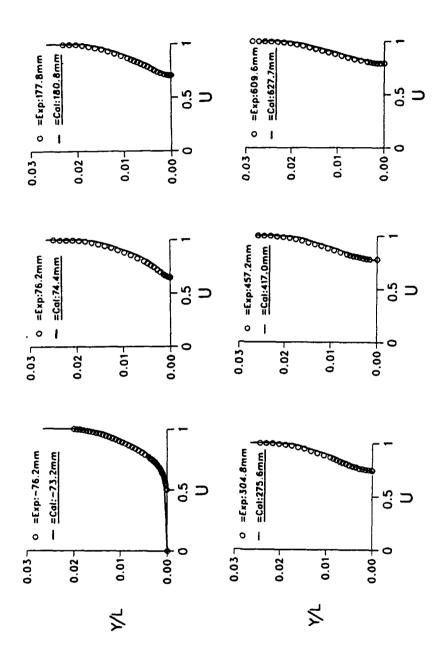


Fig. IV-8. Velocity Profiles in the Near wake

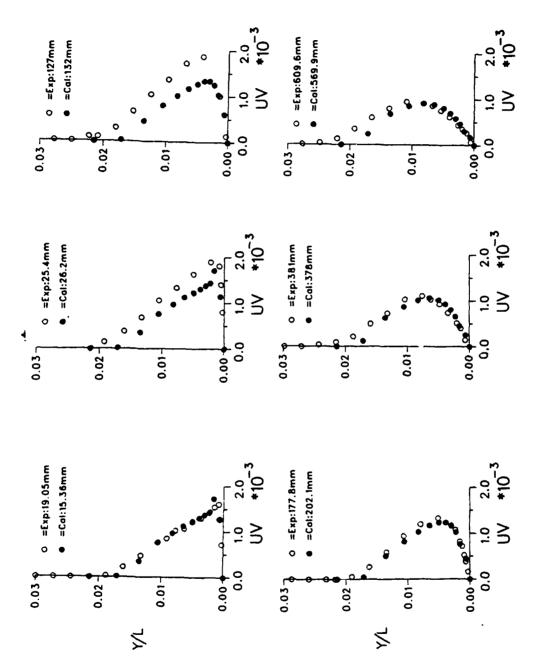


Fig.IV-9. Reynolds Shear Stress Distributions in the Near Wake

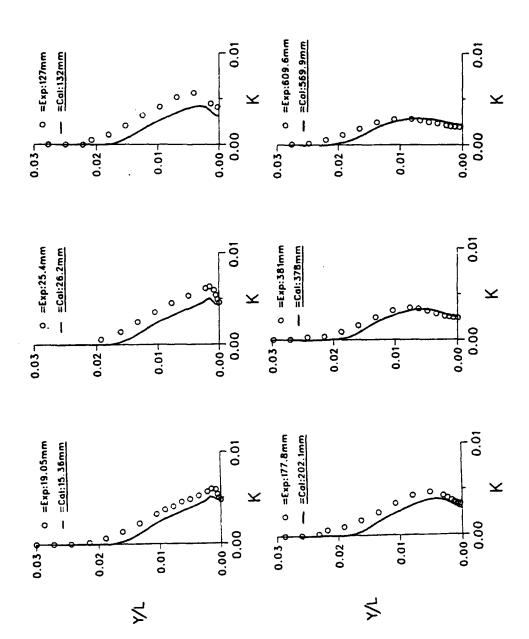


Fig.IV-10. Turbulent Kinetic Energy Distributions in the Near Wake

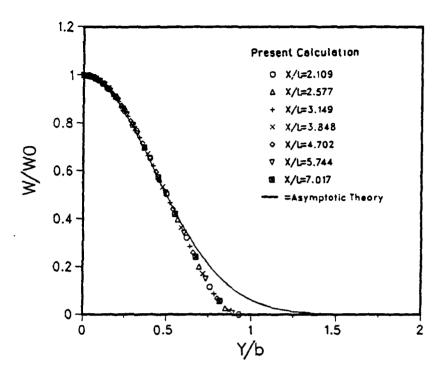


Fig. IV-12. Far-Wake Velocity Defect Profiles

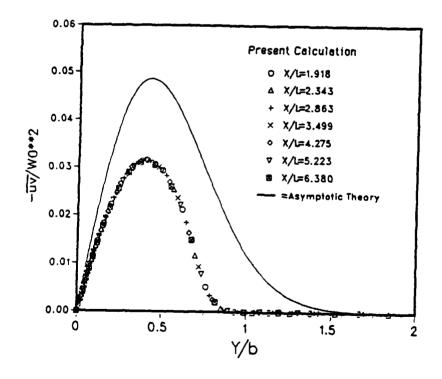


Fig. IV-13. Far-Wake Reynolds Shear Stress Profiles

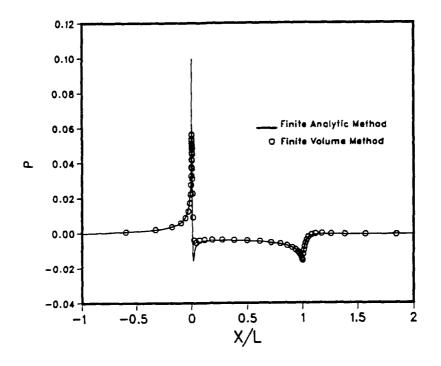


Fig.V-1. Pressure Distribution ( Laminar Flow )

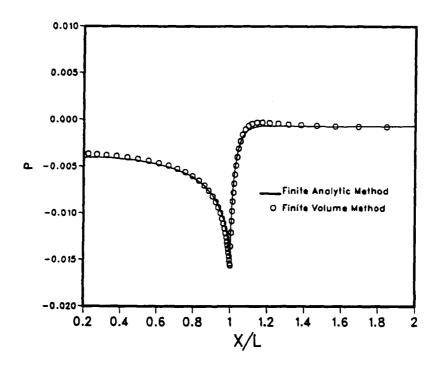


Fig.V-2. Pressure Distribution near the Trailing Edge (Laminar Flow)

•

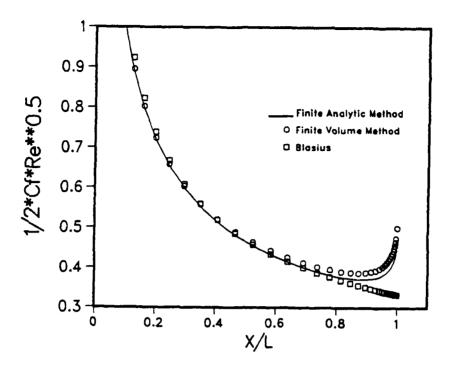


Fig.V-3. Skin Friction Coefficient (Laminar Flow)

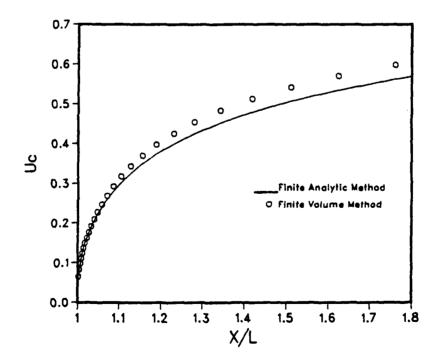


Fig.V-4. Wake Centerline Velocity Distribution ( Laminar Flow )

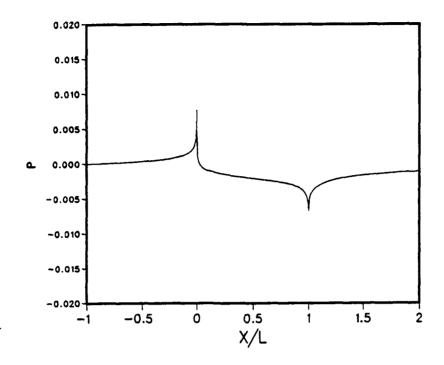


Fig.V-5. Pressure Distribution ( Turbulent Flow )

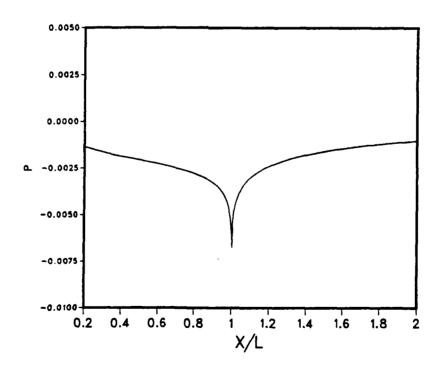


Fig.V-6. Pressure Distribution near the Trailing Edge ( Turbulent Flow )

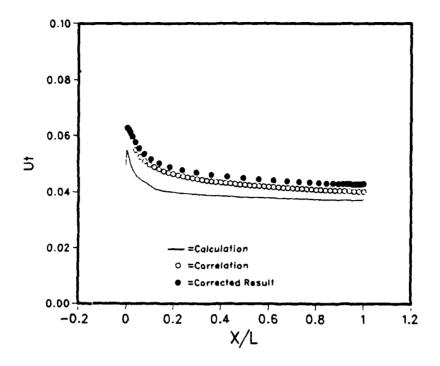


Fig.V-7. Friction Velocity Distribution (Turbulent Flow)

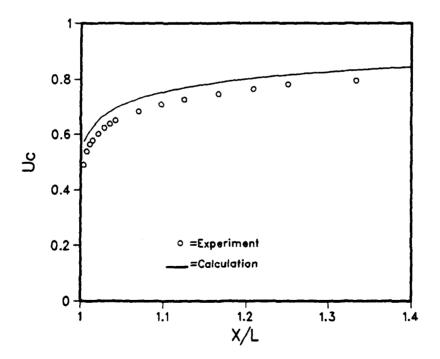


Fig.V-8. Wake Centerline Velocity Distribution (Turbulent Flow)

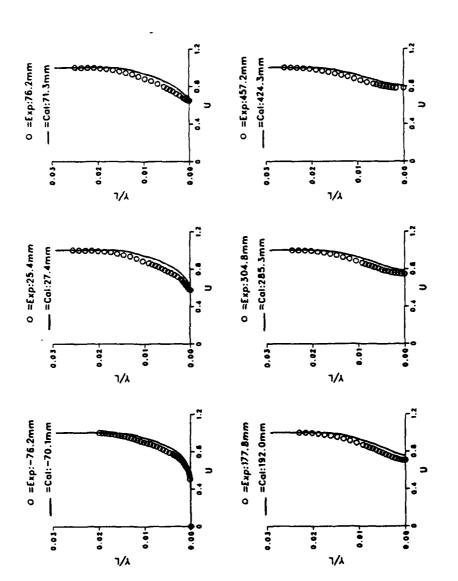


Fig. V-9. Velocity Profiles (Turbulent Flow)

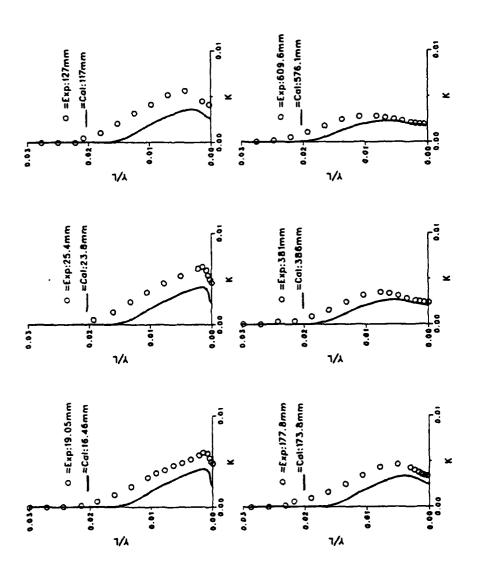


Fig.V-10. Turbulent Kinetic Energy Profiles

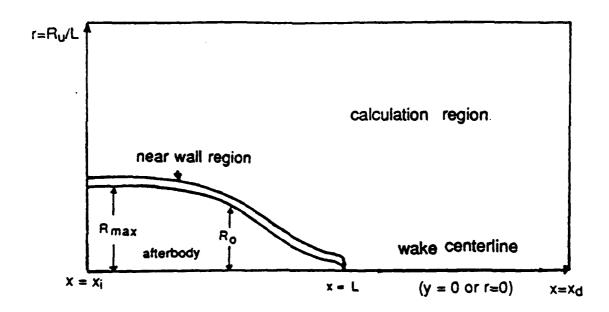


Fig.VI-1. Notations and Solution Domains

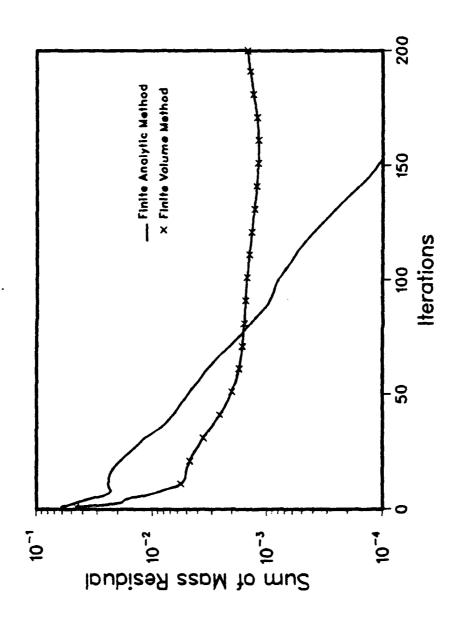


Fig.VI-2. Convergence History

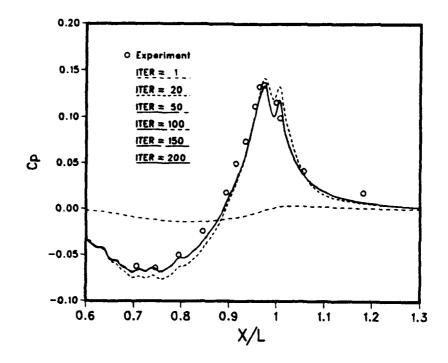


Fig.VI-3. Pressure Convergence History (Finite Analytic Method)

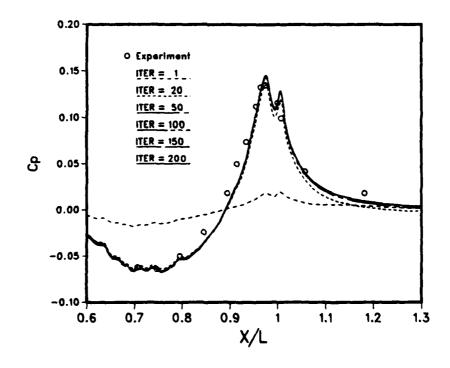


Fig.VI-4. Pressure Convergence History (Finite Volume Method)

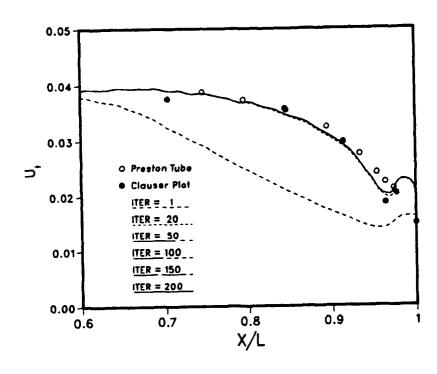


Fig.VI-5. Friction Velocity Convergence History (Finite Analytic Method)

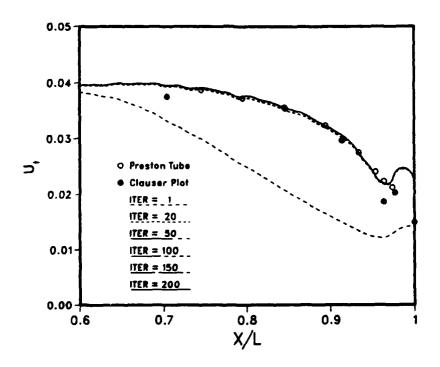


Fig.VI-6. Friction Velocity Convergence History (Finite Volume Method)

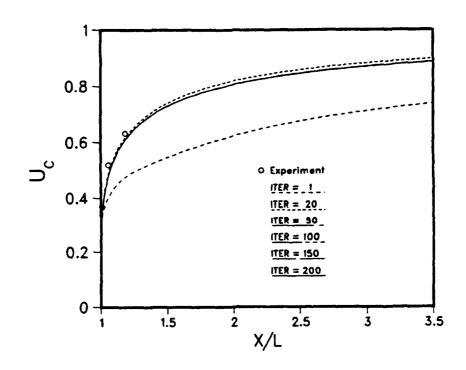


Fig.VI-7. Wake Centerline Velocity Convergence History (Finite Analytic Method)

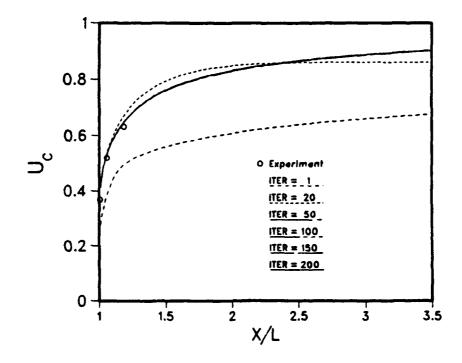


Fig.VI-8. Wake Centerline Velocity Convergence History (Finite Volume Method)

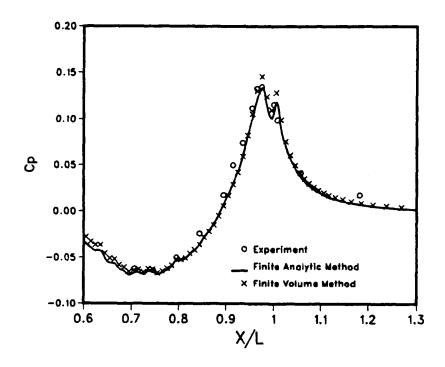


Fig.VI-9. Surface Pressure Distribution ( Afterbody-1 )

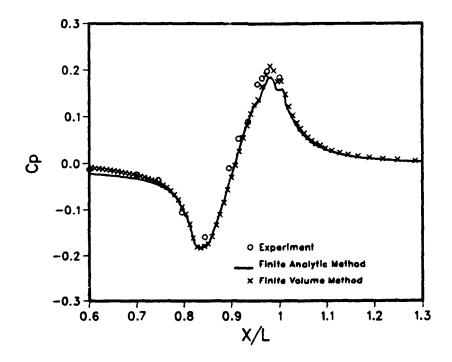


Fig.VI-10. Surface Pressure Distribution ( Afterbody-2 )

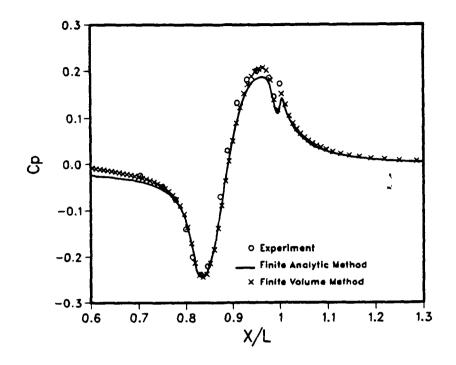


Fig.VI-11. Surface Pressure Distribution ( Afterbody-5 )

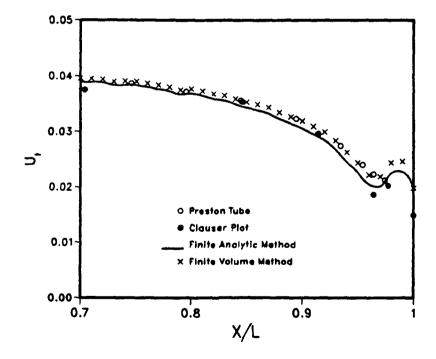
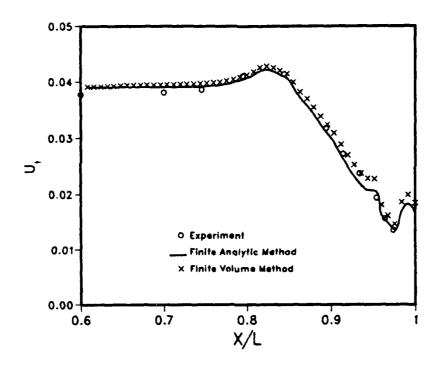


Fig.VI-12. Friction Velocity Distribution ( Afterbody-1 )



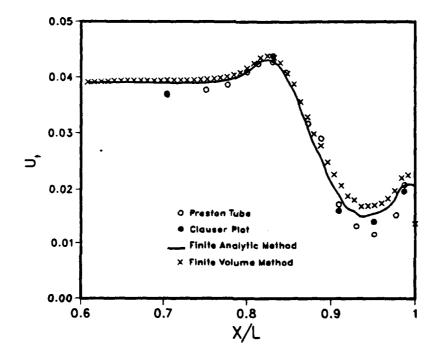
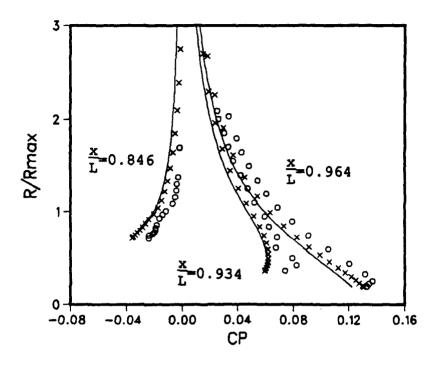


Fig.VI-14. Friction Velocity Distribution ( Afterbody-5 )



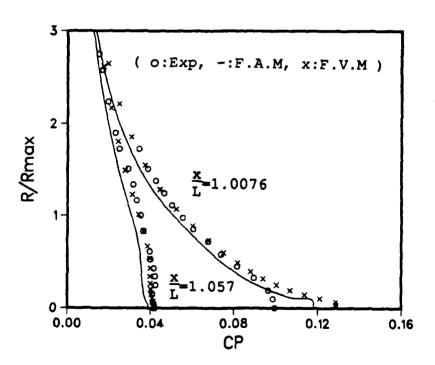


Fig.VI-15. Pressure Distributions ( Afterbody-1 )

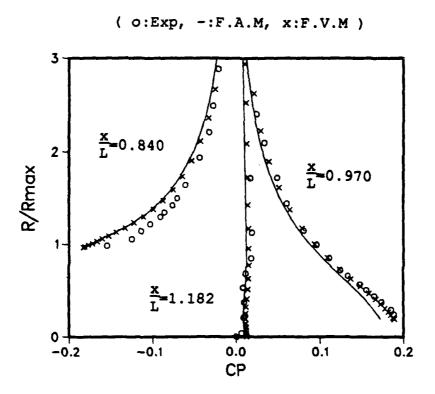
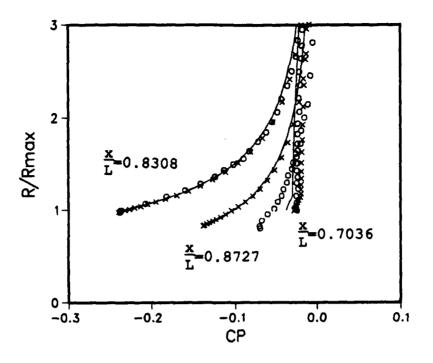


Fig.VI-16. Pressure Distributions ( Afterbody-2 )



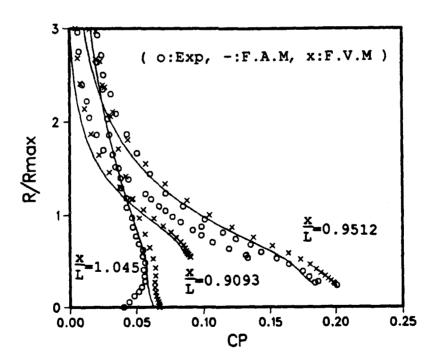


Fig.VI-17. Pressure Distributions ( Afterbody-5 )

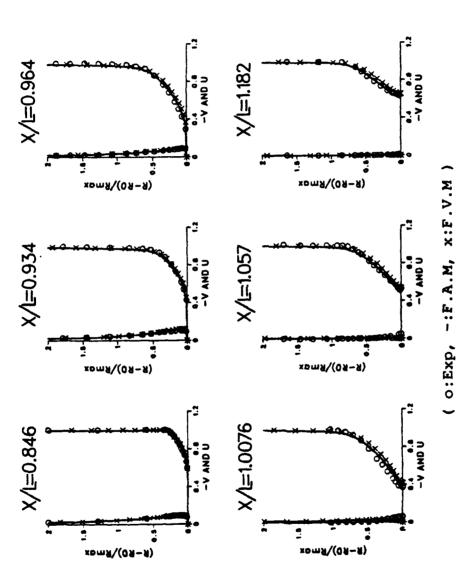
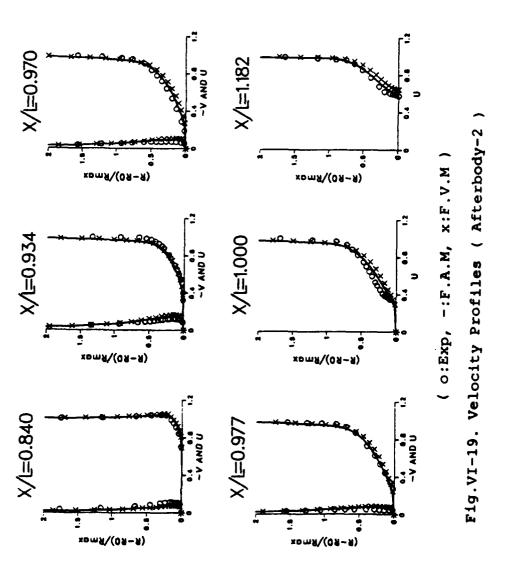
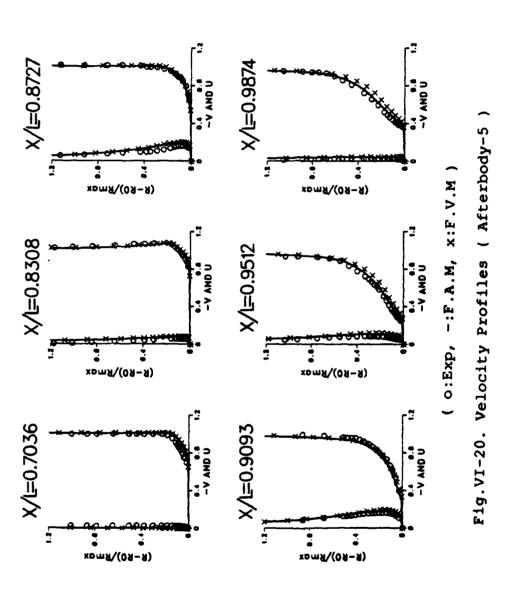
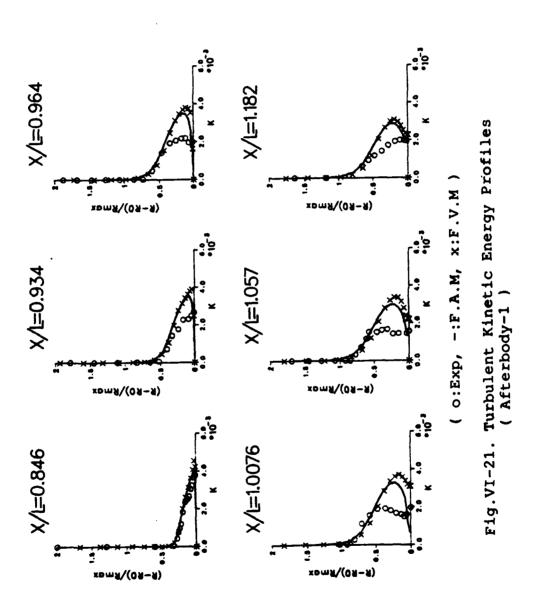


Fig.VI-18. Velocity Profiles ( Afterbody-1 )







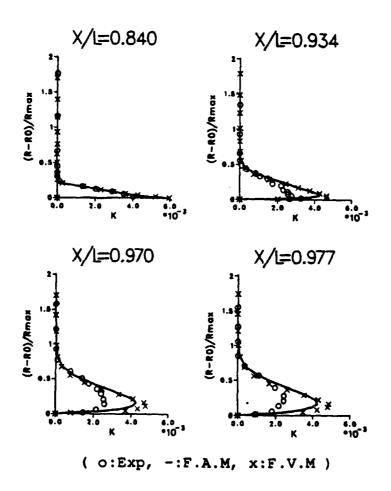
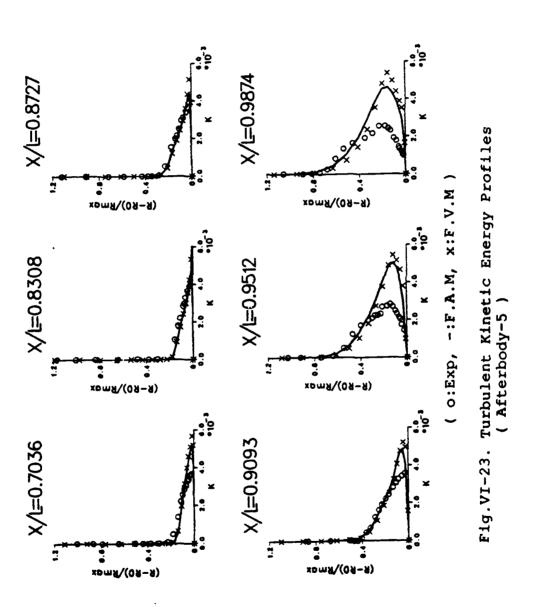


Fig.VI-22. Turbulent Kinetic Energy Profiles ( Afterbody-2 )



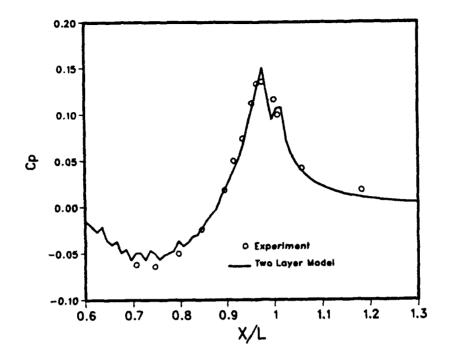


Fig.VI-24. Surface Pressure Distribution ( Afterbody-1 )

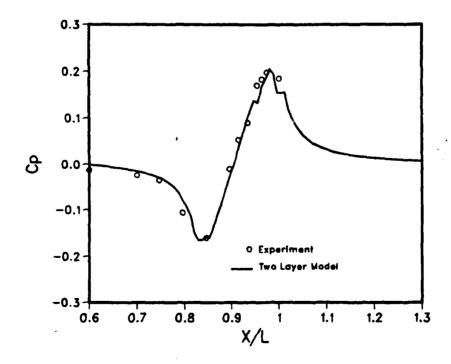


Fig.VI-25. Surface Pressure Distribution ( Afterbody-2 )

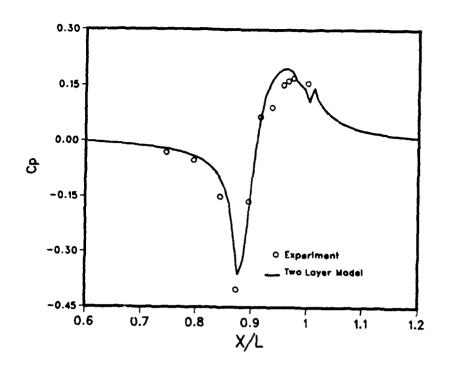


Fig.VI-26. Surface Pressure Distribution ( Afterbody-3 )

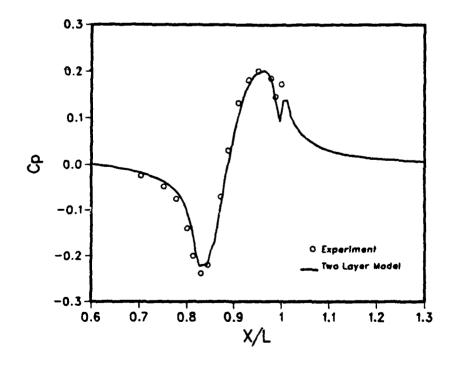


Fig.VI-27. Surface Pressure Distribution ( Afterbody-5 )

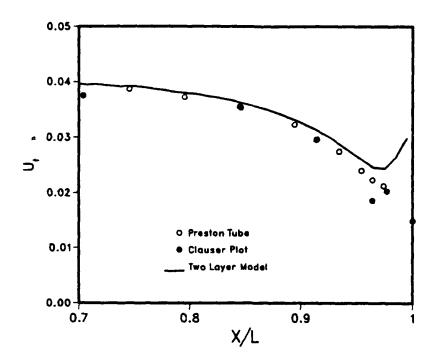


Fig.VI-28. Friction Velocity Distribution (Afterbody-1)

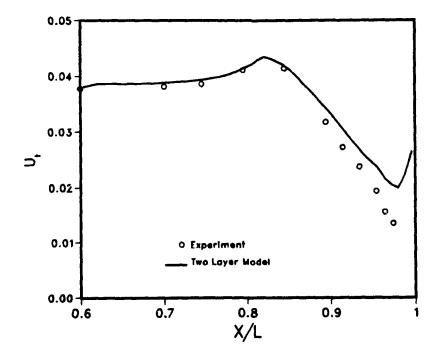


Fig.VI-29. Friction Velocity Distribution (Afterbody-2)

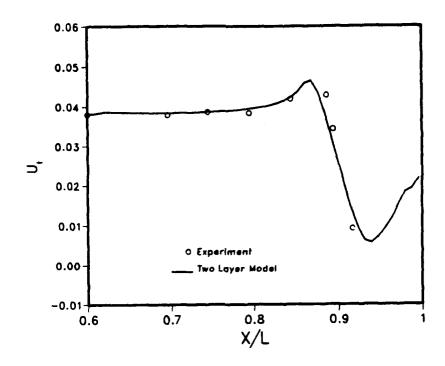


Fig.VI-30. Friction Velocity Distribution ( Afterbody-3 )

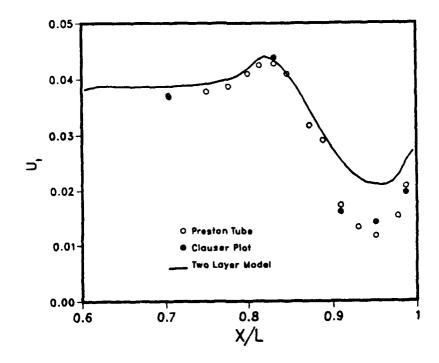


Fig.VI-31. Friction Velocity Distribution ( Afterbody-5 )

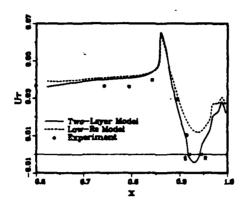


Fig.VI-32. Friction Velocity Distribution for Afterbody-3 Given in Ref.[56]

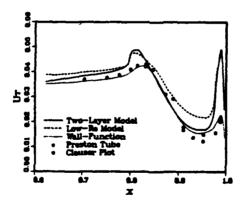


Fig.VI-33. Friction Velocity Distribution for Afterbody-5 Given in Ref.[56]

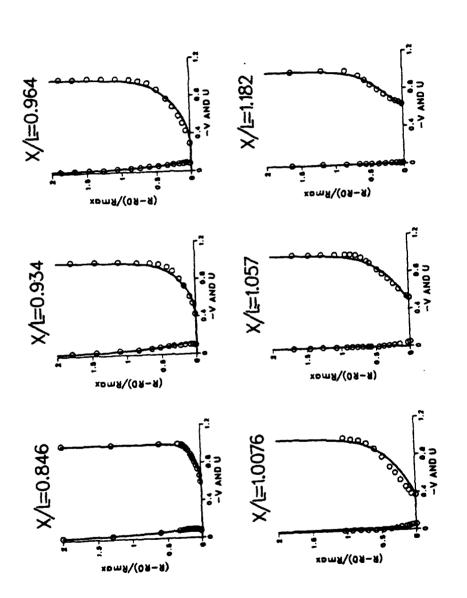


Fig.VI-34. Velocity Profiles ( Afterbody-1 )

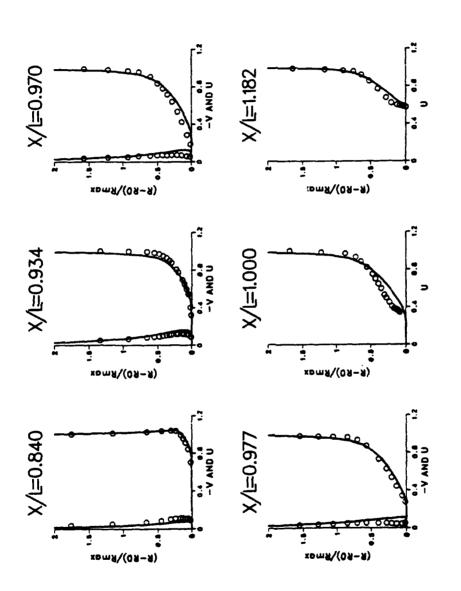


Fig.VI-35. Velocity Profiles ( Afterbody-2 )

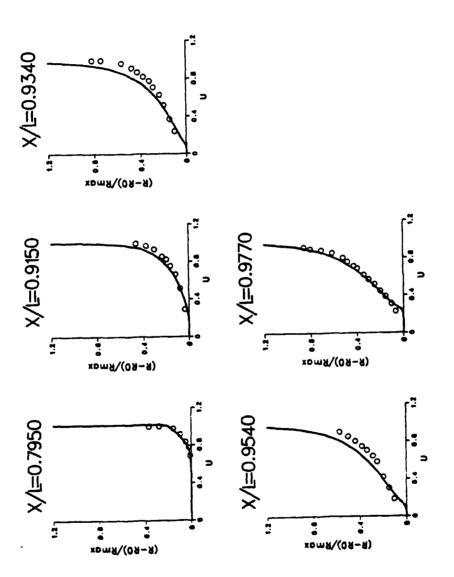


Fig.VI-36. Velocity Profiles ( Afterbody-3 )

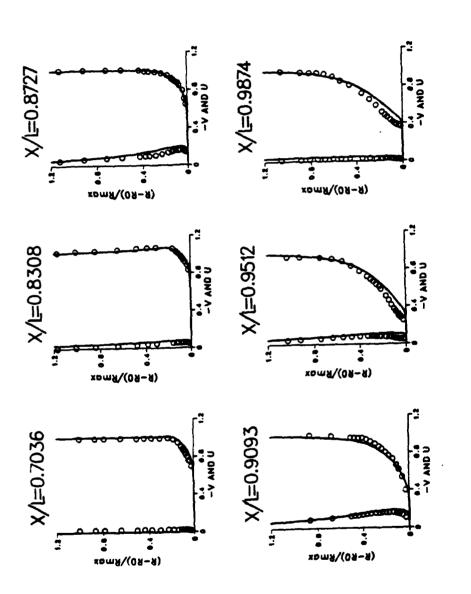


Fig.VI-37. Velocity Profiles ( Afterbody-5 )

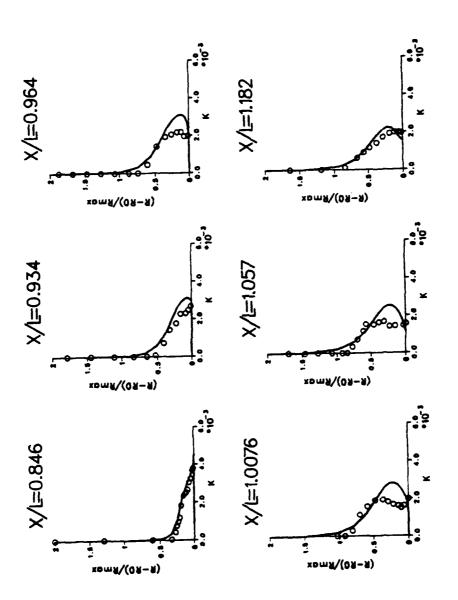


Fig.VI-38. Turbulent Kinetic Energy Profiles ( Afterbody-1 )

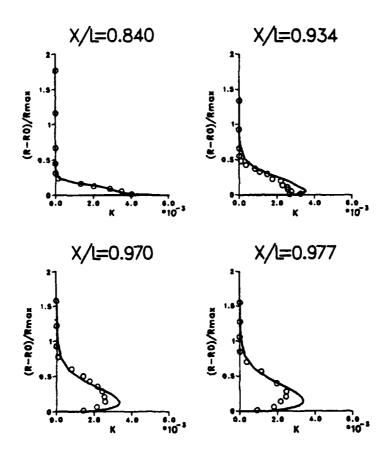


Fig.VI-39. Turbulent Kinetic Energy Profiles ( Afterbody-2 )

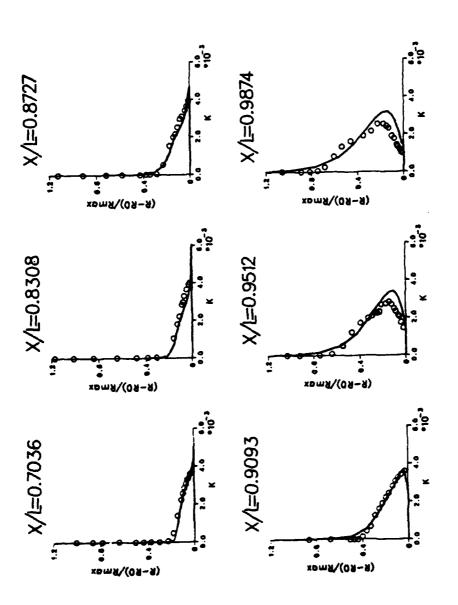


Fig.VI-40. Turbulent Kinetic Energy Profiles ( Afterbody-5 )

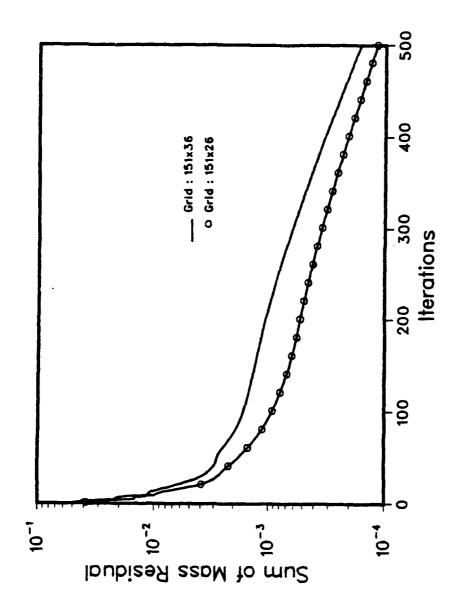


Fig.VII-1. Convergence History ( Afterbody-1 )

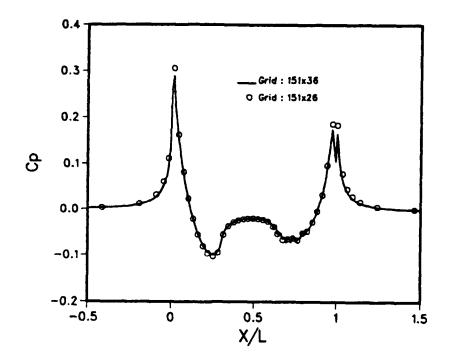


Fig.VII-2. Grid Dependence Test for Pressure ( Afterbody-1 )

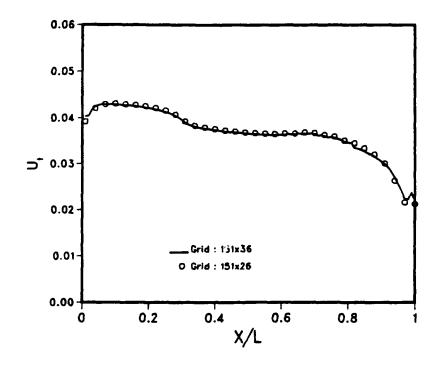
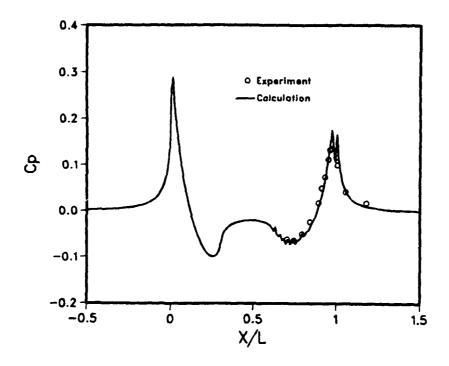


Fig.VII-3. Grid Dependence Test for Friction Velocity ( Afterbody-1 )



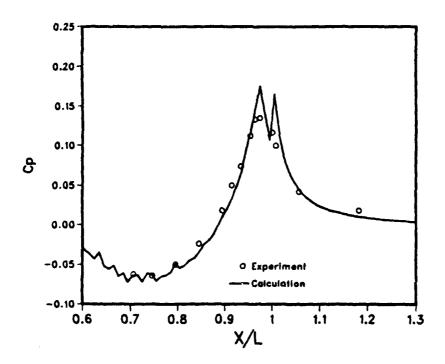
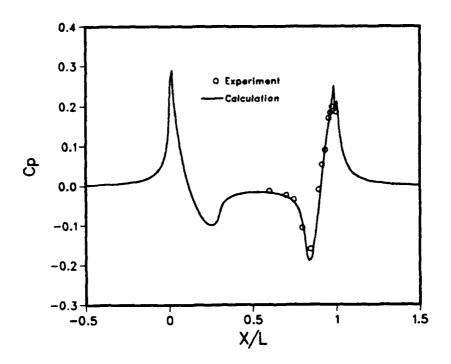


Fig.VII-4. Surface Pressure Distribution ( Afterbody-1 )



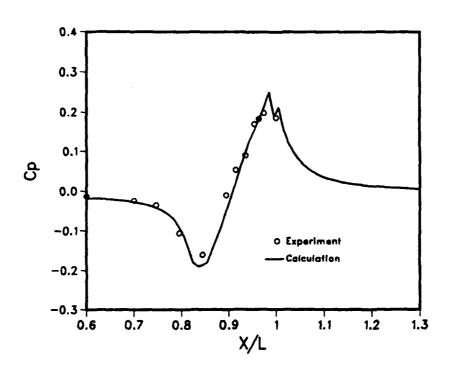
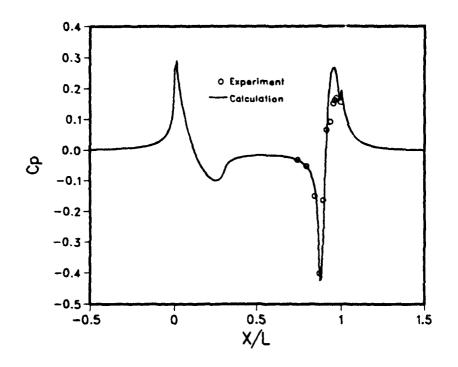


Fig.VII-5. Surface Pressure Distribution ( Afterbody-2 )



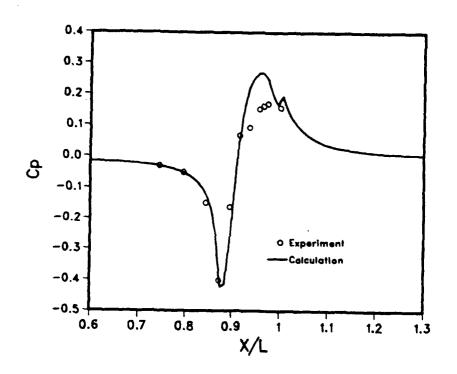
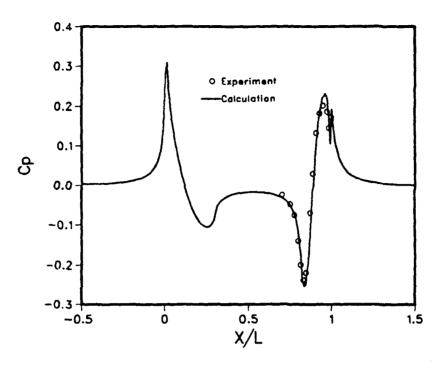


Fig.VII-6. Surface Pressure Distribution ( Afterbody-3 )



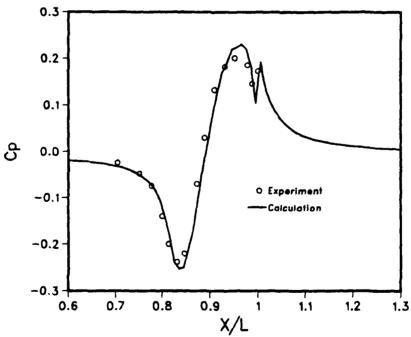
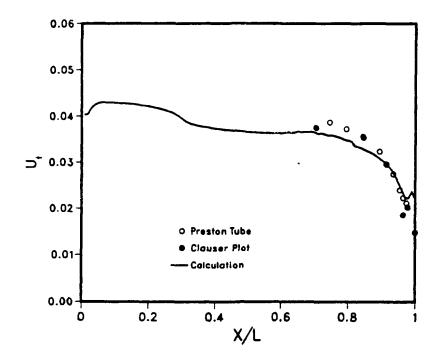
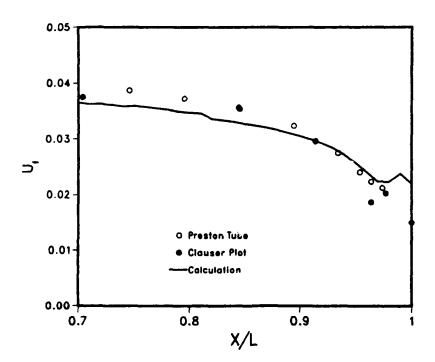
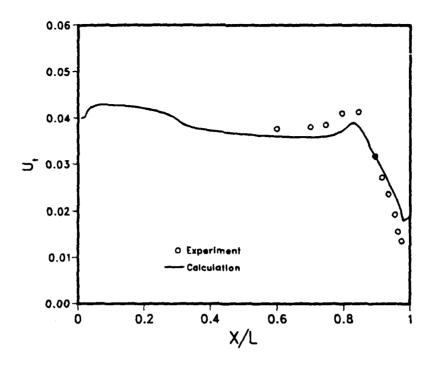


Fig.VII-7. Surface Pressure Distribution (Afterbody-5)







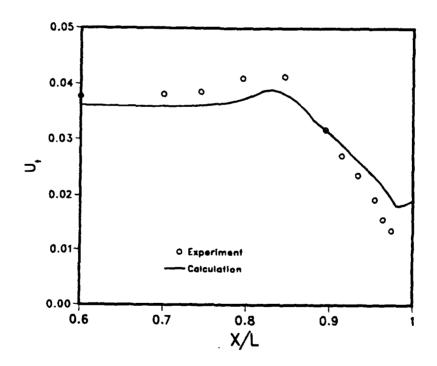
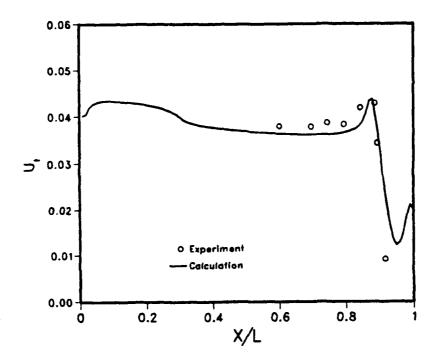


Fig.VII-9. Friction Velocity Distribution (Afterbody-2)



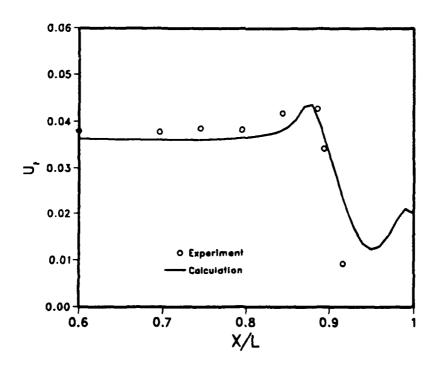


Fig.VII-10. Friction Velocity Pistribution ( Afterbody-3 )

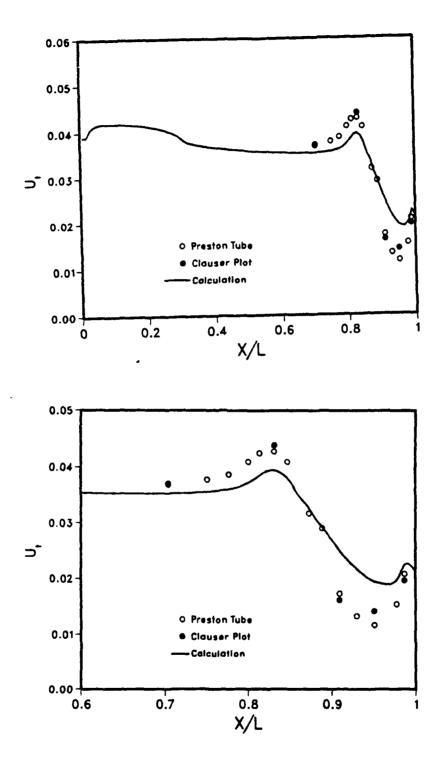


Fig.VII-11. Friction Velocity Distribution ( Afterbody-5 )

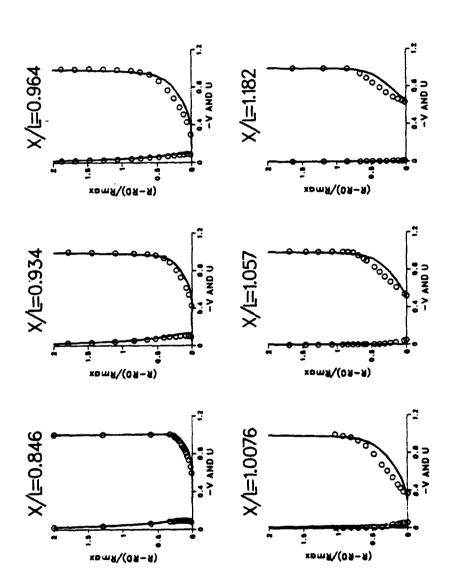


Fig.VII-12. Velocity Profiles ( Afterbody-1 )

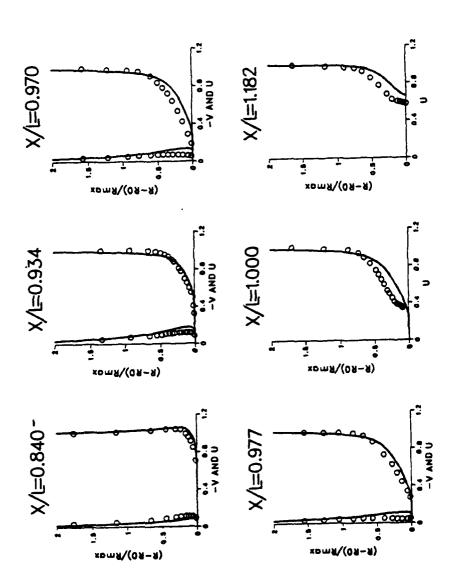


Fig.VII-13. Velocity Profiles ( Afterbody-2 )

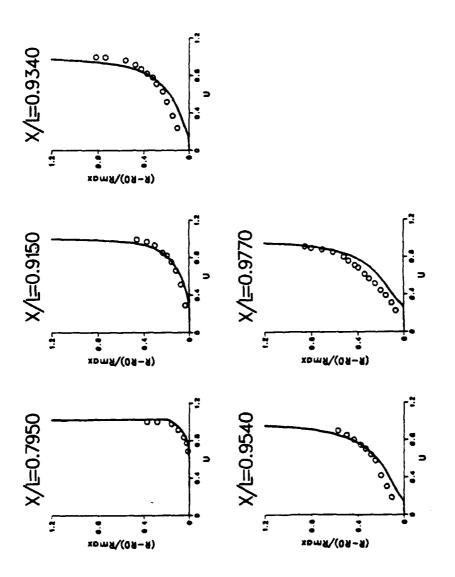


Fig.VII-14. Velocity Profiles ( Afterbody-3 )

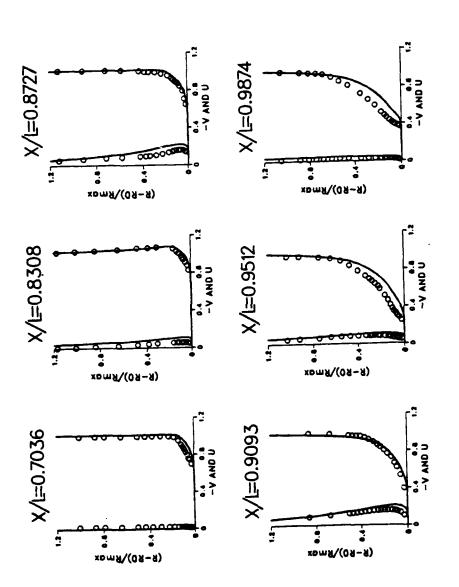


Fig.VII-15. Velocity Profiles ( Afterbody-5 )

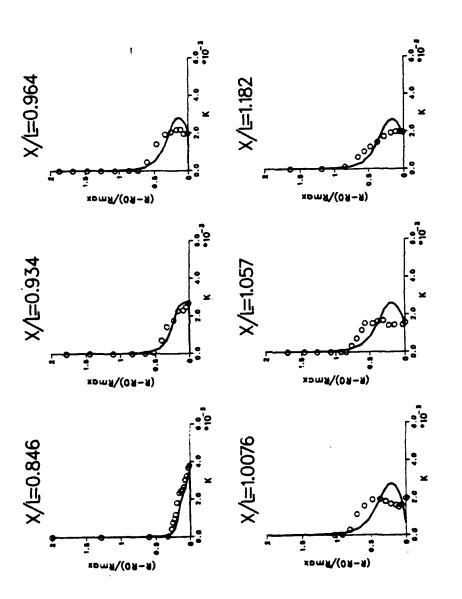


Fig.VII-16. Turbulent Kinetic Energy Profiles
 ( Afterbody-1 )

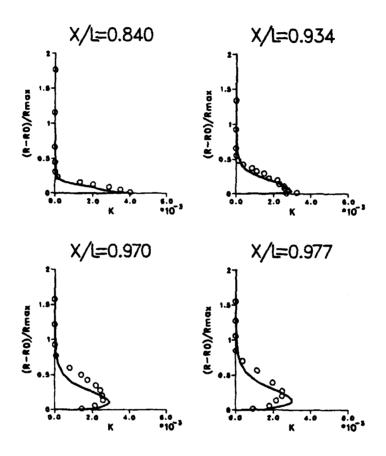


Fig.VII-17. Turbulent Kinetic Energy Profiles ( Afterbody-2 )

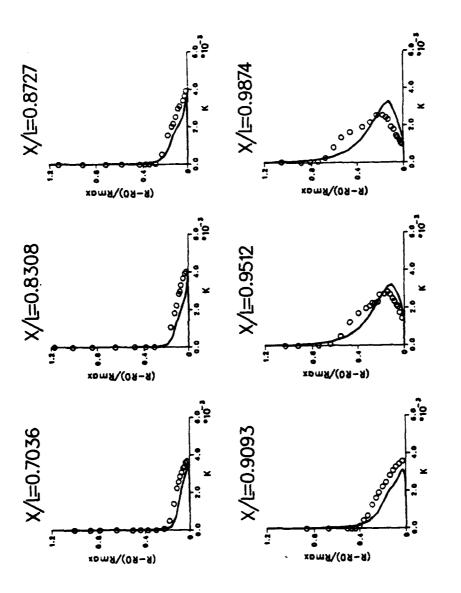


Fig.VII-18. Turbulent Kinetic Energy Profiles
 ( Afterbody-5 )

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APPENDIX

COMPUTER CODES

## Computer Code for Chapter-VI

- 1. Wall function Method
- 1-1) Geometric Data Files
- 1-2) Computer Program for the Generation of Boundary-Fitted Coordinates
- 1-3) Computer Program for Flow Calculation by Finite Analytic Method
- 1-4) Computer Program for Flow Calculation by Finite Volume Method
- 2. Two-Layer Model
- 2-1) Geometric Data Files
- 2-2) Computer Program for the Generation of Boundary-Fitted Coordinates
- 2-3) Computer Program for Flow Calculation by Finite Analytic Method

1

. 688000E+00 . 7220000E+00 . 7220000E+00 . 816000E+00 . 912000E+00 . 91200E+00 . 912000E+00 . 912000E+00 . 912000E+00 . 912000E+00 . 91200E+00 . 912000E+00 . 912000E+00 . 912000E+00 . 912000E+00 . 91200E+00 . 912000E+00 . 912000E+00 . 912000E+00 . 912000E+00 . 91200E+00 . 912000E+00 . 912000E+00 . 912000E+00 . 912000E+00 . 91200E+00 . 912000E+00 . 912000E+00 . 912000E+00 . 912000E+00 . 912000 .654000E+00 .656000E+00 .688000E+00 .7220000E+00 .752000E+00 .784000E+00 .816000E+00 .8480000E+00 000000000 .680000E+00
.712000E+00
.7140000E+00
.840000E+00
.840000E+00
.954000E+00
.956000E+01
.110788E+01
.110798E+01
.1107 616000E+00 .648000E+00 .7120000E+00 .712000E+00 .776000E+00 .842000E+00 .842000E+00 .842000E+00 00000000 7.000000E+00 7.768000E+00 7.768000E+00 8812000E+00 8812000E+00 982000E+00 992000E+00 992000E+01 102400E+01 102400E+01 102400E+01 102400E+01 102400E+01 102400E+01 102400E+01 102400E+01 102400E+01 103108E+01 124600E+01 124600E-01 124600E-01 124600E-01 124600E-01 124600E-01 1240100E-01 1240100E-01 1240100E-01 12528198E+01 1240100E-01 1240100E-01 12528198E+01 1240100E-01 12528198E+01 1240100E-01 12528198E+01 1240100E-01 12528198E+01 12528198 .608000E+00 .640000E+00 .672000E+00 .704000E+00 .708000E+00 .800000E+00 .810000E+00 .810000E+00 "ha5body" 0000000000 .600000E+00 .612000E+00 .664000E+00 .596000E+00 .728000E+00 .728000E+00 .792000E+00 .856000E+00 .664000E+00
.756000E+00
.756000E+00
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.824000E+00
.828000E+00
.925000E+00
.925000E+01
.101950E+01
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a

S-A

REYNOLDS NUMBERS AND FRICTION VELOCITIES AT THE MIDDLE OF THE BODY FROM EXPERIMENTAL DATA. NUMBER OF GRID POINTS IN X-DIRECTION. SOME CONSTANTS AND RELAXATION FACTOR OPEN(UNIT=11, FILE=FINAME(IBODY))
READ(11,1111)(X(I),I=1,IP1)
READ(11,1111)(RX(I),I=1,IP1)
CLOSE(11) READ BODY SHAPE AND X-COORDINATE. TRAILING (M2), EDGE OF THE BODY. NUMBER OF GRID IN Y-DIRECTION OF ITERATIONS ELSE IF(IBODY.EQ.5) THEN RE=9300000.D0 UTAU=0.040D0 ELSE IF(IBODY.EQ.2) THEN RE-6800000.D0 \U-0.040D0 PI=3.141592653589793D0 EPS=0.001 IF(IBODY.EQ.1) THEN MAXIMUM NUMBER RE-6600000.DO JHAX=34 JP1=JHAX+1 JHAH=JHAX-1 UTAU-0.04D0 IP1=IMAX+1 IM1=IMAX-1 ITMAX=200 MAX-95 RF=1.8 IMB=52 [KA-11 END IF [MA=2] MA-21 1111 0000 000 000 00000 υU O 0000 000 OOU

READ BODY TYPE FROM THE TERMINAL.

`

WANT ?' DTNSRDC' DTNSRDC' DTNSRDC'

WHAT KIND OF BODY DO YOU TYPE 1 FOR AFTERBODY1 OF TYPE 2 FOR AFTERBODY2 OF TYPE 5 FOR AFTERBODY5 OF

WRITE(\*,\*)
WRITE(\*,\*)
WRITE(\*,\*)

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DINDSRDC (TURBULENT). DINDSRDC (TURBULENT). DINDSRDC (TURBULENT).

IBODY-1 ; AFTERBODY1 OF IBODY-2 ; AFTERBODY2 OF IBODY-5 ; AFTERBODY5 OF

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AXISYMMETRIC BODIES.

F2NAME(1)/'halbout'/,F2NAME(2)/'ha2bout'/, F2NAME(3)/'ha3bout'/,F2NAME(4)/'ha4bout'/, F2NAME(5)/'ha5bo .t'/,F2NAME(6)/'ha6bout'/

DATA

FINAME(1)/'halbody', FINAME(2)/'ha2body'/ FINAME(3)/'ha3body'/, FINAME(4)/'ha4body'/ FINAME(5)/'ha5body'/,FINAME(6)/'ha6body'/

DATA

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F3NAME(1)/'halbdat'/,F3NAME(2)/'ha2bdat'/, F3NAME(3)/'ha3bdat'/,F3NAME(4)/'ha4bdat'/, F3NAME(5)/'ha5bdat'/,F3NAME(6)/'ha6bdat'/

DATA

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\* NUMERICAL GENERATION OF BODY FITTED COORDINATES

• OF ALMINAR AND TURBULENT FLOW CALCULATION

• POR LAMINAR AND TURBULENT FLOW CALCULATION

COMMON/XXX/X(200), Y(200,70) COMMON/ABC/AY(70), BY(70), CY(70), DY(70), TY(70) COMMON/YYY/RX(200), RD(200), CF(200), DX(70) COMMON/BBD/AAZ(200), DE(200), CC(200), DD(200), A(200) COMMON/AAAI/AII(200,70), AIZ(200,70), AZZ(200,70), AJ (200,70) COMMON/AAAZ/FI(200), FZ(200,70) COMMON/AAAZ/FI(200), FZ(200,70)

COMMON/AAA/XC(200,70), YC(200,70)

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IMPLICIT REAL\*8(A-H,O-Z)

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CHARACTER\*10 FINAME(10) CHARACTER\*10 F2NAME(10) CHARACTER\*10 F3NAME(10)

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PROGRAM FAHALP

IMPLICIT DOUBLE PRECISION (A-H,0-Z) CHARACTER\*10 FINIME(6)
CHARACTER\*10 FINIME(6)
CHARACTER\*10 FINIME(6)
CHARACTER\*10 FINIME(6)
CHARACTER\*10 FINIME(6) U Ü WELOCITY AT PREVIOUS TIME STEP.

MASS SOURCE FOR PRESSURE EQUATION.

MASS SOURCE FOR PRESSURE CORRECTION EQUATION.

MASS SOURCE GENERATED BY NON-ORTHOGONALITY OF GRID.

TURBULENT KINETIC ENERGY.

TURBULENT DISSIPATION RATE.

TURBULENT DISSIPATION RATE.

TURBULENT GENERATION RATE.

TURBULENT GENERATION TERM.

COEF OF PRESSURE TERM IN MOMENTUM EQUATION.

V-VELOCITY AT THE WALL FUNCTION CALCULATION POINT. ib : SOURCE TERM FOR U, V, K, E.
COEFFICIENTS : B11, B22, B12, G11, G12, G12, A11, A22, A12 PROGRAM NAME: BFANS2.F77. PROGRAMMER: SEOK KI CHOI. (EB-2203) VARIABLES INTERPRETATION. (NEARLY SAME AS FANS-2)

COMMON/COEF7/CF(3,3)
COMMON/FA1/AR,BR,DR,ER,FR
COMMON/FA1/AR,BI2,B1,B12
COMMON/BODY1/B11,B12,B21,B12
COMMON/BODY2/G11,G12,B21,A12,A22,G,AJI
COMMON/CONS1/I,J,IMAX,JMAX,IB1,JF1,JAU,JAV,JAP,JA,H2,H2H1
COMMON/CONS1/I,J,IMAX,JMAX,IB1,JF1,JAU,JAV,JAP,JA,H2,H2H1
COMMON/CONS2/NITER,ITH,IEND,ITERA
COMMON/CONS3/EMAX,FMAX,EPE,EPE1,PI COMMON/PRES1/PRO(1D, JD), PP(1D, JD), PR(1D, JD)

COMMON/PRES2/CU(1D, JD), CV(1D, JD), CUY(1D, JD)

COMMON/PRES3/BCU(1D, JD), YP(1D, JD)

COMMON/GEO2/XC(1D, JD), YP(1D, JD)

COMMON/GEO2/XC(1D, JD), YV(1D, JD)

COMMON/GEO2/XU(1D, JD), YV(1D, JD)

COMMON/GEO3/XU(1D, JD), YV(1D, JD)

COMMON/GEO3/XU(1D, JD), YV(1D, JD)

COMMON/GEO3/XU(2(1D), YV3(1D), YV4(1D)

COMMON/GEO5/YV2(1D), YV3(1D), YV4(1D)

COMMON/GEO5/YV2(1D), YV3(1D), YV4(1D)

COMMON/GEO5/YV2(1D), YV3(1D), YV4(1D)

COMMON/GEO3/YV2(1D), YV3(1D), YV4(1D)

COMMON/GEO3/YV2(1D), YV3(1D), YV4(1D)

COMMON/GEO3/YV2(1D), YV3(1D), YV3(1D)

COMMON/MALL2/YFP, COSA, UTAU, TAUM

COMMON/MALL2/YFP, COSA, UTAU, TAUM

COMMON/MALL2/YFP, COSA, UTAU, TAUM

COMMON/MALL2/YFP, COSA, UTAU, TAUM

COMMON/WELL/U(1D, JD), DS(1D, JD), D3(1D, JD)

COMMON/VELL/U(1D, JD), YO(1D, JD)

COMMON/TURB3/TYE(1D, JD) COMMON/STIN/SKP(ID,JD),SK(ID,JD),SK(ID,JD),SC(ID,JD)
COMMON/STIN/SKP(ID,JD),SDP(ID,JD)
COMMON/UCOEFI/UMB(ID,JD),UMC(ID,JD),UMT(ID,JD)
COMMON/UCOEFI/UMB(ID,JD),UMC(ID,JD),UMT(ID,JD)
COMMON/UCOEFI/UMB(ID,JD),UMC(ID,JD),UMT(ID,JD)
COMMON/UCOEFI/UMB(ID,JD),VMC(ID,JD),UMT(ID,JD)
COMMON/UCOEFI/VMB(ID,JD),VMC(ID,JD),VMT(ID,JD)
COMMON/TKCOEFI/TKMB(ID,JD),TKMC(ID,JD),TKMT(ID,JD)
COMMON/TKCOEFI/TWMB(ID,JD),TKMC(ID,JD),TKMT(ID,JD)
COMMON/TKCOEFI/TWMB(ID,JD),TKMC(ID,JD),TKMT(ID,JD)
COMMON/TKCOEFI/TWMB(ID,JD),TWC(ID,JD),TKMT(ID,JD)
COMMON/TKCOEFI/TWMB(ID,JD),TWC(ID,JD),TWMT(ID,JD)
COMMON/TDCOEFI/TWMB(ID,JD),TDMC(ID,JD),TDMT(ID,JD)
COMMON/TDCOEFI/TDMB(ID,JD),TDMC(ID,JD),TDMT(ID,JD)
COMMON/TDCOEFI/TDMB(ID,JD),TDMC(ID,JD),TDMT(ID,JD) PARAMETER (ID=142,JD=45)

DATA

DATA

READ(\*,\*) IBODY

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DATA

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DATA

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XF(I,J)=0.25*(XC(I,J)+XC(I-1,J)+XC(I,J-1)+XC(I-1,J-1))
XU(I,J)=0.5*(XC(I,J)+XC(I,J-1))
XU(I,J)=0.5*(XC(I,J)+XC(I-1,J))
YU(I,J)=0.5*(YC(I,J)+YC(I-1,J))
YV(I,J)=0.5*(YC(I,J)+YC(I-1,J))
YY(I,J)=0.5*(YC(I,J)+YC(I-1,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   DO 114 J-1,JP1

XC(IP1,J)=XC(IMAX,J)+0.5*(XC(IMAX,J)-XC(IMAX-1,J))

XP(IP1,J)=XC(IP1,J)

XU(IP1,J)=XC(IP1,J)

YC(IP1,J)=YC(IMAX,J)

YP(IP1,J)=YP(IMAX,J)

YP(IP1,J)=YP(IMAX,J)

YP(IP1,J)=YP(IMAX,J)

YP(IP1,J)=YP(IMAX,J)
    XU(1,3)=XC(1,3)

YU(2,3)=0.5*(YC(1,3)+YC(1,3-1))

XP(1,0)=XC(1,3)

YP(1,3)=0.5*(YC(1,3)+YC(1,3-1))

XV(1,3)=XC(1,3)

1 YV(1,3)=XC(1,3)
                                                                                                                                                    XU(I,1)=XC(I,1)
XP(I,1)=0.5*(XC(I,1)+XC(I-1,1))
XV(I,1)=0.5*(XC(I,1)+XC(I-1,1))
YU(I,1)=YC(I,1)
YP(I,1)=0.5*(YC(I,1)+YC(I-1,1))
XV(I,1)=0.5*(YC(I,1)+YC(I-1,1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 DO 115 I=1, IP1
YP2(1)=YP(1,2)=YP(1,1)
YP4(1)=YP(1,3)=YP(1,1)
YP4(1)=YP(1,4)=YP(1,1)
YU2(1)=YU(1,2)=YU(1,1)
YU3(1)=YU(1,2)=YU(1,1)
YU4(1)=YU(1,2)=YU(1,1)
YU3(1)=YU(1,2)=YU(1,1)
YU3(1)=YU(1,2)=YU(1,1)
YU3(1)=YU(1,3)=YU(1,1)
YU3(1)=YU(1,4)=YU(1,1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       YP2SQ(I)=YP2(I)*YP2(I)
YP3SQ(I)=YP3(I)*YP3(I)
YP4SQ(I)=YP4(I)*YP4(I)
YU2SQ(I)=YU2(I)*YU2(I)
                                                                                                                                                                                                                                                                                                                                                                                                    DO 113 I=1,IMAX
YC(I,JP1)=YC(I,JP1)
YV(I,JP1)=YV(I,JP1)
YP(I,JP1)=YV(I,JP1)
YU(I,JP1)=YV(I,JP1)
XC(I,JP1)=XV(I,JMAX)
XV(I,JP1)=XV(I,JMAX)
XP(I,JP1)=XV(I,JMAX)
XV(I,JP1)=XV(I,JMAX)
                                                                                                                       DO 112 I=2, IMAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          DO 116 I=1, IP1
                                                                                                                                                                                                                                                                       112
                                                                                       111
                                                                                                                                                                                                                                                                                                                                                                         112
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       113
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        115
                                                                                                                                      Ç
                                                                                                       U
                                                                                                                                                                                                                                                         U
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             XC(1,JP1)=XC(1,JNAX)
YC(1,JP1)=YC(1,JNAX)+(YC(1,JNAX)-YC(1,JNAX-1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           READ(11,2006) ((XC(I,J),I=1,IMAX),J=1,JHAX)
READ(11,2006) ((YC(I,J),I=1,IMAX),J=1,JHAX)
READ(11,2006) ((F1(I,J),I=1,IMAX),J=1,JHAX)
FORMAT(6E11.6)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              XC,YC---- CONTROL VOLUME POINT
XU,YU---- U CALCULATION POINT
XV,YY----- V CALCULATION POINT
XP,YP----- P,K,E CALCULATION POINT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             OFFSET OF NUMERICAL GRIDS
                                                                                                                                                                                                                                                                                                                                                                                              OPEN(UNIT-8, FILE-F2NAME(IBODY))
OPEN(UNIT-7, FILE-F3NAME(IBODY))
OPEN(UNIT-9, FILE-F4NAME(IBODY))
OPEN(UNIT-10, FILE-F5NAME(IBODY))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             OPEN(UNIT-11, FILE-FINAME(IBODY))
                                                                                                                                                                                                                                                                               TIME STEP AND REYNOLDS NUMBER.
                                                TURBULENCE MODEL CONSTANTS
                 PI=3.141592653589793D0
                                                                                               CNU2=DSQRT (CNU)
CNU4=DSQRT (CNU2)
CNU3=CNU4+CNU4+CNU4
CNU21=1./CNU2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            XU(1,1)=XC(1,1)
YU(1,1)=YC(1,1)
XV(1,1)=XC(1,1)
YV(1,1)=YC(1,1)
XP(1,1)=XC(1,1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             YP(1,1)-YC(1,1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               DO 111 3-2, JP1
                                                                                                                                                                                                                                                                                                                              TAU-1.
TAUI-1./TAU
                                                                                                                                                             CEPSI=1.44
CEPS2=1.92
CEPK=1.0
CEPS=1.3
CKAR=0.418
E=9.
EPEW=0.0001
                                                                                                                                                                                                                                                                                                              REI-1./RE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               CLOSE(11)
                                                                                CNU=0.09
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                2006
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		15 CONTINUE C	C START SPACE MARCHING FROM UPSTREAM TO DOWN STREAM.		C INITIAL GUESS FOR THE FIRST MARCHING PROCESS. C ARRESTABLES FOR THE FIRST MARCHING PROCESS.	C IF(NITER.EQ.1) THEN	C UTAUA(I)-UTAUA(I-1)	C U(I,J)=U(I-1,J)		C U(I+1,J) = U(I,J) V(I+1,J) = V(I,J) US(I+1,J) = US(I,J)	VS(1+1,3) = VS(1,3) UO(1+1,3) = UO(1,3)	VO(I+1,J)=VO(I,J) TKEO(I+1,J)=TXEO(I,J)	TDSO(1+1,J) =TDSO(1,J) TRE(1+1,J) =TRE(1,J) TDS(1+1,J) =TDS(1,J)	18 CONTINUE C	END IF C constants to the constants of the constant of the consta	
C ELSE IF(YPLUS.LT.1000.D0) THEN U0(1,J)=(2.5D0*DLOG(YPLUS)+5.5D0)*UTAUA(1)	C	ELSE UO(1,3)=1.Do END IF		TREO(1,J)-UTADA(1)+UTAUA(1)+CNU2I+(1ETA) IF(ETA.GE.1.0)TKEO(1,J)-1.0D-8 TDSO(1,J)-CNU3+TKEO(1,J)+*1.5/(CKAR*YY)	C TME(1,J)=TMEO(1,J) TDG(1,J)=TPGO(1,J) U(1,J)=U0(1,J)	US(1,3) =U(1,3) UH(1,3) =U(1,3)	122 CONTINUE C	C COMPUTE INLET MEAN VELOCITY, MASS FLUX C AND MOUNTWITH FLUX. C SARBERFREE FRUX.	FLOWIN=0.DO DO 123 J=2,JWAX ADD 123 J=2,JWAX ARDEN-YU(1,J)*(YC(1,J)-YC(1,J-1)) FLOWIN-FLOWIN+ARDEN*UO(1,J) 123 CONTINUE	C START TIME MARCHING (ITERATIONS)	C DO 4000 NITER-1, IEND	RESPOND DO	DO 4 J=1,JP1 V(1,J)=VO(1,J) VS(1,J)=V(1,J)	4 VH(1,3)=V(1,3)	DO 14 J-1,JP1 DO 14 J-1,JP1 CU(I,J)=0.DO CV(I,J)=0.DO CUY(I,J)=0.DO	DS(I,J)=0. 14 PP(I,J)=0.

C DO 20 J=4,JP1 IF(TNU(I,J-1).LE.TNU(I,J-2).AND.TNU(I,J-1).LT. 1 TNU(I,J) TNU(I,J)=TNU(I,J-1) 20 CONTINUE	D=REFF*UPC(I,J)/(1.+D1(I,J)*UPC(I,J)) CU(I,J)=D/(XP(I+1,J)-XP(I,J)) CUY(I,J)=D*(YP(I,J)-YP(I+1,J))/(XP(I+1,J)-XP(I,J)) C /(0.25*(YP(I,J+1)+YP(I+1,J+1)-YP(I+1,J-1)-YP(I,J-1))) BCU(I,J)=B11C(I,J)*CU(I,J)
IF(I.EQ.2) THEN	23 CONTINUE
21 TNU(1,J)=TNU(2,J) END IF	DO 24 J=JAP,JP1 BCU(1,J)=0. 24 BCU(IP).J)=0.
IF(NITZR.EQ.1) THEN DO 22 J=1.JP1	
22	C CALCULATE THE COEFFICIENT FOR V-MONENTUM EQUATION.
C CALCULATES THE CORPTICIENTS FOR THE U-MOMENTUM EQUATION.	C Do 25 J=JAV,JHAX
DO 23 3-5AU,3MAX	TNUP=0.5*(TNU(I,J+1)+TNU(I,J)) REFF=1./(REI+TNUP)
TNUP=0.5+(TNU(I+1,J)+TNU(I,J))	CALL SOURCEV
C CALL COLLEGE	UU=0.25*(U0(I,J)+U0(I,J+1)+U0(I-1,J)+U0(I-1,J+1))
כ כאדו פסתאכבת	FX=-A11V(I,J)*(FI(I,J)+FI(I-1,J))
	FY=-A22V(I,J)*(F2(I,J)+F2(I-1,J))+1./B11V(I,J) ER=BSGRT(A11V(I,J)) FPE-DSORT(A22V(I,J))
FX=-2.*Allu(1,J)*F1(1,J) FX=-A22u(1,J)*(F2(1,J)+F2(1,J-1))+1./Bllu(1,J)	AR=0.5*(REFF*AJIV(I,J)*(B11V(I,J)*UU+B21V(I,J)*VV)~FX) BR=0.5*(REFF*AJIV(I,J)*(B12V(I,J)*UU+B22V(I,J)*VV)-FY)
ER-DSQRT(Allu(I,J)) FR-DSORT(Allu(I,J))	DR=2, 4AR
AR-0.5*(REFFAAIU(I,J)*(B11U(I,J)*UU+B21U(I,J)*VV)-FX) BR-0.5*(REFF*AIU(I,J)*(B12U(I,J)*UU+B22U(I,J)*VV)-FY)	
	ELISE CALL CORPES
CALL CORPES	VNB(I,J) =CF(1,1)
ELSE CALL COEFF3	VWC(I,J) = CF(1,Z) VWT(I,J) = CF(1,Z) VDB(T,T) = T_T_T_T_T_T_T_T_T_T_T_T_T_T_T_T_T_T_T
C END IF	VPC(I,J)=CF(2,2)
UMB(1,J)=CF(1,1) UMC(1,J)=CF(1,2)	VPT(I,J)=CF(2,3) VEB(I,J)=CF(3,1)
UMT(1,3) = CF(1,3)	VEC(I,J)=CF(3,2) VET(I,J)=CF(3,3)
UPC(1,J) =CF(2,Z)	IF(IFA.EQ.2) THEN
UPT(1,3)=CF(2,3) UEB(1,3)=CF(3,1)	D2(1,3)=VWC(1,3) ELSE
UEC(I,J) = CF(3,2) UET(I,J) = CF(3,3)	D2(1,3)=0. END IF
IF (IPA. EQ. 2) THEN	C
	D=REFF*VPC(I,J)(1.+D2(I,J)+E2(I,J)*VPC(I,J)) CU(I,T)=D/(VP(I,J)+D/I,J)+E2(I,J)*VPC(I,J))
	BCV(I,J)=B22C(I,J)*CV(I,J)
E1(1,J)-REFF*TAUI	25 CONTINUE

CALCULATE V-STÁR VELOCITY.

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UU#0.5*(U0(I,J)+U0(I-1,J))*CEPK
VV#0.5*(V0(I,J-1)+V0(I,J))*CEPK
FX#-0.5*AllP(I,J)*(F1(I,J)+F1(I-1,J)+F1(I,J-1)+F1(I-1,J-1))
FY#-0.5*A22P(I,J)*(F2(I,J)+F2(I-1,J)+F2(I,J-1)+F2(I-1,J-1))+
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      CALCULATE F-A COEFFICIENT OF TURBULENT KINETIC ENERGY.
                                                                                                                                                        FR=DSQRT(A22P(I,J))
AR=0.5*(REFF*AJIP(I,J)*(B11P(I,J)*UU+B21P(I,J)*VV)-FX)
BR=0.5*(REFF*AJIP(I,J)*(B12P(I,J)*UU+B22P(I,J)*VV)-FY)
                                                                                                                                                                                                                                                                                                                                                                                                    U(I,JAU-1) = ((YU4SQ(I) -YUZSQ(I)) *U(I,JAU)

- (YU3SQ(I) -YUSQ(I)) *U(I,JAU+1))

- (YU4SQ(I) -YU3SQ(I))

U(I,JAU-2) = (YU4SQ(I)*U(I,JAU) - YU3SQ(I)*U(I,JAU+1))

/ (YU4SQ(I) - YU3SQ(I))
DD(J)=BCU(I,J)*PP(I+1,J)+BCU(I-1,J)*PP(I-1,J)
-DS(I,J)
CALL TRIDAG(JAP,JMAX,AA,BB,CC,UD,T)
                                                                                                                                                                                                                                                                                                             V(I,J)=VS(I,J)-CV(I,J)*(PP(I,J+1)-PP(I,J))
V(I,JP1)=V(I,JMAX)*B22C(I,JMAX)/B22C(I,JP1)
                                                                                                                                                                                                                                                       U(I,J) = US(I,J) - CU(I,J) * (PP(I+1,J) - PP(I,J))
                                                                                                                                                                          CALCULATE VELOCITY CORRECTION FIELD.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     V(I,2) "V(I,JAV) *YV2(I)/YV3(I)
                                                                                                                                                                                                                                                                                                                                                                    IF(I.LT.M2) GO TO 42
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  C 1./B11P(I,J)
ER=DSQRT(A11P(I,J))
FR=DSQRT(A22P(I,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   TNUP=TNU(I,J)
REFF=1./(REI+TNUP)
CALL SOURCEK
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              TKWB(1, J) = CF(1, 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 TKWC(I, J) = CF(1, 2)
                                                                                                                                                                                                                                    40 J-JAU, JMAX
                                                                                                                                                                                                                                                                                          DO 41 J-JAV, JHAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   IF(IFA.EQ.2)THEN
                                                             DO 39 J=JAP, JMAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 DO 50 J-JA, JMAX
                                                                              PP(I,J)=T(J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CALL COEFF2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           CALL COEFF3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        V(I,1)=0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           42 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                777 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  DR-2. *AR
                                                                                                CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           END IF
                                                                                                                                                                                                                                      8
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                                                                                                                                                                                                                                                                                                                                                                                                                                           CALCULATE MASS SOURCE FOR PRESSURE CORRECTION EQUATION.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               DO 37 ITER=1,ITPP
DO 38 J=JAP,JHAX
AA(J)=-BCV(I,J-1)
BB(J)=BCV(I,J)+BCV(I,J)+BCV(I,J)+BCV(I,J-1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     DS(I,J) =B11C(I,J) +US(I,J) -B11C(I-1,J) +US(I-1,J) + H22C(I,J) +VS(I,J) -B22C(I,J-1) +VS(I,J-1)
                                                                                                                                   +VET(I,J) *VS(I+1,J+1) +VWC(I,J) *VS(I-1,J)
+VWB(I,J) *VS(I-1,J-1) +VWT(I,J) *VS(I-1,J+1)
+VPC(I,J) *(E2(I,J) *VO(I,J) +VV(I,J))
-BB(J) *CV(I,J) *(PR(I,J+1) -PR(I,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      VE=0.25*(V(I,J)+V(I,J-1)+V(I+1,J)+V(I+1,J-1))
VN=0.25*(V(I-1,J)+V(I-1,J-1)+V(I,J)+V(I,J-1)
UN=0.25*(V(I,J)+U(I-1,J)+V(I,J-1)+V(I-1,J+1)
UB=0.25*(V(I,J)+V(I-1,J)+V(I,J-1)+V(I-1,J-1))
DF(I,J)=B21C(I,J)*VE=B21C(I-1,J)*VW
+B12C(I,J)*VA=B21C(I,J-1)*VB
                                                                                                                                                                                                                                                                                                   vs(I,JP1)=vs(I,JMAX)*B22C(I,JMAX)/B22C(I,JP1)
IF(I,LT,M2) GO TO 30
vs(I,2)=vs(I,3)*Yv2(I)/Yv3(I)
vs(I,1)=0.
                                                             AA(J)=-VPB(I,J)
BB(J)=1.+D2(I,J)+E2(I,J)*VPC(I,J)
CC(J)=-VPT(I,J)
DD(J)=-VEC(I,J)*VB(I+1,J)+VEB(I,J)*VS(I+1,J-1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                CALCULATE PRESSURE CORRECTION FIELD.
                                                                                                                                                                                                                DD(JAV) =DD(JAV) -AA(JAV) +VS(I,JAVHI)
DD(JKAX) =DD(JKAX) -CC(JKAX) +VS(I,JPI)
CALL TRIDAG(JAV,JKAX,AA,BB,CC,DD,T)
DO 32 J=JAV,JKAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                COMPUTE SUM OF ABSOLUTE MASS SOURCE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     RESIGN-RESIGN+DARS(DS(I,J))
                        DO 30 IUV-1, ITUV
DO 31 J-JAV, JMAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       DO 35 J-JAP, JMAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 CC(J) =-BCV(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        DO 36 J-1,JP1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       PP(I-1,J)=0.

PP(I+1,J)=0.

CONTINUE
                                                                                                                                                                                                                                                                                              VS(I,J) "T(J)
                                                                                                                                                                                                                                                                                                                                                                                         CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   1-5
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CALCULATE THE PSEUDO VELOCITIES.
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DO 56 J=JA,JHAX
AA(J)=-TDPB(I,J)
BB(J)=1.+04(I,J)+(E4(I,J)-SDP(I,J))
BB(J)=1.+04(I,J)+(E4(I,J)-SDP(I,J))
BB(J)=TDPE(I,J)
CC(J)=-TDPE(I,J)+TDS(I+1,J+1)+TDEB(I,J)+TDS(I-1,J-1)
1 +TDEF(I,J)+TDS(I-1,J-1)+TDMT(I,J)+TDS(I-1,J)
2 +TDME(I,J)+TDS(I-1,J-1)+TDMT(I,J)+TDS(I-1,J)
DD(JA)=DD(JA)-AA(JA)+TDS(I-1,J+1)+TDMT(I,J)+TDS(I-1,J-1)
DD(JAA)=DD(JA)-AA(JA)+TDS(I,J-NA)
DD(JAA)=DD(JAA)-CC(JAAX)+TDS(I,J-NA)
DD(JAA)=DD(JAAX)-CC(JAAX)+TDS(I,J-NA)
DD(JAAX)-DD(JAAX)-CC(JAAX)+TDS(I,J-NA)
DD(JAA)-DD(JAAX)-TDS(I,J-NAX)
TDS(I,J-NAX)
TDS(I
                                                                                                                                                                                                                 AA(J)=TKPB(I,J)

BB(J)=1,+D3(I,J)+(E3(I,J)-SKP(I,J))*TKPC(I,J)

BC(J)=TKPT(I,J)

DD(J)=TKEC(I,J)*TKE(I+1,J)+TKEB(I,J)*TKE(I+1,J-1)

1 +TKET(I,J)*TKE(I+1,J+1)+TKWC(I,J)*TKE(I-1,J)

2 +TKPG(I,J)*TKE(I-1,J-1)+TKWT(I,J)*TKE(I-1,J)

DD(JA)=DD(JA)-AA(JA)*TKE(I,JAM1)

DD(JA)=DD(JA)-AA(JA)*TKE(I,JAM1)

DD(JA)=DD(JAA)-CC(JMAX)*TKE(I,JP1)

CALL TRIDAG(JA,JMAX,AA,BB,CC,DD,T)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      **********************************
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         CALCULATE TURBULENT DISSIPATION RATE FIELD.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 DO 54 J=A,JMAX

TKE(I,J)=T(J)

TKE(I,JP)=TKE(I,JMAX)

IF(I.LT.M2) GO TO 52

TKE(I,JA-1)=((YP4SQ(I)-YP2SQ(I))*TKE(I,JA)

- (YP4SQ(I)-YP3SQ(I))*TKE(I,JA+1))

Z / (YP4SQ(I)-YP3SQ(I))*TKE(I,JA+1))

TKE(I,JA-2)=(YP4SQ(I)*TKE(I,JA)-YP3SQ(I)*TKE(I,JA+1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   /(YP4SQ(I)-YP3SQ(I))
                                                                                                                                       DO 52 ITK=1,ITKD
DO 53 J=JA,JMAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               57
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      THUP-THU[I,J]

REFF=1./(REI*CEPS+THUP)

CALL SOUNCED

UU=0.5*(V0[I,J)+U0[I-1,J])*CEPS

VV=0.5*(V0[I,J-1)+V0[I,J])*CEPS

VV=0.5*(V0[I,J-1)+V0[I,J])*CEPS

FX=-0.5*(V0[I,J-1)+V0[I,J])*CEPS

FX=-0.5*(V0[I,J-1)+V0[I,J])*CEPS

FX=-0.5*(V0[I,J-1)+V0[I,J])*CEPS

FX=-0.5*(V0[I,J-1)+V0[I,J])*CEPS

FX=-0.5*(V0[I,J-1)+V0[I,J])*CEPS

FX=-0.5*(V0[I,J-1)+V0[I,J])*CEPS

FX=-0.5*(V0[I,J)*CEPS

FX=-0.5*(V
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 CALCULATE P-A COEFFICIENT OF TURBULENT DISSIPATION RATE.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          CALCULATE TURBULENT KINETIC ENERGY FIELD.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               E4(I,J)=CEPS*REFF*TAUI
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           E) (I,J) = CEPK*REFF*TAUI
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     TDEC([,J)~CF(3,2)
TDET([,J)~CF(3,3)
IF(IPA.EQ.2) THEN
O4(I,J)~TDMC(I,J)
ELSE
                                  TKPB [1, J) = CF(2, 1)
TKPC [1, J) = CF(2, 2)
TKPT [1, J) = CF(2, 3)
TKEB [1, J) = CF(3, 2)
TKEC [1, J) = CF(3, 2)
TKET [1, J) = CF(3, 2)
TKET [1, J) = CF(3, 3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 TDMB(I,J) = CF(1,1)
TDMC(I,J) = CF(1,2)
TDWT(I,J) = CF(1,3)
TDPB(I,J) = CF(2,1)
TDPC(I,J) = CF(2,2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       TDEB(1,3)-CF(3,1)
                                                                                                                                                                                                                                                                                                                                                                 D3 (I,J)-TKWC(I,J)
FKWT(I,J)=CF(1,3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      IF (IFA.EQ.2) THEN CALL COEFF2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            51 J~JA, JRAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         CALL COEFF3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        D4(I,J)=0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                             D3 (I, J) =0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               DR-2. *AR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ENO IF
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    END IF
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PI-Y

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DO 64 J=1,JP1 U(IP1,J)=U(IMAX,J) US(IPP,J)=U(IMAX,J) UO(IP1,J)=UO(IMAX,J) V(IP1,J)=VS(IMAX,J) VS(IP1,J)=VS(IMAX,J) VO(IP1,J)=VS(IMAX,J)

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PRINT 701, NITER, RESHM
FORMAT(3X, 'NO. OF ITERATION=',15,5X, 'RESHM=',2X,Ell.4)
PRINT SOME VARIABLES ON THE TERMINAL AND RETURN SPACE MARCHING PROCESS
                                                                                                                                                                                                                UPDATE THE PRESSURE FIELD BY GLOBAL ITERATIONS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                PRINT 9997, I,XU(I,1),UO(I,2),YPP,UTAUA(I)
FORMAT(3X,'I=',I3,2X,'X=',E11.4,2X,'U2=',E11.4,2X,
'YPLUS=',E11.4,2X,'UTAU=',E11.4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        FORMAT(/5x,'NO. OF ITERATION =',15,
5x,'Wall OR CENTERLINE PRESSURE')
WRITE(8,2009)(PR(I,1),I=2,IMAX)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 FORMAT(/5X, 'CENTERLINE VELOCITY')
WRITE(8,2009) (U0(I,1),I=M2,IMAX)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                FORMAT(/5X,'FRICTION VELOCITY')
WRITE(8,2009)(UTAUA(I),I=2,H2M1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        OUTPUT FOR EACH ITERATION
                                                                                                                                                                                                                                                                                                                                                                                                           WRITE(9,7010) NITER, RESMM FORMAT(3X,15,2X,E11.4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          WRITE(8,4111) NITER
                                                                                                                                                                                                                                                                                        RESMM=RESMM/FLOWIN
                                                                                                                                                                                                                                                                                                                                                                         STORE THE ERRORS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                WRITE(8,4112)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       WRITE(8,4113)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        CALL PRESS
                                                                                                                                                                 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                              7010
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             1111
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                                                                                                                 1666
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TKE(IPI,J)=TKE(IMAX,J)
TDS(IPI,J)=TDS(IMAX,J)
TKEO(IPI,J)=TKEO(IMAX,J)
TDSO(IPI,J)=TDSO(IMAX,J)
TNU(IPI,J)=TNU(IMAX,J)
END IF

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COMMON/PRES1/PRO(ID,JD), PP(ID,JD), PR(ID,JD)
COMMON/PRES2/CU(ID,JD), CV(ID,JD), CUY(ID,JD)
COMMON/PRES2/BCU(ID,JD), BCV(ID,JD), CUY(ID,JD)
COMMON/GEO1/XP(ID,JD), YP(ID,JD)
COMMON/MASS1/DH(ID,JD), VS(ID,JD)
COMMON/COMS1/IT,JJ, IMAX,JMAX, IP1,JP1,JAU,JAV,JAP,JA,MZ,HZHI
COMMON/CONSI/ITER,ITM,IEND,ITERA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         CALCULATE PRESSURE FIELD.
                                                                                                                                                       WRITE(7,2005)U0(1,3),V0(1,3),PR(1,3),TKE0(1,3),
TDSO(1,3),TNU(5,3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              FOR ELLIPTIC CALCULATION, IT IS NECESSARY
TO UNDERRELAX SEVERELY IN FIRST FEW ITERATIONS
DEPENDING ON THE BODY SHAPE.
WRITE(7,2009) (YU(I,1), I=1,IP1)
WRITE(7,2009) (PR(I,1), I=2,IMAX)
WRITE(7,2009) (UO(I,1), I=M2,IMAX)
WRITE(7,2009) (UTAUA(I), I=2,M2M1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           IF(IBODY.EQ.5) RFP=0.01
ELSE IF(NITER.LE.50) THEN
RFP=0.2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        IMPLICIT REAL*8(A-H,0-Z)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   PARAMETER (ID-142, JD-45)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  IF (NITER. LE. 30) THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         IF(IFA.EQ.2) THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         IF (IFA. EQ. 1) THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    COMMON/CONSB/IFA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               SUBROUTINE PRESS
                                                                                                                5001 J-1, IP1
5001 J-1, JP1
                                                                                                                                                                                                                           2005 FORMAT(6E12.4)
2009 FORMAT(6E12.4)
                                                                                                                                                                                                                                                                                                               CLOSE(7)
CLOSE(8)
CLOSE(9)
CLOSE(10)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 RFP=0.5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          RFP=0.1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       END IF
                                                                                                                                                                                                                                                                                                                                                                                                                            STOP
```

```
COMMON/GEO3/XU(1D,JD),YU(1D,JD)
COMMON/GEO4/XU(1D,JD),YU(1D,JD)
COMMON/VELL/U0(1D,JD),YU(1D,JD)
COMMON/VELL/U0(1D,JD),YU(1D,JD)
COMMON/VELL/U0(1D,JD),TKE0(1D,JD)
COMMON/TURBJ/TYE(1D,JD),TKE0(1D,JD)
COMMON/TURBJ/TYU(1D,JD),SV(1D,JD),SK(1D,JD)
COMMON/TURBJ/TYU(1D,JD),SV(1D,JD),SK(1D,JD)
COMMON/CONSILI,J,IMAX,JMAX,IPI,JPI,JAU,JAV,JAP,JA,M2,M2M1
COMMON/CONSILI,J,IMAX,JMAX,IPI,JPI,JPI,JAU,JAV,JAP,JA,M2,M2M1
COMMON/CONSS/RE,REI,TAU,TAUI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  XET=0.25*(XP(I,J+1)+XP(I+1,J+1)-XP(I,J-1)-XP(I+1,J-1))
YET=0.25*(YP(I,J+1)+YP(I+1,J+1)-YP(I,J-1)-YP(I+1,J-1))
XXI=XP(I+1,J)-XP(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      XET=0.5*(XV(I+1,3)+XV(I,3)-XV(I+1,3-1)-XV(I,3-1)
YET=0.5*(YV(I+1,3)+YV(I,3)-YV(I+1,3-1)-YV(I,3-1)
XXI=0.5*(XV(I+1,3)+XV(I+1,3-1)-YV(I,3)-YV(I,3-1)
XXI=0.5*(XV(I+1,3)+XV(I+1,3-1)-YV(I,3-1)
XXI=0.5*(XV(I+1,3)+XV(I+1,3-1)-YV(I,3)-YV(I,3-1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  SS=0.5*A12*(U0(1+1,J+1)+U0(I-1,J-1)-U0(I+1,J-1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    DVXI=0.5*(V(I+1,J)+V(I+1,J-1)-V(I,J)-V(I,J-1))
DVET=0.5*(V(I+1,J)+V(I,J)-V(I+1,J-1)-V(I,J-1))
DVX=AJI*(B11*DVXI+B12*DVET)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      YX]=YP(I+1,J)=YP(I,J)
CALL GEOCOE
INXI=TWU(I+1,J)=TWU(I,J)
TNET=0.25*(TMU(I,J+1)+TMU(I+1,J+1)=TNU(I,J-1)
DXXI=TRE(I+1,J)=TRE(I,J)
DXXI=TRE(I+1,J)=TRE(I,J)
DXXI=TRE(I+1,J)=TRE(I,J)
                                                                                                                                                                                                                                                                                                                                                                     COMMON/BODY1/B11,B12,B21,B22
COMMON/BODY2/G11,G12,G22,A11,A12,A22,G,AJI
COMMON/BODY3/XXI,YXI,XET,YET,R
                                                                                            COMMON/GEO1/XP(ID,JD),YP(ID,JD)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    YET=0.5* (YU(I,J+1) -YU(I,J-1))
XXI=0.5* (XU(I+1,J) -XU(I-1,J))
YXI=0.5* (YU(I+1,J) -YU(I-1,J))
CALL GEOCOE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       XET=0.5*(XU(I,J+1)-XU(I,J-1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     DUET=0.5*(U(I,J+1)-U(I,J-1))
DUY=AJI*(B21*DUXI+B22*DUET)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        TNUX=AJI* (B11*TNXI+B12*TNET
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  TNUY-AJI * (B21 * TNXI + B22 * TNET
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 DUXI=0.5*(U(I+1,J)-U(I-1,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           DKX=AJI*(B11*DKXI+B12*DKET)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     DUX=AJI* (B11*DUXI+B12*DUET
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         -U0(I-1,J+1))
IMPLICIT REAL*8(A-H,0-Z)
                                               PARAMETER (ID=142, JD=45)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  CALL GEOCOE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 U
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                U
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                                                                                                                                                                                                                                                                                                                                                                                                                                            Ç
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    AAAAAAA SOURCE FUNCTION OF U-VELOCITY...
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          PR(I,2)=((YP(I,4)-YP(I,2))*PR(I,3)-(YP(I,3)-YP(I,2))

*PR(I,4)/(YP(I,4)-YP(I,3))

PR(I,1)=((YP(I,4)-YP(I,3))-(YP(I,3)-YP(I,1))

*PR(I,4)-(YP(I,4)-YP(I,3))
                                                                                                                                                                                                                                                                                                                             DO 400 ITERG=1,20
DO 600 II=2,IMAX
I=IMAX+2=1I
DO 500 ITER=1,ITER=
DO 100 J=JAP,JMX
AA(J)=-BCV(I,J-1)
BB(J)=BCV(I,J)+BCV(I,J)+BCV(I,J-1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           DD(J)=BCU(I,J)*PR(I+1,J)+BCU(I-1,J)*PR(I-1,J)
1 -DH(I,J)
CALL TRIDAG(JAP,JMAX,AA,BB,CC,DD,T)
DO 200 J-JAP,JMAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             DO 700 J=1,JP1
PR(I,J)=PR0(I,J)+RFP*(PR(I,J)-PR0(I,J))
                                             IF(IBODY.EQ.5) RFP-0.1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       DO 501 J-1,JP1
501 PR(IP1,J)-PR(IMAX,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    SUBROUTINE SOURCEU
                                                                                                                                                                                                                                    DO 300 I=1,IP1
DO 300 J=1,JP1
PRO(I,J)=PR(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      PR(I,2)=PR(I,3)
PR(I,1)=PR(I,3)
END IF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         (1) =-BCV(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   IF (I.LT.M2) THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      DO 700 I=1, IP1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      200 PR(I,J)=T(J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   500 CONTINUE
600 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           400 CONTINUE
                                                                                                                                                                                         ITERP-10
                           RFP-0.2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 RETURN
                                                                        END IF
                                                                                                                     END IF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ELSE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          END
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   700
                                                                                                                                                                                                                                                                                    300
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                100
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            υ
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LT-A

IF (IBODY.EQ.5) RFP=0.05

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COMMON/GEO1/XP(ID,JD),YP(ID,JD)
COMMON/GEO3/XU(ID,JD),YV(ID,JD)
COMMON/GEO4/XU(ID,JD),YV(ID,JD)
COMMON/GEL1/U(ID,JD),YV(ID,JD)
COMMON/YEL1/U(ID,JD),Y(ID,JD)
COMMON/TURB1/TKE(ID,JD),TKE(ID,JD)
COMMON/TURB1/TKE(ID,JD),TKE(ID,JD)
COMMON/TURB3/TNU(ID,JD)
COMMON/TURB3/TNU(ID,JD)
COMMON/TURB4/TGE(ID,JD)
COMMON/TURB3/TNU(ID,JD),SP(ID,JD)
COMMON/STLN/SRF(ID,JD),SPE(ID,JD)
COMMON/STLN/SRF(ID,JD),SPE(ID,JD)
COMMON/CONSJ/LJ,IMAX,JMAX,IPI,JPI,JAU,JAV,JAP,JA,HZ,HZHI
COMMON/CONSJ/CHEFF CALCULATE SOURCE FUNCTION OF KINETIC ENERGY FIELD. XXI=YU(I,J)-YU(I-1,J)
XET=0.25\*(XU(I,J+1)+XU(I-1,J+1)-XU(I,J-1)-XU(I-1,J-1)
YET=0.25\*(YU(I,J+1)+YU(I-1,J+1)-YU(I,J-1)-YU(I-1,J-1)
CALL GEOCOE DUET=0.25\*(U(I,J+1)+U(I-1,J+1)-U(I,J-1)-U(I-1,J-1)) SS=0.5\*A12\*(VO(I+1,J+1)+VO(I>1,J-1)-VO(I+1,J-1)
-VO(I-1,J+1)) COMMON/BODY1/B11, B12, B21, B22 COMMON/BODY2/G11, G12, G22, A11, A12, A22, G, AJI COMMON/BODY3/XXI, YXI, XET, YET, R SV(I,J)=SS+REFF\*(TNUX\*(DVX+DUY) +2.\*TNUY\*DVY-2./3.\*DKY)-VO/R/R

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	COMMON/TURB3/TNU(ID,JD)
XET=XV(I,3)-XV(I,3-1)	COMMON/TURBA/TGE(ID,JD)
XXI=0.25+(X(I+1,J)+XV(I+1,J-1)-XV(I-1,J)-XV(I-1,J-1)) XXI=0.25+(XV(I+1,J)+XV(I+1,J-1)-YV(I-1,J-1))	COMMON/STAT/SO(IN), SO(IN), SD(IN), SD(IN), SO(IN), SV(IN), SD(IN), SV(IN), SD(IN), SV(IN), SD(IN), SV(IN), SV
CALL GEOCOS  DVFT-V(T I)-V(T I)-)	COMMON / CONST, TITLE, TOTAL CEPS1, CEPS2, CEPK, CEPS, CKAR, E
DVXI-0(1,0)-v(1,0)-v(1,0)-1) DVXI-1:25*(v(1+1,0)+v(1+1,0-1)-v(1-1,0)-v(1-1,0-1)) DVX-AJI:25*(v(1+1,0)+v(1+1,0-1)-v(1-1,0-1)) DVY-AJI:25*(v(1+1,0)+v(1+1,0-1)-v(1-1,0-1))	COMMON/BODYS/REFF COMMON/BODYS/BII, BI2, B21, B22 COMMON/BODY2/GII, GI2, G22, AII, A12, A22, G, AJI COMMON/BODY3/XXI, YXI, XET, YET, R
XXI=0.5*(XP(I+1,J)-XP(I-1,J))	
XXI=0.5e(YP(I+1,J)-XP(I+1,J) XYT=0.5e(XP(I,J+1)-XP(I,J+1) XYT=0.5e(YP(I,J+1)-XP(I,J+1))	R=YP(I,J) XXI=XU(I,J) -XU(I-1,J) YXI=YU(I,J) -YU(I-1,J)
CALL GEOCOE DERT-0.5*(TKE(1,J+1)-TKE(1,J-1))	XET=0.25*(XU(I,J+1)+XU(I-1,J+1)-XU(I,J-1)-XU(I-1,J-1) YET=0.25*(YU(I,J+1)+YU(I-1,J+1)-YU(I,J-1)-YU(I-1,J-1))
TWET=0.5*(TMU(I,J+1)-TMU(I,J-1)) DXXI=0.5*(TRE(I+1,J)-TKE(I-1,J))	CALL GEOCOE DUET=0.25*(U(1,3+1)+U(I-1,3+1)-U(I,3-1)-U(I-1,3-1))
TMXI=0.5e(TNU(I+1,J)-TNU(I-1,J)) DKX=AJI*(BII*DKXI+BI2*DKET)	DUXI=U(I,J)-U(I-1,J) DUX=AJI*(B11*DUXI+B12*DUET)
DKY=AJI*(B21*DKXI+B22*DKET) TWUY=AJI*(B21*TKXI+B22*TKET)	DUY-AJI*(B21*DUXI+B22*DUET) C
Thux=Aji+(bii+Thxi+bi2+Thet)	XET=XV(I,J)-XV(I,J-1) YET=VV(I,J)-YV(I,J-1)
88-0.5*A12*(TXE0(I+1,J+1)+TXE0(I-1,J-1)-TXE0(I+1,J-1) 1	XXI=0.25*(XV(I+1,J)+XV(I+1,J-1)-XV(I-1,J)-XV(I-1,J-1))
R-YP(I,J)	CALL GEOCOE  DVET=V(I,J)-V(I,J-1)
VO=0.5*(V(I,J)+V(I,J-1))	DVXI=0.25*(V(1+1,3)+V(1+1,3-1)-V(1-1,3)-V(£-1,3-1)) DVX=ATT*(R1)*DVYT*R13*DVPP1
TGE(I,J)=TNU(I,J)*(2.*DUX*DUX+2.*DVY*DVY+ 1	DVY-AJI*(B21*DVXI+B22*DVET)
	XXImO.5*(XP(I+1,J)-XP(I-1,J)) XXImO.5*(YP(I+1,J)-YP(I-1,J))
SKP(I,J)	XET=0.5+(XP(I,J+1)-XP(I,J+1) XET=0.5+(YP(I,J+1)-YP(I,J+1))
1 +CEPK*REFF*(TNUX*DKY+TNUX*DKX)	CALL GEOCOE DEFINE RATIOS (1 141) - FDS (1 1-1)
RETURN	TNET=0.56 (TNU(I,J-1)) TNET=0.56 (TNU(I,J-1)) DEXI=0.56 (TDS(I+J-1)-TNU(I,J-1))
	TNXI=0.5*(TNU(I+1,3)-TNU(I-1,3))
bedatharadestrockerstockerstockerstockerstockerstockerstockers Caldings Acids Principa Of Dissipation Desp	DEY-A1 (011 - 011 - 011)  DEY-A1 (011 - 011 - 011)  FULLY-A1*(01) + 011 - 011
	TNUX=AJI+(B11*TNXI+B12*TNET)
SUBROUTINE SOURCED	SS=0.5*A12*
IMPLICIT REAL*8(A-H,O-2)	(1101-1)0001-
PARAMETER (ID=142,JD=45)	R=YP(I,J) VO=0.5+(V(I,J)+V(I,J-1))
COMMON/GEOL/XP(ID,JD), YP(ID,JD)	TGE(I,J) -TNU(I,J) *(
COMMON/GEOJ/XV(ID,JD),YV(ID,JD) COMMON/GEO4/XV(ID,JD),YV(ID,JD)	1 (DVX+bUY)**2+2.*(VO/R)**2) C
COMMON/VELL/U0(ID,JD),V0(ID,JD) COMMON/VEL4/U(ID,JD),V(ID,JD)	ADK~TDS(I,J)/TKE(I,J) SDP(I,J)=-ADK*CEPS*REFF*CEPS2
COMMON/TURBL/TKE(ID, JD), TKE0(ID, JD) COMMON/THIRDS/TDS (TD, JD), TDSO(ID, JD)	SD(I,J)=SS+CEPS*REFF*CEPS1=TCE(I,J)*TDS(I,J)/TKE(I,J)

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COEFF3 FOR CALCULATING 9-PIONT FINITE-ANALYTIC COEFFICIENTS OF TRANSPORT EQUATIONS-OLD VERSION.
IMPLICIT DOUBLE PRECISION (A-H,O-Z)
COMMON/COEF7/CF(3,3)
COMMON/FA1/AR, BR, DR, ER, FR
COMMON/COMS3/EMAX, FWAX, EPE1, PI
                                                                                                                                                                                                                  HAX-12
DAR-DHAX1 (DABS (AR), EPE)
DBR-DHAX1 (DABS (BR), EPE)
AR-DSIGN (DAR, AR)
                                                                                                BUBROUTINE COEFF3
                                                                                                                                                                                                                                                                                             BR-DSIGN(DBR, BR)
AR-AR/ER
BR-BR/FR
                                                                                                                                                                                                U
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SUBMOUTINE COEFT? FOR CALCULATINGPARTIALLY PARABOLIC FINITE ANALYTIC COFFICIENTS OF TRANSPORT EQUATIONS ADDRESSES ANALYTIC COFFICIENTS OF TRANSPORT EQUATIONS
                                                                                                                                                                                  IMPLICIT DOUBLE PRECISION (A-H,0-Z)
COMBON/COET/CF(3,3)
COMBON/FAL/AR,BR,BR,BR,ER,FR
COMBON/COM3/EMAX,FWAX,EPE,EPE1,PI
IP(DABS(BR).LT.EPE) GO TO 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                      TANHB-(EPBK-EPBKI)/(EPBK+EPBKI)
CF(2,3)=EPBKI/(EPBKI+EPBK)
CF(2,2)=TANHB/(2.*BRO)
CF(2,1)=EPBK/(EPBKI+EPBK)
GO TO 2
                                                                                                                                                                                                                                                                                                          BR-BR/FR
HY-1./FR
BK-BR-HY
BR-DR-IN (DABS (BK), FMAX)
BK-DSIGN (DBK, BK)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 CF(1,2)-CF(2,2)*DR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           CF(2,1)=0.5
CF(2,2)=0.5/FR/FR
CF(2,3)=0.5
                                                                                                                                                                    SUBROUTINE CORFF2
                                                                                                                                                                                                                                                                                                                                                                                                                                          epbki=1./epbk
                                                                                                                                                                                                                                                                                                                                                                                                                   EPBK-DEXP (BK)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             CF(3,1)=0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          CONTINUE
RETURN
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IF(DMAX1(DAH, DBK).GE.EMAX) GO TO 120

COTHA COSHA/SINHA COTHB COTHB SINHB

SINHA-EPAH-EPAHI SINHB-EPBK-EPBKI COSHA-EPAH-EPAHI COSHB-EPBK+EPBKI

./EPBK

EPBKI-1

EPAH=DEXP(AH) EPBK=DEXP(BK) EPAHI=1./EPAH

IF(HX.GT.HY) GO TO 21

PWR=1.

DAH=DMIN1(DABS(AH), FMAX) DBK=DMIN1(DABS(BK), FMAX) AH=DSIGN(DAH, AH)

AB2-AR\*AR+BR\*BR

AK-AR\*HY BK=BR\*HY

FR2=FR4FR AH-AR\*HX BH-BR\*HX

HY=1./FR ER2=ER\*ER

BK-DSIGN (DBK, BK)

AH2-AH\*AH BK2=BK+BK

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AB=DEXP(DSQRT(AB2+ZA2*FR2)*HX)

EY2=EY2-PWR*ZA/((AB+1./AB)*(BK2+ZA2)*(BK2+ZA2))

PB=2.*BK*COTHB*COSHA*COSHB*EY2

PA=1.+AK*COTHA/(BH*COTHB)*(PB-1.)
                                                                                                             EX2=EX2-PWR*ZA/((AB+1./AB)*(AH2+ZA2)*(AH2+ZA2))
PA=2.*AH*COTHA*COSHA*COSHB*EX2
PB=1.+BH*COTHB/(AK*COTHA)*(PA=1.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Q-DAK/(AB1+DBH)
IF(DAK.GT.DBH) Q-DBH/(AB1+DAK)
PA-1.-(1.+Q)*AK*COTHA/(AK*COTHA+BH*COTHB)
                                                                                                                                                                                         CF(2,2)=0.5*HX/(AR*COTHA)*(1.-PA)
                                                                                                                                                                                                                                                                                                                                                                                                                     CF(2,2)=0.5+HX/(AR+COTHA)+(1.-PA)
                                                                                          ab=dexp (dsqrt (ab2+za2*er2) *hy)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              AB1=A1+A1+HY/HX+B1+B1+HX/HY
DAK=DABS(AK)
EX2-0.
DO 10 M-1, MAX
ZA-(M-0.5)*PI
ZA2-ZA*ZA
                                                                                                                                                                                                                                                DO 20 N=1, MAX
ZA=(M-0.5) *PI
                                                                                                                                                                                                                                                                                                                                                                                                                                                            A1-AH/SINHA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     DBH-DABS (BH)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                               B1=BK/SINHB
                                                                                                                                                                        Q=1.-PA-PB
                                                                                                                                                                                                                                                                                                                                                                                                   Q-1.-PA-PB
                                                                                                                                                                                                          GO TO 160
                                                                                                                                                                                                                                                                                    242-242A
                                                                                                                                                                                                                                                                                                                                                                                                                                          GO TO 160
                                                                           PWR -- PWR
                                                                                                                                                                                                                                                                                                        PWR=-PWR
                                                                                                                                                                                                                              EY2=0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                            120
                                                                                                                                                                                                                                                                                                                                             20
                                                                                                                 2
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PB=1.-PA-Q

CF(2,2)=0.5*HX/(AR*COTHA)*(1.-PA)

160 BE=PRAH/COSHA

BN=EPRAH/COSHA

BN=EPRAH/COSHB

CF(1,1)=BN*BR*Q

CF(1,1)=BN*BR*Q

CF(1,1)=BN*BR*Q

CF(1,1)=BN*BR*Q

CF(1,2)=BN*PR

CF(1,2)=BN
```

C CALCULATE THE GEOMETRIC CONSTANTS.

C CALCULATE THE GEOMETRIC CONSTANTS.

C SUBROUTINE GEOCOB

C IMPLICIT REAL\*8 (A-W, 0-2)

COMMON/BODY1/B11, B12, B21, B22

COMMON/BODY1/B11, B12, B21, B22

COMMON/BODY2/B11, B12, B21, B22

COMMON/BODY2/S11, S12, B21, B22

IMPLICIT REAL=8(A-H, O COMMON/BODY1/B11, B12, COMMON/BODY2/G11, G12, COMMON/BODY3/XXI, YXI, B11-R\*YET B12-R\*XI B21-R\*XI G11-XXI\*XXI\*YXI\*YXI G11-XXI\*XXI\*XXI

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and THE BASIC FEATURE OF THIS CODE. THIS PROGRAM CALCULATES PAST AXISYMETRIC BODIES \*
• USING THE K-E TURBULENCE MODEL AND WALL FUNCTION \*
• METHOD WITH A SPACE MARCHING TECHNIQUES. BODY-FITTED COORDINATE USING PARTIAL TRANSFORMATION ( CARTESIAN, CYLINDRICAL BASE COORDINATE. ) COMMON/PRESI/FR(ID,JD), PP(ID,JD), PRO(ID,JD)
COMMON/PRESI/CXUE(ID,JD), CYUE(ID,JD)
COMMON/PRESI/CXVM(ID,JD)
COMMON/PRESI/CXVM(ID,JD)
COMMON/PRESI/CYVM(ID,JD)
COMMON/PRESI/CYVM(ID,JD)
COMMON/PRESI/CYVM(ID,JD)
COMMON/PRESI/CYVM(ID,JD)
COMMON/GEOC/XC(ID,JD), SPR(ID,JD)
COMMON/GEOC/XC(ID,JD), YP(ID,JD)
COMMON/GEOC/XC(ID,JD), YR(ID,JD)
COMMON/GEOL/YE(ID,JD), YR(ID,JD)
COMMON/GEOL/YE(ID,JD), YR(ID,JD)
COMMON/GEOL/YE(ID,JD), YR(ID,JD)
COMMON/GEOL/YE(ID,JV,YM(ID)
COMMON/GEOL/YE(ID,JV,YM(ID),YR(ID)
COMMON/GEOL/YE(ID,JV,YM(ID),YR(ID)
COMMON/GEOL/YE(ID,JV,YM(ID),YR(ID)
COMMON/GEOL/YE(ID,JV,YM(ID),YR(ID)
COMMON/GEOL/YE(ID,JV,YM(ID),YR(ID)
COMMON/GEOL/YE(ID,JV,YM(ID),YR(ID),YR(ID)
COMMON/GEOL/YE(ID,JV,YM(ID),YR(ID),YR(ID)
COMMON/GEOL/YE(ID,JV,YM(ID),YR(ID),YR(ID)
COMMON/GEOL/YE(ID,JV,YM(ID,JV) ONE-VELOCITY STAGGERED GRID SYSTEM SIMPLER NUMERICAL ALGORITHM (A-H,0-Z) SPACE MARCHING TECHNIQUE. \* PROGRAMMED BY S.K.CHOI IMPLICIT DOUBLE PRECISION CHARACTER\*10 F2NAME(10) CHARACTER\*10 F3NAME(10) CHARACTER\*10 F4NAME(10) CHARACTER\*10 F5NAME(10) CHARACTER\*10 FINAME(10) Parameter (ID-142, JD-45) PROGRAM HAWKEYE U U

COMMON/VELS/VO(ID, JD)
COMMON/TURB1/AKE(ID, JD), ADS(ID, JD)
COMMON/TURB1/AKE(ID, JD), ADS(ID, JD)
COMMON/TURB1/AKE(ID, JD), ADS(ID, JD)
COMMON/TURB1/AKE(ID, JD), SPUR(ID, JD)
COMMON/STZ/SCVN(ID, JD), SPUR(ID, JD)
COMMON/STZ/SCVN(ID, JD), SPUR(ID, JD)
COMMON/STZ/SCVN(ID, JD), SPUR(ID, JD)
COMMON/STS/SUKD(ID, JD), SPUR(ID, JD)
COMMON/COEF1/AEE(ID, JD), APUE(ID, JD), ANE(ID, JD)
COMMON/COEF1/AEE(ID, JD), APUE(ID, JD), ANE(ID, JD)
COMMON/COEF1/AEE(ID, JD), ANE(ID, JD), ANE(ID, JD)
COMMON/COEF1/AEN(ID, JD), ANE(ID, JD), ANE(ID, JD)
COMMON/COEF1/AEN(ID, JD), ANE(ID, JD), AND(ID, JD)
COMMON/COEF6/ASN(ID, JD), AND(ID, JD), AND(ID, JD)
COMMON/CONSI/IMAK, JMAK, JMAK, JNAK, NESNA, NESNA
COMMON/CONSI/RENUM, DENSIT, VISCOS, PRANDT
COMMON/CONSI/RENUM, DENSIT, VISCOS, PRANDT
COMMON/CONSI/RENUM, DENSIT, VISCOS, PRANDT
COMMON/CONSI/RENUM, DENSIT, VISCOS, PRANDT F2NAME(1)/'hfvalol'/,F2NAME(2)/'hfva2ol'/, F2NAME(3)/'hfva3ol'/,F2NAME(4)/'hfva4ol'/, F2NAME(5)/'hfva5ol'/,F2NAME(6)/'hfva6ol'/ F3NAME(1)/'hfvalo2'/,F3NAME(2)/'hfva202'/, F3NAME(3)/'hfva302'/,F3NAME(4)/'hfva402'/, F3NAME(5)/'hfva602'/,F3NAME(6)/'hfva602'/ F4NAME(1)/'hfvalo3'/,F4NAME(2)/'hfvato3'/, F4NAME(3)/'hfva303'/,F4NAME(4)/'hfvato3'/, F4NAME(5)/'hfva503'/,F4NAME(6)/'hfva603'/ F5NAME(1)/'hfvalo4'/,F5NAME(2)/'hfva204'/, F5NAME(3)/'hfva304'/,F5NAME(4)/'hfva404'/, F5NAME(5)/'hfva504'/,F5NAME(6)/'hfva604'/ FINAME(1)/'halbdat'/,FINAME(2)/'ha2bdat'/,FINAME(3)/'ha3bdat'/,FINAME(4)/'ha4bdat'/,FINAME(6)/'ha5bdat'/ COMMON/CONS7/NITER, MAXIT, ITMAX, NINER, ITOUT COMMON/CONS9/CMU, CD, C1, C2, ELOG, CAPPA, PRTE, PRED COMMON/CONS9/PI, GREAT DATA DATA DATA DATA 000000000000 U ပ U U U

AXISYMMETRIC BODIES.

COMMON/VEL2/VN(ID,JD) COMMON/VEL3/UHE(ID,JD) COMMON/VEL4/VHN(ID,JD)

MAIN PROGRAM

SS-A

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ES-A

C PRESSURE CORRECTION EQUATION.	BCU(I,J)=0.D0 BCV(I,J)=0.D0	C SOURCE TERMS.	C FOR VELOCITY, UE.	SCUE(I,J)=0.D0 SPUE(I,J)=0.D0	C FOR VELOCITY, VN.	SCVN(I,J)=0.D0 SPVN'I,J)=0.D0	C FOR KINETIC ENERGY, AKE.		SUKD(1,3)=0.DO SPKD(1,3)=0.DO	C FOR DISSIPATION RATE, ADS.	SCD(1,1)=0.D0		C FOR PRESSURE AND PRESSURE CORRECTION EQUATION.		C 14 CONTINUE	C seessessesses		FLOWIN=0.DO ARDEN=0.DO ARDENT=0.DO	XMONIN=0.D0	UTAUA(1)=0.038 DELTAX=0.006 DELTAIDELTAX	C UE(1,1)=0.0	VN(1,1)=0.0 AKE(1,1)=0.0 ARE(1,1)=0.0		C YY=YE(1, J) -YE(1, 1)
Do 119 J=1, JP1	DO 12-1 1P1	120 VOL(1,1)=0.00		GET VALABLES TO LEKO.	DO 14 I=1, IP1	WALL SURFACE VELOCITY  VSF(1)=0.D0	DO 14 J=1,JP1	CARTESIAN ( OR CYLINDRICAL ) VELOCITY COMPONENTS.	UE(I,J)=0.DO VN(I,J)=0.DO		c pseudo-velocity components.	UHE(I,J)=0.D0 VHN(I,J)=0.D0	C PRESSURE, PRESSURE CORRECTION FIELD.	PR(I,J)=0.D0 PRO(I,J)=0.D0 PP(I,J)=0.D0	C KINETIC EMERGY AND DISSIPATION RATE.	AKE(1,J)=0.D0 ADS(1,J)=0.D0	C DENSITY AND VISCOSITY		C COEFFICIENTS OF PRESSURE TERM IN		CYUE(I,J)=0.D0	CXVN(I,J)=0.D0 CYVN(I,J)=0.D0	QXUE(I,J)=0.D0 QYVN(I,J)=0.D0	C COEFFICIENTS OF PRESSURE AND

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RETURN POINT OF SPACE MARCHING PROCESS.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         GO TO 19
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               YE2SQ=YE2(I)*YE2(I)
YE3SQ=YE3(I)*YE3(I)
YE4SQ=YE4(I)*YE4(I)
YN2SQ=YN2(I)*YN3(I)
YN3SQ=YN3(I)*YN3(I)
YN4SQ=YN3(I)*YN3(I)
YP2SQ=YP2(I)*YP2(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               IF (NITER.EQ.1) THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        AKE(I,J)=AKE(I-1,J)
ADS(I,J)=ADS(I-1,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         UTAUA(I)=UTAUA(I-1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      AKE(I+1,J)=AKE(I,J)
ADS(I+1,J)=ADS(I,J)
                                                                                                                                                                        DO 19 J=1,JP1
DO 21 I=1,IP1
SPP(I,J)=0.D0
PP(I,J)=0.D0
VN(I,J)=VN(2,J)
VN(I,J)=VN(2,J)
AKE(I,J)=AKE(2,J)
ADS(I,J)=ASS(2,J)
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               UE(I+1,J)=UE(I,J)
VN(I+1,J)=VN(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       U0(I+1,J)=UE(I,J)
V0(I+1,J)=VN(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             VN(I,J)=VN(I-1,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    UO(1,3)=UE(I-1,3)
VO(1,3)=VN(I-1,3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                UE(I,J)=UE(I-1,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     DO 3000 I=2, IMAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      J=1, JP1
                          RESAK-0.
RESAD-0.
RESMM-0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CONTINUE
RESVN=0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 END IF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   DO 23
                                                                                                                                                                                                                                                                                                                                                                                                                                                   19
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    23
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ARDEN-DEN(1,J) *0.5*(R(1,J)+R(1,J-1)) *(YC(1,J)-YC(1,J-1))
XHONIN-XHONIN-ARDEN*UE(1,J)*UE(1,J)
ARDENT-ARDENT-ARDEN
TLOHIN-FLOWIN-ARDEN*UE(1,J)
UMEAN-FLOWIN/ARDEN*U
                                                                                                                                                   UE(1,J)=1.02=EIA++0.143
IF(EIA-GE.1.) UE(1,J)=1.02-0.02*(EIA-1.)/(EIAH-1.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ELSE IF(YPLUS.LE.DPLUS) THEN
UE(1,J)=UTAUA(1)*(2.5*DLOG(YPLUS)+5.5
+ 0.5*2./CAPPA*(DSIN(PI/2.*YY/DELTAX))**2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   AKE(1,J)=UTAUA(1)*UTAUA(1)*(1.D0=ETA)/(CHU**0.5)
IF(ETA.GE.1.) AKE(1,J)=1.D-8
ADS(1,J)=(CHU**0.75)*AKE(1,J)**1.5/(CAPPA*Y)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Annabathannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannanahannahannanahannanahannanahannanahannanahannanahannanahannanahannahannanahannanahannanahannanahannanahannanahannanahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannahannaha
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ELSE IF(YPLUS.LE.50.) THEN
UE(1,J)=UTAUA(1)*(5.D0*DLOG(YPLUS)-1.05D0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  COMPUTE INLET MEAN VELOCITY, MASS FLUX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ELSE IF(YPLUS.LE.1000.) THEN
UE(1,J)=UTAUA(1)*(2.5*DLOG(YPLUS)+5.5)
ETAM*(YE(1,JP1)-YE(1,1))*DELTAI
                                                                                                                                                                                                                                          DPLUS-DELTAX*RENUM*UTAUA(1)
IF(DPLUS-LE.1000.) DPLUS-1001.
                                                                                            1/7TH LAW FOR U-VELOCITY
                                                                                                                                                                                                                                                                                                                              YPLUS-RENUM*YY*UTAUA(1)
                                                                                                                                                                                                                                                                                                                                                                                         IF(YPLUS.LE.S.) THEN
UE(1,J)-UTAUA(1)*YPLUS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            AND MOMENTUM PLUX.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       UHE(1,3)=UE(1,3)
UO(1,3)=UE(1,3)
VN(1,3)=0.DO
VO(1,3)=0.DO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   DO 201 J=2, JHAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            4000 NITER-NITER+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            UE(1,3)=1.
END IF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      RESUE=0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ELSE
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	C AMARAMAMAMAMAMAMAMAMAMAMAMAMAMAMAMAMAMA
CALCULATE THE EFFECTIVE EDDY VISCOSITY assessessessessessessessessessessessesse	C NORTH CELL SURFACE VELOCITIES.
DO 240 J=2,JP1	C DO 380 J=3,JMAX
VISOLD-VIS(I, 3)	COMPUTE
IF(ADS(I,J).EQ.0.D0) GO TO 241	C FOR EAST CONTROL VOLUME SURFACE
VIS(I,J)=CMU*DEN(I,J)*AKE(I,J)*AKE(I,J)/ADS(I,J) 1 +VISCOS	
GO TO 242	NG*K(1,J) B11E*E(1,J+1)-YE(1,J) B12E*E(1,J+1)-YE(1,J)
241 VIS(I,J)=VISCOS	B21E=-(XI(1,0+1,0)) B21E=-(YI(1+1,0)-YI(1,0)) B22E=YI(1+1,1)=YI(1,0)
UNDER-RELAX VISCOSITY	D1E=RE*RE*(B11E*B12E*B12E) D12E=RE*RE*(B11E*B12E*B12E)
242 VIS(I,J)=URFVIS*VIB(I,J)+(1.D0-URFVIS)*VISOLD	
240 CONTINUE	C FOR WEST CONTROL VOLUME SURFACE
DO 244 J=4,JP1 IF(VIS(I,J=1).LE.VIS(I,J=2).AND.VIS(I,J=1).LT. 1 VIS(I,J) VIS(I,J)=VIS(I,J-1) 244 CONTINUE.	EMER(I-1,J) Blim=YE(I-1,J+1)-YE(I-1,J) Blim=Y(XE(I-1,J+1)-XE(I-1,J) Blim=(YE(I-1,J+1)-XE(I-1,J)) Blim=(Y(I,J)-Y(I-1,J)) Blim=(Y(I,J)-X(I-1,J))
ALONG THE BOTTOM WALL AND SYMMETRY LINE.	DIIW-RW-RW-RW-(BIIW-BIIW-BI2W) DIZW-RW-RW-(BIIW-BI2W-BI2W-BI2W-
IF(I.GE.M2) VIS(I,1)=VIS(I,2) IF(I.LT.M2) VIS(I,1)=VISCOS	VOLM=0.25*(VOL(I-1,J)+VOL(I-1,J+1)+VOL(I,J)+VOL(I,J+1)) C FOR NORTH CONTROL VOLUME SURFACE
INLET AND OUTLET CONDITIONS	
IF(I.EQ.2) THEN DO 26 J=1,JP1 26 VIS(1,J)=VIS(2,J) END IF	B11N=YN(I,J+1)-YN(I,J) B12N=-(XN(I,J+1)-YN(I,J) B21N=-(YN(I,J+1)-XN(I,J)) B21N=-(YN(I,J+1)-YN(I,J+1)) B21N=-(YN(I,J+1)-YN(I,J+1)) B21N=-(YN(I,J+1)-YN(I,J+1)) B21N=-(YN(I,J+1)-YN(I,J+1)-YN(I,J+1))
261 VIS(IP1,J)=VIS(IMAX,J) END IF	C FOR SOUTH CONTROL VOLUME SURFACE
IF(NITER.EQ.1) THEN DO 262 J=1,JP1 262 VIS(I+1,J)=VIS(I,J) END IF	RS=0.25*(R(I-1,J)+R(I-1,J-1)+R(I,J)+R(I,J-1)) B11S=YN(I,J)-YN(I,J-1) B12S=(NN(I,J)-YN(I,J-1)) B12S=(NN(I,J)-YN(I,J-1)) B22S=XE(I,J)-XE(I-1,J))
270 CONTINUE	D21S=RS*RS*(B11S*B21S*B12S*B22S) D22S=RS*RS*(B21S*B21S+B22SS*B22S)
entertantententententententententententententen	
C. 1971-176 FOLTS. CF LEGICE. L. ECALLION. Betsebesesesesesesesesesesesesesesesesese	C FOR CENTER POINT
	RP=0.5*(R(I,J)+R(I-1,J))

YP3SQ=YP3(I) +YP3(I) YP4SQ=YP4(I) +YP4(I)

<b>\$3</b> \$2		AEN(I,J)=DMAX1(DABS(0.5D0*FE),DE)-0.5D0*FE AWN(I,J)=DMAX1(DABS(0.5D0*FW),DW)+0.5D0*FW
<b>a</b> a :	B21P=- (YC(I,J)-YC(I-1,J)) B22P=XC(I,J)-XC(I-1,J)	COEFFICIENTS OF PRESSURE TERM IN MOMENTUM EQUATION
	VOLET-U-5" (VOL(1,0)+VOL(1,0+1))	CXVN(I,J)=RP#B12P CVVN(I,J)=RP#R22P
	COMPUTE CELL SURFACE VALUES	SHORT STATES OF STATES WITH THE CONDITIONS OF STATES
	UNN=0.5*(UE(I,J+1)+UE(I-1,J+1)) VNN=0.5*(VN(I,J)+VN(I,J+1))	
	USS=0.5*(UE(I,J)+UR(I-1,J)) VSS=0.5*(VN(I,J)+VN(I,J-1))	DVDX=RF=(B11F=(VEE-VWW)+B21F=(VNN-VSS))/VOLF DKDX=RF=(B11F=(AKEE-AKWW)+B21F=(AKNN-AKSS))/VOLF DVIDX=RF=(B11F=(VIEE-VIWW)+B21F=(VINN-VISS))/VOLF
	UEE=0.5*(UE(I,J)+UE(I,J+L)) VEE=0.5*(VN(I,J)+VN(I+1,J))	DUDY=RP*(B12P*(UEE-UWW)+B22P*(UNN-USS))/VOLP
	UWM=0.5*(UE(1-1,J)+UE(1-1,J+1)) VWW=0.5*(VN(1,J)+VN(1-1,J))	DVIDY=RP*(B12P*(VIEE-VIWW)+B22P*(VINN-VISS))/VOLP
<b>4444</b> U (	AKNN-AKE(I,J) AKSS-AKE(I,J) AKEE-0.25¢(AKE(I,J)+AKE(I,J+1)+AKE(I+1,J+1)+AKE(I+1,J) AKMM-0.25¢(AKE(I-1,J)+AKE(I-1,J+1)+AKE(I,J+1)+AKE(I,J))	DVNDEE-0.25*(VN( DVNDEW-0.25*(VN( DVNDKN-0.25*(VN(
	VISS=VIS(I,J+) VISS=VIS(I,J) VISS=VIS(I,J) VISS=VIS(I,J) VISSION (VIS(I,J+VIS(I,J+1)+VIS(I+1,J+1)+VIS(I+1,J)) VINDE OF OFFICE (I,J+VIS(I+1,J+1)+VIS(	DVNDKS=0.25*(VN(I-1,J-1)-VN(I-1,J)  1
, paaa		SBVNE-VIEF*D12E/VOLE*DVNDEE SBVNW-VIWW*D12W/VOLM*DVNDEW SBVNW-VIWN*D11W/VOLM*DVNDEW SBVNW-VIWN*D11W/VOLM*DVNDKN
o o o		SBVN=SBVNE-SBVNW+SBVNN-SBVNS
	FN=DENN*RN*(B21N*UNN+B22N*VNN)  FN=DESS*RS*(B21S*USS*B2S*VSS)  FN=DEEE*RS*(B11E*UEE*B12E*VEE)  C	COMPUTE SOURCE FUNCTIONS SORCVN=DVIDX*DUDY*DVDY-2./3.*DKDY
υυ.	FW=DEWW*RW*(B11M*UWW+B12M*VWW)  COMPUTE DIPPUSION COEFFICIENTS  C	SCVN(I,J)=CPO*VN(I,J)+SORCVN*VOLP+SBVN
	DN-VINN+D22N/VOLN	SPVN(I,J)=-CP
-		IF(ICORD.EQ.2) THEN SPVN(I,J)=SPVN(I,J)
	COMPUTE COEFFICIENTS OF SOURCE TERM	1 -0.5*(VIS(I,J)+VIS(I,J+1))*VOLP/RP/RP END IF
	SMP=FN-FS+FE-FW CP-DMAX1(0.D0,SMP)	380 CONTINUE
. <b>.</b> 	ASSEMBLE MAIN COEFFICIENTS	CONSIDER THE BOUNDARY CONDITIONS
	ANN(I,J)=DMAX1(DABS(0.5D0*FN),DN)-0.5D0*FN CASN(I,J)=DMAX1(DABS(0.5D0*FS),DS)+0.5D0*FS	OUTLET CONDITION

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VINN-0.25D0*(VIS(I,J)+VIS(I,J+1)+VIS(I+1,J)+VIS(I+1,J+1)
VISS-0.25D0*(VIS(I,J)+VIS(I,J-1)+VIS(I+1,J)+VIS(I+1,J-1)
VIEE-VIS(I+1,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 AKNN=0.25*(AKE(I,J)+AKE(I,J+1)+AKE(I+1,J+1)+AKE(I+1,J))
AKSS=0.25*(AKE(I,J-1)+AKE(I,J)+AKE(I+1,J)+AKE(I+1,J-1))
AKEE=AKE(I+1,J)
                                                                                                                                                                                                                                                                                                                    D22N=RN*RN*(B21N*B21N+B22N)
VOLN=0.25*(VOL(I,J)+VOL(I,J+1)+VOL(I+1,J+1)+VOL(I+1,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            VOLS=0.25*(VOL(I,J-1)+VOL(I,J)+VOL(I+1,J)+VOL(I+1,J-1))
                                                                                                                                                                                                                                                                                                                                                                                                                          RS=R(I,J-1)
B11S=YE(I,J)-YE(I,J-1)
B12S=-(XE(I,J)-XE(I,J-1))
B21S=-(YN(I+1,J-1)-YN(I,J-1))
B22S=XN(I+1,J-1)-XN(I,J-1))
D21S=RS*RS*(B11S*B21S*B22S)
D22S=RS*RS*(B21S*B21S*B22S*B22S)
                B21W=-(YE(I,J)-YE(I-1,J))
B22W=XE(I,J)-XE(I-1,J)
D11W=RW=RW=KW=(B11W*B11W+B12W*B12W)
VOLW=VOL(I,J)
                                                                                                                                                                                         RN=R(I,J)
Blin=YE(I,J1)-YE(I,J)
Blin=-(XE(I,J1)-XE(I,J))
B2ln=-(XE(I,J1)-XE(I,J))
B2ln=-(X(I+1,J)-XN(I,J))
D2ln=XN(I+1,J)-XN(I,J)
D2ln=RN*RN*(Blin*B2ln*B12N*B22N)
                                                                                                                                                                                                                                                                                                                                                                                   FOR SOUTH CONTROL VOLUME SURFACE
                                                                                                                                                    FOR NORTH CONTROL VOLUME SURFACE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      UEE=0.5*(UE(1,J)+UE(1+1,J))
VEE=0.5*(VN(1+1,J)+VN(1+1,J-1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        USS=0.5*(UE(I,J)+UE(I,J-1))
VSS=0.5*(VN(I,J-1)+VN(I+1,J-1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          VOLP=0.5*(VOL(1,J)+VOL(1+1,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  COMPUTE CELL SURFACE VALUES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         UNN=0.5*(UE(I,J)+UE(I,J+1))
VNN=0.5*(VN(I,J)+VN(I+1,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     UWW=0.5*(UE(I,J)+UE(I-1,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          VWW-0.5*(VN(I,J)+VN(I,J-1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              RP=0.5*(R(I,J)+R(I,J-1))
B11P=*XC(I,J)-YC(I,J-1)
B12P=-(XC(I,J)-XC(I,J-1))
B21P=-(YP(I+1,J)-YP(I,J))
B22P=*YP(I+1,J)-YP(I,J)
B12W=-(XN(I,J)-XN(I,J-1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        FOR CENTER POINT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  AKWW-AKE(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             000
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                                                                                                                                 000
                                                                                                                                                                                                                                                                                                                                                                  000
                                                                                                                                                                                                                                                                                 APVN(I,J)=ANN(I,J)+ASN(I,J)+AEN(I,J)+AWN(I,J)-SPVH(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        CALCULATE THE COEFFICIENTS AND SOURCE TERMS FOR EAST CALCULATE THE COEFFICIENTS AND SOURCE TERMS FOR THE CHARACTER OF THE COEFFICIENTS AND SOURCE TERMS FOR THE COEFFICIENT OF THE COEFFICIENT OF THE COEFFICIENT OF THE CO
                                                                                                                                                                      FINAL CORFF ASSEMBLY AND RESIDUAL SOURCE FOR UN
                                                                                                                                                      IF(-SPVN(I,J).GT.0.5*SORVOL) RESOR-RESOR/SORVOL RESVN-RESVN+DABS(RESOR)
                                                                                                                                                                                                                                                                                                                      RESOR-ANN(I,J) *VN(I,J+1) +ASN(I,J) *VN(I,J-1)
+AEN(I,J) *VN(I+1,J) +AWN(I,J) *VN(I-1,J)
-APVN(I,J) *VN(I,J) +SCVN(I,J)
+CXVN(I,J) *0.25 * (PR(I-1,J+1) +PR(I-1,J)
-PR(I+1,J+1) -PR(I+1,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           RE=0.25*(R(I+1,J)+R(I+1,J-1)+R(I,J-1)+R(I,J))
B11E=YN(I+1,J)-YN(I+1,J-1)
B12E=-(XN(I+1,J)-XN(I+1,J-1))
B21EE--(YE(I+1,J)-YE(I,J))
B22E=XE(I+1,J)-YE(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            RW=0.25*(R(I,J)+R(I,J-1)+R(I-1,J-1)+R(I-1,J))
B11W=YN(I,J)-YN(I,J-1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           SCVN(I,J)=SCVN(I,J)
\ +(I.Do-URFV)/URFV*APVN(I,J)*VN(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                 +CYVN(I,J)*(PR(I,J)-PR(I,J+1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   D11E=RE*RE*(B11E*B11E+B12E*B12E)
D12E=RE*RE*(B11E*B21E+B12E*B22E)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    FOR EAST CONTROL VOLUME SURFACE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       FOR WEST CONTROL VOLUME SURFACE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                          VOLP=0.5*(VOL(I,J)+VOL(I,J+1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          COMPUTE GEOMETRIC CONSTANTS
                         IF(I.EQ.IMAX) THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  SORVOL-GREAT * VOLP
                                       DO 381 J=3,JMAX
AEN(IMAX,J)=0.D0
END IF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     UNDER-RELAXATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  DO 280 J-3, JMAX
                                                                                                                                                                                                                                         DO 384 J=3,JMAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           VOLE=VOL(I+1,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           384 CONTINUE
                                                                    381
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ပပပ
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CONSIDER THE BOUNDARY CONDITIONS
                                                                                                                                                                                                                                                 SORCUE=DVIDX*DUDX+DVIDY*DVDX-2./3.*DKDX
                                                                                                                                                                                                                                                                                           SCUE(I, J) = CP0 * UE(I, J) + SORCUE * VOLP + SBUE
SOURCE FUNCTION BY NON-ORTHOGONALITY.
                                                                                                                                                          SBUE-SBUEE-SBUEW+SBUEM-SBUES
                                                                SBUEW=VIWW*D12W/VOLM*DUEDEW
SBUEN=VINN*D21N/VOLN*DUEDKN
SBUES=VISS*D21S/VOLS*DUEDKS
                                            SBUEE=VIEE*D12E/VOLE*DUEDEE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                TOP FREE STREAM BOUNDARY.
                                                                                                                                                                                                    COMPUTE SOURCE FUNCTIONS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  IF(I.EQ.IMAX) THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    DC 281 J=3,JMAX
AEE(IMAX,J)=0.D0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      OUTLET CONDITION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             UE(I, JP1)=1.D0
                                                                                                                                                                                                                                                                                                                                       SPUE(I,J)=-CP
                                                                                                                                                                                                                                                                                                                                                                                   CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    END IF
                                                                                                                                                                                                                                                                                                                                                                                     280
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             O
                                            DENN=0.25*(DEN(I,J)+DEN(I,J+1)+DEN(I+1,J)+DEN(I+1,J+1))
DESS=0.25*(DEN(I,J)+DEN(I,J-1)+DEN(I+1,J)+DEN(I+1,J-1))
DEEE=DEN(I+1,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           COEFFICIENTS OF PRESSURE TERM IN MOMENTUM EQUATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  DUDX-RP*(B11P*(UEE-UWM)+B21P*(UNN-USS))/VOLP
DVDX-RP*(B11P*(VEE-WWM)+B21P*(VNN-VSS))/VOLP
DVDX-RP*(B11P*(VEE-AKW)+B21P*(AKNN-AKSS))/VOLP
DVIDX-RP*(B11P*(VIEE-VIWW)+B21P*(VINN-VISS))/VOLP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              DUDY=RP*(B12P*(UZE-UWM)+B22P*(UNN-USS))/VOLP
DUDY=RP*(B12P*(VZE-VWM)+B22P*(VMU-VSS))/VOLP
DVDY=RP*(B12P*(VZE-AKWM)+B22P*(AKNN-AKSS))/VOLP
DVIDY=RP*(B12P*(VIZE-VWW)+B22P*(VINN-VISS))/VOLP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ANE (I, J)=DMAXI (DABS (0.5D0*FN), DN)-0.5D0*FN
ASE (I, J)=DMAXI (DABS (0.5D0*FS), DS)+0.5D0*FS
AEE (I, J)=DMAXI (DABS (0.5D0*FE), DE)-0.5D0*FE
AME (I, J)=DMAXI (DABS (0.5D0*FW), DW)+0.5D0*FW
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        COMPUTE DERIVATIVE VALUES FOR SOURCE TERMS.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             DUEDEE=0.25*(UE(I+1,J+1)+UE(I,J+1)
-UE(I+1,J-1)-UE(I,J-1)
DUEDEE=0.25*(UE(I-1,J+1)+UE(I,J+1)
-UE(I-1,J-1)-UE(I,J-1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               DUEDKS=0.25*(UE(I+1,J-1)+UE(I+1,J)
-UE(I-1,J-1)-UE(I-1,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              DUEDKN-0.25*(UE(I+1,3+1)+UE(I+1,3)
-UE(I-1,3+1)-UE(I-1,3))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                COMPUTE COEFFICIENTS OF SOURCE TERM
                                                                                                                                                                                                                                 FS=DESS*RS*(B11S*UEE+B12E*VEE)
FE=DEEE*RE*(B11E*UEE+B12E*VEE)
                                                                                                                                                                                                                                                                           FW=DEWW+RW+ (BILW+UWW+BI2W+VWW)
                                                                                                                                                                                                           FN=DENN+RN+ (B21N+UNN+B22N+VNN)
                                                                                                                                                                                                                                                                                                                       COMPUTE DIFFUSION CORFFICIENTS
                                                                                                                                                               COMPUTE CONVECTION MASS FLUX.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ASSEMBLE MAIN COEFFICIENTS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          SMP=FN-FS+FE-FW
CP=DMAX1(0.D0,SMP)
                                                                                                                                                                                                                                                                                                                                                                                        DS=VISS*D22S/VOLS
DE=VIEE*D11E/VOLE
DW=VIWW*D11W/VOLW
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CXUE(I,J)-RP+B11P
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           CYUE(I,J)-RP+B21P
                                                                                                                                                                                                                                                                                                                                                                    DN-VINN*D22N/VOLN
      (I'I)SIN-MMIN
                                                                                                                       DEWM-DEN(I,J)
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APUE(I,J)=ANE(I,J)+ASE(I,J)+AEE(I,J)+AWE(I,J)-SPUE(I,J)
FINAL COEFF ASSEMBLY AND RESIDUAL SOURCE FOR UF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        IF(-SPUE(I,J).GT.0.5*SORVOL) RESOR=RESOR/SORVOL RESUE=RESUE+DABS(RESOR)
                                                                                                                                                                                                         RESOR-ANE(I,J) *UE(I,J+1) +ASE(I,J) *UE(I,J-1)
+AEE(I,J) *UE(I+1,J) +AWE(I,J) *UE(I-1,J)
-AUE(I,J) *UE(I,J) +SCUE(I,J)
+CXUE(I,J) *(PR(I,J) +PR(I+1,J))
+CXUE(I,J) *0.25*(PR(I,J-1) *PR(I+1,J-1)
i
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           SCUE(I, J) = SCUE(I, J)
+(1.DO-URFU)/URFU*APUE(I, J)*UE(I, J)
                                                                                                                                                                                                                                                                                                                                                                                                         VOLP=0.5*(VOL(I,J)+VOL(I+1,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                              SORVOL-GREAT * VOLP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           UNDER-RELAXATION
                                                                                                    DO 283 J-3, JMAX
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v

000

A22=RW\*RW\*GI\*G11 A12=-RW\*RW\*GI\*G12 All-RW\*RW\*GI\*G22

GI=1./G

B12=-RW\*YXI B21=-RW\*XET B22-RW\*XXI

Ç

B11=RW\*YET

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DG11=DSQRT(G11) AJI \*DSQRT(GI)

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UTAU-UTAUA(I)

U

U

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U3=UE(I,3)

U

00000

283 CONTINUE

ပ UU IF(I.EQ.M2M1) THEN

RW-YC(I,1)

DO 285 ITUV-1, NSWPU DO 286 J=3, JMAX AA(J)=-ASE(I,J)	C FOR SOUTH CONTROL VOLUME SURFACE
285 ITUV=1,NSWPU 286 J=3,JNAX J=-ASE(I.J)	rok south control velone
\frac{1}{2} \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	RS=0.5*(R(I-1,J-1)+R(I,J-1)) B21S=-(YC(I,J-1)-YC(I-1,J-1))
BB(J) =APUR(I,J)/URFU	
CC(J) = -ANE(I,J) $DD(J) = AEE(I,J) + UE(I+1,J) + ANE(I,J) + UE(I-1,J) + SCUE(I,J)$	C COMPUTE FACE DENSITIES.
+CAUE(1,J)*(FAL,J)*FR(1+1,J-1) +CYUE(1,J)*0.25*(FL,J-1)*PR(1+1,J+1)*PR(1+1,J+1)	DENN=0.5D0*(DEN(I,J)+DEN(I,J+1)) DESS=0.5D0*(DEN(I,J)+DEN(I,J-1))
DD(3)=DD(3)=AA(3)*UE(1,2) DD(JMAX)=DD(JMAX)=CC(JMAX)*UE(1,JMAX+1)	DEEE=0.5D0*(DEN(I,J)+DEN(I+1,J) DEWW=0.5D0*(DEN(I,J)+DEN(I-1,J)
CALL TRIDAG(3,JHAX, AA, BB, CC, DD, T)	C COMPUTE CONVECTION MASS FLUX.
DO 287 J=3,JWAX UE(I,J)=T(J)	FN=DENN*RN*B22N*VN(I,J) FS=DESS*RS*B22S*VN(I,J-1) FE=DEEE*RE*B11E*UE(I,J)
IF(I.II.H2) GO TO 285	FW=DEWW*RW*BLIW*UE(I-1,J)
UE(I,2)=((YE4SQ-YE2SQ)+UE(I,3)-(YE3SQ-YE2SQ)+UE(I,4))	
/(Ye4sq-Ye3sq) UE(I,1)=(Ye4sq=Ve(I,3)-Ye3sq*Ue(I,4)) /(Ye4sq-Ye3sq)	UNN=0.25D0*(U0(I,J)+U0(I,J+1)+U0(I-1,J)+U0(I-1,J+1) USS=0.25D0*(U0(I,J)+U0(I,J-1)+U0(I-1,J)+U0(I-1,J-1) VEE=0.25D0*(V0(I,J)+V0(I,J-1)+V0(I+1,J)+V0(I+1,J-1)
CONTINUE	VMM=0.2500*(V0(1,3)+V0(1,3-1)+V0(1-1,3)+V0(1-1,3-1) C
	FN=DENN*RN*B21N*UNN FS=DESS*RS*B21S*USS FE=DEEE*RE*B12E*VEE
ANTEREST THE MASS SOURCE FOR PRESSURE CORRECTION	FW=DEWW+RW+B12W+VWW
CCCATIONS	
	100 - 200 - 100 -
DO 480 J™3,JMAX	C COMPUTE SUM OF ABSOLUTE MASS SOURCE
COMPUTE GEOMETRIC CONSTANTS	RESHM-RESHM+DABS(SPP(I,J))
FOR EAST CONTROL VOLUME SURFACE	C COMPUTE COEFFICIENTS OF PRESSURE C AND PRESSURE CORRECTION.
RE=0.5*(R(I,J)+R(I,J-1)) B11E=YC(I,J)-YC(I,J-1) R11E=-(XC(I,J)-XC(I,J-1))	QXUE(I,J)=URFU*RE*B11E/APUE(I,J) QYVN(I,J)=URFV*RN*B22N/APVN(I,J)
FOR WEST CONTROL VOLUME SURFACE	BCU(I,J)=DEEE*RE*BllE*QXUE(I,J) BCV(I,J)=DENN*RN*B22N*QYVN(I,J)
RN-0.5*(R(I-1,J)+R(I-1,J-1)	C 480 CONTINUE
B12H=-(XC(I-1,J)-XC(I-1,J-1))	
FOR NORTH CONTROL VOLUME SURFACE	
RN=0.5*(R(I=1,J)+R(I,J))	

EE-A

ALONG THE BOTTOM WALL AND SYMMETRY LINE.

CO

	COMPUTE GEOMETRIC CONSTANTS	
C	FOR EAST CONTROL VOLUME SURFACE	CALCULATE THE COEFFICIENTS AND SOURCE FUNCTIONS FOR TURBULENCE KINETIC ENERGY
		AND DISSIPATION RATE EQUATIONS.
BII	RE=0.5+(I,J)+R(I,J=1)) C BllE=VC(I,J)-YC(I,J=1) C	
		- 1
C TOR	FOR WEST CONTROL VOLUME SURFACE	DO 580 J=3,JMAX
		COMPUTE GEOMETRIC CONSTANTS
	B11M=YC(1-1,J)-YC(1-1,J-1)	FOR EAST CONTROL VOLUME SURFACE
n C	FOR NORTH CONTROL VOLUME SURPACE	RE=0.5*(R(I,J)+R(I,J-1)) BllE=YC(I,J)-YC(I,J-1)
	0.5*(R(I-1.J)+R(I.J))	B12E=-(XC(I,J)-XC(I,J-1))
821	B21N(YC(I,J)-YC(I-1,J))	B22E=XP(I+1,J)-YP(I,J)
	. (p'1-1)-xc(1-1)	DIIE=RE*RE* (BIIE+BIIE+BI2E*BI2E)
S C C	FOR SOUTH CONTROL VOLUME SURFACE	VOLE=0.5*(VOL(I,J)+VOL(I+1,J))
	RS=0.5*(R(I=1,J=1)+R(I,J=1))	FOR WEST CONTROL VOLUME SURFACE
B21 B22		
		XX#C.5#(K(L+1,C)+K(L+1,C+1)) B]]%#YC(I+1,J)-YC(I+1,J+1)
<b>X</b> 00	COMPUTE PACE DENSITIES.	B12W=-(XC(I-1,J)-XC(I-1,J-1))
	N=0.5D0*(DEN(I,J)+DEN(I,J+1))	B22W=XP(I,J)-YP(I-1,J) B22W=XP(I,J)-XP(I-1,J)
DES	DESS=0.5D0*(DEN(1,J)+DEN(1,J-1)) DEEE=0.5D0*(DEN(1,J)+DEN(1+1,J)	DIIW=RW*RW*(BIIW*BIIW+BI2W*BI2W)
		VOLM=0.5*(VOL(I,J)+VOL(I-1,J))
NOO O	COMPUTE CONVECTION MASS FLUX.	FOR NORTH CONTROL VOLUME SURFACE
	FM=DENN*RN*B22M*VHN(1.3)	CH TATT (TIME OF ORRE
-S4	FS-DESS*RS*B22S*VHR(I,J-1)	B11N=YP(I,J+1)-YP(I,J)
	FW-DEWWARM-BLIN-CHE(I-1,J)	B12N=-(XP(I,J+1)-XP(I,J)) B21N=-(XC(I,J)-YC(I-1,J))
S	76 - 66 * 66 * 76 * 75	B22N-XC(I,J)-XC(I-1,J)
S. S	**************************************	D2IN=RN*RN*(B11N*B21N+B12N*B22N) D22N=RN*RN*(B21N*B21N+B22N)
NEO I	J) +U0(I, -1, J+1))	VOLN=0.5*(VOL(I,J)+VOL(I,J+1))
227	VEE-0.25500* (C(1,0) * VC(1,0-1) * VC(1+1,0) * VC(1+1,0-1) C	FOR SOUTH CONTROL VOLUME SURFACE
U	7)+40(1-1,3-1))	RS=0.5*(R(1-1.1-1)+R(1.1-1))
	FN-DEXX & RN & B21X & UNX	B11S=YP(1,J)-YP(1,J-1)
	TRIDERARE AND RAVER	B12S=-(XP(1,J)-XP(1,J-1)) B21S=-(YC(1,J-1)-YC(1-1,J-1))
- NA.	fw=dewv=rr=bl2v=vnv	B228=XC(I,J-I)-XC(I-1,J-I)
	SNP=FN-FS+FE-FW	D215=K5*K5*(B115*B215+B128*B225) D225=R5*R5*(B215*B215+B225*B225)
	SPR(I,J)=SMP+SMP	VOLS=0.5*(VOL(I,J-1)+VOL(I,J))
C 493 COR	CONTINUE	FOR CENTER POINT
υc		RP=0.25*(R(I,J)+R(I-1,J)+R(I-1,J-1)+R(I,J-1))
,		B11P=YN(I,J)-YN(I,J-1)

C UNDER-RELAXATION	APK(1, J) = APK(1, J) / URFK  CCK(1, J) = APK(1, J) / URFK	C C CONTINUE	3			AA(J) = -ASK(I,J) BB(J) = APK(I,J) CC(J) = -ANK(I,J)	585	C DD(3)=DD(3)=AA(3)*AKE(I,2) DD(JHAX)=DD(JHAX)-CC(JHAX)*AKE(I,JHAX+1)	CALL TRIDAG(3, JMAX, AA, BB, CC, DD, T)	DO 586 J=J,JMAX S86 AKE(I,J)=T(J)	C AKE(I,JHAX+1)=AKE(I,JHAX)	IF(I.LT.M2) GO TO 584	AKE(I,2)=((YP4SQ-YP2SQ)*AKE(I,3)-(YP3SQ-YP2SQ)*AKE(I,4))  1 /(YP4SQ-YP3SQ)	AKE(I,1) = (YP4SQ+AKE(I,3) - YP3SQ+AKE(I,4) $1 / (YP4SQ-YP3SQ)$	C ARE(1,2)=ARE(1,3) C ARE(1,1)=ARE(1,3)	584 CONTINUE	C FINAL COEFF ASSEMBLY AND RESIDUAL SOURCE FOR ADS C SARABBANASABA	C DO 683 J=3,JMAX	APD(I,J)-AND(I,J)+ASD(I,J)+AED(I,J)+AWD(I,J)-SPD(I,J) RESOR-AND(I,J)*ADS(I,J+1)*ASD(I,J)*ADS(I,J-1) 1 +AED(I,J)*ADS(I+1,J)+AMD(I,J)*ADS(I-1,J) 2 -APD(I,J)*ADS(I,J)+SCD(I,J)	C VOLP-VOL(I,3)	SORVOL-GREAT*VOLP IF(-SPD(1,J).GT.0.5*SORVOL) RESOR-RESOR/SORVOL RESAD=RESAD+DABS(RESOR)
END IF	COMPUTE SOURCE FUNCTIONS	C FOR KINETIC ENERGY EQUATION.	SCK(I,J)=CPO*AKE(I,J)+SBAKE SUKD(I,J)=SCK(I,J) SCK(I,J)=SCK(I,J)	SPK(I,J)=CP SPK(I,J)=SPK(I,J)	-	C C For dissipation rate equation.		SCD(I,J)=SCD(I,J) SCD(I,J)=SCD(I,J) 1 +DEN(I,J)=C1*GEN(I,J)*ADS(I,J)*VOLP/AKE(I,J)	SPD(I,J)=-CP SPD6(I,J)=SPD(I,J)	SPD(1,J)=SPD(1,J) 1 -C2*DEN(1,J)*ADS(1,J)*VOLP/AKE(1,J)	SSO CONTINUE	CONCINED THE PATHWEST CONTINUES.	CONTROL AND ECONOMIS (CONTROL OF A PROPERTY	ALONG THE OUTI	IF(I.EQ.IMAX) THEN DO 582 J=3,JWAX AEK(IMAX J=0.DO		There is a second of the secon	DO 563 J=3,JWAX	APK(I,J)=ANK(I,J)+ASK(I,J)+AEK(I,J)+AWK(I,J)-SPK(I,J) RESOR=ANK(I,J)+AKE(I,J+1)+ASK(I,J)*AKE(I,J-1) 1 +AEK(I,J)*AKE(I+1,J)+AWK(I,J)*AKE(I-1,J) 2 -APK(I,J)*AKE(I,J)+SCK(I,J)	VOLP-VOL(1,3)	SORVOL-GREAT+VOLP IF(-SPK(I,J).GT.O.S+SORVOL) RESOR-RESOR/SORVOL RESAR-RESAK+DABS(RESOR)

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UNDER-RELAXATION

'YPLUS=', E11.4,2X,'UTAU=',E11.4)

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outeur Apres Calculation
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 WRITE(8,12)MITER, I, XP(I,1), URFU
12 FORMAT(//5X, 'NO. OF ITERATION =', I3,5X,'STATION', I3
1,5X,'X =',F8.4,5X,'U-RF =',F6.3)
                                                                                                                                                                                                                                                                                                                                                                                                                                    WRITE(8, 2097) URFU, URFV, URFD, URFVIS, URFPR FORMAT(//5%, 'RELAXATION FACTORS(U, V, K, E, VIS, PR)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   3001 FORMAT(//5X,'Y-CORD',6X,'VEL U',7X,'VEL V',6X,
1'TURB KE',5X,'TURB DIS',3X,'PRESSURE'//)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            2098 WRITE(8,2099) UTAUA(I),CFS(I)
2099 FORMAT(5X,'UTAU=',E12.4,5X,'TAUM=',E12.4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 DO 3003 J-1,JP1
3003 WRITE(8,2007) YP(I,J),UE(I,J),VN(I,J)
1 ,AKE(I,J),ADS(I,J),PR(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    WRITE(7,2009)(XP(I,1),1-1,IP1)
WRITE(7,2009)(XE(I,1),I-1,IP1)
WRITE(7,2009)(YP(I,1),I-1,IP1)
WRITE(7,2009)(YN(I,1),I-1,IP1)
WRITE(7,2009)(PR(I,1),I-2,IMAX)
WRITE(7,2009)(UE(I,1),I-2,IMAX)
WRITE(10,2009) (UTAUA(I), I=2, M2M1)
                                          WRITE(10, 2009) (UE(I,1), I-M2, IMAX)
                                                                                                                                               IF(NITER.GE.MAXIT) GO TO 702
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             SAVE DATA FOR PLOTTING.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      IF(I.GE.M2) GO TO 2222
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         DO 3333 I-1, IPA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               2117 FORMAT(4E12.4)
2007 FORMAT(6E12.4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 6F6.3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           2222 WRITE(8,3001)
                                                                                                                                                                                              GO TO 4000
                                                                                                                                                                                                                                      702 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       3333 CONTINUE
                                                                                    END IF
                                                                                                                                                                                                                                                                                                                                                                                                                                                         2097
                                                                                                                                                                                                                   v
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       PROVIDE DATA FOR CONVERGENCE HISTORY
                                                                                                                                                                                                                                                                                                                                                OUTPUT FOR EACH ITERATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         IF (NITER. EQ. 1.0R.NITER. EQ. 20.0R.NITER. EQ. 50.0R.
NITER. EQ. 100.0R.NITER. EQ. 150.0R.NITER. EQ. 200.
OR.NITER. EQ. 300) THEN
                                          DO 9999 I=1,IP1
DO 9999 J=1,JP1
9999 PR(I,J)=PRO(I,J)+URFPR*(PR(I,J)-PRO(I,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              DO 4999 1=1, IP1
DO 4999 J=1, JP1
IF(DABS(PR(I,J)).GT.10.D0) GO TO 5555
IF(DABS(UE(I,J)).GT.10.D0) GO TO 5555
                                                                                                                                                                                                                     SELECT NUMBER OF ITERATION FOR OUTPUT
                                                                                                                                                                                                                                                                                                                                                                                                                                                         WRITE(8,4111) NITER
FORMAT(/5x,'NO. OF ITERATION =',15,
15x,'WALL OR CENTERLINE PRESSURE')
WRITE(8,2009)(PR(1,1),1=2,IMAX)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 WRITE(0,4113)
FORMAT(/5X,'CENTERLINE VELOCITY')
WRITE(6,2009)(UE(1,1),L=M2,IMAX)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 WRITE(8,4112)
FORMAT(/5X, 'FRICTION VELOCITY')
WRITE(8,2009) (UTAUA(I), I=2,M2M1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               WRITE(10,2009) (PR(I,1),I-2,IMAX)
                                                                                                                                                                                                                                                             ITPRINT=MAXIT-ITOUT
IP(NITER.LE.ITPRINT) GO TO 6666
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                WRITE(10,4114) NITER
FORMAT(/5X,15)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        CHECK FOR OVERFLOW
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           6666 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CONTINUE
  4001 CONTINUE
                                                                                                                                1234 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      4114 )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    4999
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        4112
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             4113
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             U
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PARAMETER(JD=45)
DIMENSION A(JD), B(JD), C(JD), D(JD), V(JD), BETA(JD), GAMMA(JD)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               SUBROUTINE PRESU(F, DHS, I, M)
IMPLICIT DOUBLE PRECISION (A-H, O-Z)
PARAMETER(ID-142, JD-45)
DIMENSION P(ID, JD)
DIMENSION DHS(ID, JD)
COMMON/PRESE/BCU(ID, JD), BCV(ID, JD)
COMMON/AAA/AA(JD), BB(JD), CC(JD), DD(JD), T(JD)
COMMON/CONSI/IMAX, JNAX, IPI, JPI, M2, M2M1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        DO 660 J=3,JMAX
AA(J)=-BCV[I,J-1)
BB(J)=BCU(I,J,J)*M+BCU(I,J)+BCV(I,J-1)
1 BCV(I,J)
CC(J)=-BCV(I,J)
CC(J)=-BCV(I,J)
660 DD(J)=BCU(I,J)*P(I+1,J)+BCU(I-1,J)*P(I-1,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                BETA(IF)=B(IF)

GANMA(IF)=D(IF)/BETA(IF)

IFPL=IF+1

DO 1 I=IFPL, L

BETA(I)=B(I)-A(I)*C(I-1)/BETA(I-1)

1 GANMA(I)*(D(I)-A(I)*CAMMA(I-1)/BETA(I)

LAST=L-IF

DO 2 K=1, LAST
                                        DO 5001 [=1,IP]
DO 5001 J=1,JP]
5001 WRITE(7,2005)UE(1,J),VN(1,J),PR(1,J)
1 ,AKE(1,J),ADS(1,J),VIS(1,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                      IMPLICIT DOUBLE PRECISION (A-H, 0-Z)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    V(I)-GAMMA(I)-C(I)*V(I+1)/BETA(I)
RETURN
END
                                                                                                                                                                                                                                                                                                                                                                                                                 SUBROUTINE TRIDAG(IF, L, A, B, C, D, V)
WRITE(7,2009) (UTAUA(I), I=2, H2H1)
                                                                                                                                  2005 FORMAT(6E12.4)
2009 FORMAT(6E12.4)
                                                                                                                                                                                                                                               CLOSE(7)
CLOSE(8)
CLOSE(9)
CLOSE(10)
                                                                                                                                                                                                            5555 CONTINUE
C
                                                                                                                                                                                                                                                                                                                                               STOP
                                                                                                                                                                                                                                                                                                                                                                END
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Ų
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0.530000E+00 0.510000E+00 0.610000E+00 0.650000E+00 0.770000E+00 0.770000E+00 0.850000E+00 0.950000E+00 0.970000E+00 0.970000E+00 0.105000E+01 0.105000E+01 0.105000E+01 0.105000E+01 0.105000E+01 0.105000E+01 0.105000E+01 0.45600E-01 0.45600E-01 0.45600E-01 0.45200E-01 0.44700E-01 0.44700E-01 0.36200E-01 0.36200E-01 0.36200E-01 0.36200E-01 0.376200E-01 0.72400E-01 0.72400E-01 calculation 0.520000E+00 0.560000E+00 0.640000E+00 0.720000E+00 0.720000E+00 0.800000E+00 0.800000E+00 0.920000E+00 0.920000E+00 0.920000E+00 0.104000E+01 0.124499E+01 0.124499E+01 0.124499E+01 0.124499E+01 0.456000E-01 0.456000E-01 0.455000E-01 0.49200E-01 0.435600E-01 0.435600E-01 0.379200E-01 0.378200E-01 0.275000E-01 0.275000E-01 0.2750000E-01 geometric data for half body using two-layer model 0.510000E+00 0.550000E+00 0.530000E+00 0.630000E+00 0.710000E+00 0.750000E+00 0.790000E+00 0.870000E+00 0.950000E+00 0.950000E+00 0.950000E+00 0.107000E+01 .456000E-01 .455000E-01 .455000E-01 .455000E-01 .455000E-01 .439600E-01 .346800E-01 .394600E-01 .239400E-01 .239400E-01 "falbody" 600000000000000 0.500000E+00 0.540000E+00 0.540000E+00 0.700000E+00 0.700000E+00 0.700000E+00 0.700000E+00 0.940000E+00 0.940000E+00 0.940000E+00 0.940000E+00 0.940000E+00 0.940000E+00 0.940000E+00 0.940000E+00 0.940000E+00 0.102000E+01 0.133939E+01 0.133939E+01 0.133939E+01 0.133939E+01 0.133939E+01 0.133939E+01 0.133939E+01 0.145000E-01 0.450000E-01 0.45000E-01 0.45100E-01 0.45100E-01 0.45100E-01 0.45100E-01 0.45100E-01 0.45100E-01 0.45100E-01 0.45100E-01 0.45100E-01 0.37200E-01 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 £110 000000

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.856000E+0	.864000E+0	.872000E+0	. 880000E+0
.888000E+0	.896000E+0	.904000E+0	.912000E+0
.920000E+0	.928000E+0	.936000E+0	.944000E+0
.952000E+0	.960000E+0	.968000E+0	.976000E+0
.984000E+0	.992000E+0	.100000E+0	.100800E+0
.101600E+0	.102400E+0	.103200E+0	.104000E+0
.104800E+0	.105600E+0	.106400E+0	.107200E+0
.108160E+0	.109312E+C	.110694E+0	.112353E+0
.114344E+0	.116733E+0	.119599E+0	.123039E+0
.127167E+0	.132120E+0	.138064E+0	.145197E+0
.153757E+0	.164028E+0	.176354E+0	.191144E+0
.208893E+0	.230192E+0	.255750E+0	.286420E+0
.32322E+0	.367389E+0	.420387E+0	.483985E+0
.560302E+0			
.456000E-0	.456000E-0	.456000E-0	.456000E-0
.456000E-0	0.456000E-01	456000E-	-300095
.456000E-0	.456000E-0	.456000E-0	.456000E-0
.456000E-0	.456000E-0	.456000E-0	.456000E-0
.456000E-0	.456000E-0	.456000E-0	.456000E-0
.456000E-0	.456000E-0	.456000E-0	.456000E-0
.456000E-0	.455500E-0	.454700E-0	.453500E-0
.450200E-0	.444600E-0	.437100E-0	.428000E-0
.416300E-0	.402400E-0	.387100E-U	.37000E-0
.351300E-0	.331300E-0	.310100E-0	.287100E-0
.263000E-0	.237900E-0	.212200E-0	.186200E-0
.161700E-0	.131200E-0	.101800E-0	.718700E-0
.516600E-0	.400100E-0	.190000E-C	.000000E+0
.000C00E+0	.000000E+0	.000000E+C	.000000E+0
.000000E+0	.000000E+0	.000000E+0	.000000E+0
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.000000E+0	.000000E+0	.000000E+0	.000000E+0
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.624000E+00 .656000E+00 .689000E+00 .720000E+00 .752000E+00 .816000E+00 .816000E+00 .816000E+00 .944000E+00 .944000E+00 .944000E+01 .107200E+01 .107200E+01 .107309E+01 .112353E+01 00000000000000000 .616000E+00 .648000E+00 .680000E+00 .7120000E+00 .744000E+00 .776000E+00 .872000E+00 .872000E+00 .916000E+00 .916000E+01 .103200E+01 .103200E+01 .119599E+01 .119599E+01 666666666666666666 . 608000E+00 . 640000E+00 . 704000E+00 . 736000E+00 . 736000E+00 . 812000E+00 . 812000E+00 . 861300E+00 . 861300E+00 . 928000E+00 . 928000E+00 . 102400E+01 . 102400E+01 . 102400E+01 . 102400E+01 0.600000E+00 0.632000E+00 0.696000E+00 0.728000E+00 0.728000E+00 0.76000E+00 0.824000E+00 0.856000E+00 0.952000E+00 0.952000E+00 0.952000E+00 0.984000E+00 0.984000E+00 0.101600E+01 0.101600E+01 000

"fa3body"

file

.191144E+0 .286420E+0 .483985E+0 .893654E+0	0.456000E-01 0.456000E-01 0.456000E-01 0.456000E-01 0.456000E-01 0.456000E-01 0.456000E-01 0.456000E-01 0.4712E-01 0.10772E-01 0.10772E-01 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00	0.6240008+00 0.656000E+00 0.656000E+00 0.7250008+00 0.725000E+00 0.784000E+00 0.816000E+00 0.912000E+00 0.912000E+01 0.107200E+01 0.107300E+01 0.10730E+01 0.10730E+01 0.10730E+01 0.10730E+01 0.10730E+01 0.121039E+01 0.121039E+01 0.121039E+01 0.121039E+01 0.121039E+01 0.121039E+01 0.121039E+01 0.121039E+01 0.121039E+01 0.121039E+01 0.121039E+01 0.480000E-01 0.480000E-01
176354E+0 .255750E+0 .420387E+0 .761779E+0	0.456000E-01 0.456000E-01 0.456000E-01 0.456000E-01 0.456000E-01 0.456000E-01 0.456000E-01 0.456000E-01 0.456000E-01 0.456000E-01 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00	0.61600E+00 0.648000E+00 0.712000E+00 0.776000E+00 0.84000E+00 0.84000E+00 0.96000E+00 0.96000E+00 0.96000E+00 0.10500E+00 0.10590E+01 0.10590E+01 0.10590E+01 0.10590E+01 0.10590E+01 0.10590E+01 0.10590E+01 0.10590E+01 0.10590E+01 0.10590E+01 0.10590E+01 0.10690E-01 0.10690E-01 0.10690E-01
164028E+0 230192E+0 367389E+0 651882E+0	2000000	0.64000E+00 0.64000E+00 0.642000E+00 0.736000E+00 0.736000E+00 0.964000E+00 0.864200E+00 0.864200E+00 0.864200E+00 0.95600E+00 0.95600E+00 0.95600E+00 0.95600E+01 0.105400E+01 0.105400E+01 0.105400E+01 0.106713E+01 0.116713E+01
151757E+0 208893E+0 323225E+0 .560302E+0	0.456000 0.456000 0.456000 0.456000 0.456000 0.456000 0.456000 0.456000 0.000000 0.0000000 0.0000000 0.000000	### ##################################

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0.48000E-01 0.46660E-01 0.306200E-01 0.189800E-02 0.88500E-02 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00

0.479400E-01 0.456700E-01 0.27400E-01 0.271000E-02 0.711000E-02 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00

0.478000E-01 0.443100E-01 0.248100E-01 0.135100E-01 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00

0.480000E-01 0.473900E-01 0.42700E-01 0.218300E-01 0.218300E-01 0.000000E-02 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00

FINAME(1)/'FA1BODY'/,FINAME(2)/'FA2BODY'/, FINAME(3)/'FA3BODY'/,FINAME(4)/'FA4BODY'/, FINAME(5)/'FA5BODY'/,FINAME(6)/'FA6BODY'/

F2NAME(1)/'FA1BOUT'/, F2NAME(2)/'FA2BOUT'/, F2NAME(4)/'FA4BOUT'/, F2NAME(6)/'FA4BOUT'/, F2NAME(6)/'FA6BOUT'/ DATA

F3NAME(1)/'FA1BDAT'/, F3NAME(2)/'FA2BDAT'/, F3NAME(4)/'FA4BDAT'/, F3NAME(4)/'FA4BDAT'/, F3NAME(6)/'FA6BDAT'/

AXISYMMETRIC BODIES.

(TURBULENT). (TURBULENT). (TURBULENT). P DINDSRDC (TURBULENT).
P DINDSRDC (TURBULENT).
P DINDSRDC (TURBULENT).
P DINDSRDC (TURBULENT). IBODY=1 ; AFTERBODY1 OF IBODY=2 ; AFTERBODY2 OF IBODY=3 ; AFTERBODY3 OF IBODY=5 ; AFTERBODY5 OF

\* READ BODY TYPE FROM THE TERMINAL.

WANT ?'
DTNSRDC'
DTNSRDC'
DTNSRDC'
DTNSRDC' WHAT KIND OF BODY DO YOU 'TYPE I FOR AFTERBODY1 OF 'TYPE 2 FOR AFTERBODY3 OF 'TYPE 5 FOR AFTERBODYS OF 'TYPE 5 FOR AFTERBODYS OF WRITE(\*,\*) WRITE(\*,\*) WRITE(\*,\*) WRITE(\*, .)

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READ(\*,\*) IBODY

REYNOLDS NUMBERS AND FRICTION VELOCITIES AT THE STARTING POINT OF THE BODY FROM EXPERIMENTAL DATA.

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RATIO=10. \*\*0.125 YPLUS=0.1 JMAX=52 NRP=45

IF(IBODY.EQ.1) THEN RE=6600000.D0 UTAU-0.04D0

IMB-52 IMAX-84

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ELSE IF(IBODY.EQ.2) THEN RE-6800000. DO UTAU-0.038D0

MAX-84 [MA=25 MB-52

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ELSE IF (IBODY.EQ.3) THEN RE-6000000.DO UTAU-0.038D0 MA-32

ELSE IF(IBODY.EQ.5) THEN EMAX-89

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RE-9300000.D0 MA=26

END IF

MAX=64

NUMBER OF GRID POINTS IN X-DIRECTION

READ BODY SHAPE AND X-COORDINATE. IP1=IMAX+1 IM1=IMAX-1

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OPEN(UNIT-7, FILE-FINAME(IBODY))
FEAD(7,1111)((X(I),I=1,IP1)
FEAD(7,1111)(RX(I),I=1,IP1)
FORHAT(4E14.6) 1111

CLOSE(7)

MODIFY THE LEADING EDGE AND TRAILING EDGE.

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OPEN(UNIT=10, FILE=F2NAME(1BODY)) 我们的现在分词 化环环 化环环 医克克特氏 医克克特氏 医克特特氏 医克特特氏 医克特特氏 医克特特氏 医克特特氏 医克特氏病

751 Y(I,J) "Y(I,1)+FR(J) \*(DELTA-Y(I,1))

DO 750 J=NRP, JP1

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DO 110 J=2,JMAX

DO 110 I=2,IMAX

F2(I,J)=(F2(I,J)*(RD(IMB)-RD(I))+F2(IP1,J)*(RD(I)-RD(IMA)))

I (RD(IMB)-RD(IMA))

IF(I.GT.IMB) F2(I,J)=F2(IP1,J)

IF(I.LT.IMA) F2(I,J)=F2(I,J)
                                                                                                                                                              107 F2(IP1,J) = (Y(IMB,J+1)+Y(IMB,J-1)-2.*Y(IMB,J))
                                                                                                                                                                                                                                                                                                                                                                  F1(I) = (X(I+1) + X(I-1) - 2 \cdot *X(I)) / (X(I+1) - X(I-1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           START ITERATION PROCESS FOR GRID GENERATION.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    *************************
                                                                                                                                                                                                                                                                                                                                                                                                                    我在我也我有我我也在我也就是我也有我也是我也是我的我也是我也是我也是我也是我也是我也
                                                                                                                       F2(1,J)=(Y(1,J+1)+Y(1,J-1)-2.*Y(1,J))
/(Y(1,J+1)-Y(1,J-1))
                                                SPECIFY THE GRID CONTROL FUNCTIONS.
                                                                                                                                                                            /(Y(IMB, J+1)-Y(IMB, J-1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                WRITE(10,2005)(Y(1,J),J=1,JP1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               DO 100 I=2,IMAX
DO 100 J=2,JMAX
XXI=0.5*(X(I+1)-X(I-1))
YXI=0.5*(Y(I+1,J)-Y(I-1,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                YET=0.5*(Y(I,J+1)-Y(I,J-1))
                                                                                                                                                                                                                                                                                                                                                                                                          PRINT INLET Y-COORDINATE.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               G11-XXI*XXI+XXI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            G22=XET*XET+YET*YET
G12=XXI*XET+YXI*YET
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      G=(G11+G22-G12+G12)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            DO 300 IT-1, ITMAX
                                                                                                                                                                                                      DO 108 I=1, IMAX
108 RD(I)=DELTA-RX(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   AJ(I,J)=DSQRT(G)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             A22(1,3)=G11/G
A12(1,3)=-G12/G
                                                                                                                                                                                                                                                                                                                                                    DO 297 I=2, IMAX
                                                                                             DO 107 J=2, JMAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 A11(I,J)=G22/G
             750 Y(I,J)~Y(1,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      DRMAX=0.
                                                                                                                                                                                                                                                                                                                                                                  297
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                                                                                                                                                                                                                                                                                                                        GENERATE Y-DIRECTIONAL GRID AT THE CENTER OF BODY.
                                                                                                                                                                                                                                                                                                             在各种的现在分词 计记录程序 化环境 医克拉特氏 医克拉特氏 医克拉特氏 医克拉特氏 医克拉特氏 医克拉特氏 医克拉特氏
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     GENERATE INITIAL GRID IN THE WHOLE DOMAIN.
                                                                                                                                                                                                                                                                                                                                                                                                                                                         GRID NUMBER OF STARTING POINT OF BODY.
                                                                                                                                                                                                                                                                                                                                                                                                                                               **********************
                                      SOME CONSTANTS AND RELAXATION FACTOR.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                FR(J)-(Y(1,J)-RX(1))/(DELTA-RX(1))
                                                                                                                                                                            NUMBER OF GRID IN Y-DIRECTION
                                                                                                                                                                                                                                           NUMBER OF GRID IN Y-DIRECTION WHERE GRID IS ORTHOGONAL.
                                                                                                                       MAXIMUM NUMBER OF ITERATIONS.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Y(1,1)=RX(1)
Do 82 J=2,JP1
Y(1,J)=Y(1,J-1)+DY1(J)
                                                                PI-3.141592653589793D0
EPS-0.001
                                                                                                                                                                                                                                                                                                                                                                                                                    DY1 (J) = DY1 (J-1) *RATIO
                                                                                                                                                                                                                                                                                                                                                               DY1(1)=0.
DY1(2)=YPLUS/RE/UTAU
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        DO 91 I=1,IP1
Y(I,1)=RX(I)
Y(I,NRP)=DELTA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          DO 750 I-1, IP1
DO 751 J-2, NRP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        DELTA-Y (1, NRP)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 DO 90 J=1,NRP
                                                                                                                                                                                                                                                                                                                                                                                                       DO 10 J-3,JP1
                                                                                                                                                                                                     JP1=JMAX+1
JMAM=JMAX-1
                                                                                                                                                 TWAX-500
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 CONTINUE
                                                                                             RF=1.8
                                                                                                                                                                                                                                                                                   J-KRP
                                                                                                                                                                                                                                                                                                                                                                                                                    2
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IMPLICIT REAL*8(A-H,O-Z)
DINENSION A(70),B(70),C(70),D(70),V(70),BETA(70),GAMMA(70)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         WRITE(11,2009) ((XC(I,J), i=1, FP1), J=1,JP1)
WRITE(11,2009) ((YC(I,J), i=1, IP1), J=1,JP1)
WRITE(11,2009) ((FX(I,J), i=1, IP1), J=1,JP1)
FORMAT(4D14.8)
                                                                                                                                                                                                                                                                                                                                                                                           -', FB.4)
                                                                                                                                                                                                                                                                                                         PRINT OUTPUT AFTER ITERATION PROCESS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            SUBROUTINE TRIDAG(IF, L, A, B, C, D, V)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           OPEN(UNIT=11, FILE=F3NAME(IBODY))
                                                                                                                                                                                                                                                                                                                                                                        WRITE(10,601) I,X(I)
FORMAT(5X, STATION ', I5,5X,'X '
WRITE(10,2005)(Y(I,J),J=1,JP1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          DO 250 J-1,JP1
250 WRITE(10,2005)(Y(I,J),I=1,IP1)
2005 FORMAT(4D14.6)
                                                                                                                                                                                                                                                                                                                                                                                                                                                            WRITE(10,2007)(X(I),I=1,IP1)
2007 FORMAT(6F12.8)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         SAVE DATA FOR CALCULATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              BETA(IF)=B(IF)
Ganna(IF)=D(IF)/BETA(IF)
                                             DO 301 J=1,JP1
F2(1,J)=F2(2,J)
F2(IP1,J)=F2(IMAX,J)
                                                                                                                                                                                                            FX(I,J) = FI(I)

FY(I,J) = F2(I,J)

YC(I,J) = Y(I,J)
                F1 (IP1)=F1 (IMAX)
                                                                                                                             REARRANGE DATA
                                                                                                                                                                            DO 123 I=1,IP1
DO 123 J=1,JP1
                                                                                                                                                                                                                                                                                                                                                           IGI,1=I 500 OG
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           IFP1=IF+1
DO 1 =IFP1,L
                                                                                                                                                                                                                                                              XC(I,J)=X(I)
F1(1)=F1(2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CLOSE(11)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CLOSE(10)
                                                                                                                                                                                                                                                                                                                                                                                                                             302 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            STOP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              END
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            2009
                                                                                                                                                                                                                                                              123
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                                                                                              00000
                                                                                                                                                                            SY=0.5*A12(I,J)*(Y(I+1,J+1)+Y(I-1,J-1)-Y(I+1,J-1)-Y(I-1,J+1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         PRINT 999, IT, DRHAX
999 FORMAT(5X, 'NO. OF ITERATION = ', IS, 5X, 'DRHAX=', D12.4)
                                                                                                                                                                                       AY(J)=-2.*A22([,J)*EPB*AZ/(EPB-1./EPB)

BY(J)=2.*A11(I,J)*A1*(EPA+1./EPA)/(EPA-1./EPA)

1 +2.*A22(I,J)*A2*(EPB+1./EPB)/(EPB-1./EPB)

CY(J)=-2.*A22(I,J)*BP$*A2/(EPB-1./EPB)

DY(J)=2.*A11(I,J)*A1/(EPA-1./EPA)*(Y(I-1,J)*EPA)

2 +Y(I+1,J)/EPA)+8Y
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           **************************
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ***********************
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          PRINT OUTPUT IN EACH ITERATION PROCESS.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        WRITE(10,189) IT, DRHAX
FORMAT(5X,'IT=',15,5X,'DRMAX=',D12.4)
                                                                                                                                                                                                                                                                                                                         DY(2)=DY(2)=AY(2)*Y(1,1)
DY(JHAX)=DY(JHAX)-CY(JHAX)*Y(1,JP1)
                                                                                                                                                                                                                                                                                                                                                                           CALL TRIDAG(2, JMAX, AY, BY, CY, DY, TY)
                                                                                                                                                                                                                                                                                                                                                                                                                YDIFF-DABS (TY(J)-Y(I,J))
IF(YDIFF.GT.DRMAX) DRMAX-YDIFF
Y(I,J)=Y(I,J)+RF*(TY(J)-Y(I,J))
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           SPECIFY THE BOUNDARY CONDITIONS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          SPECIFY BOUNDARY CONDITIONS
                                           A1-F1(I)
IF(DABS(A1).LT.EPS) A1-EPS
EPA-DEXP(A1)
                                                                                                                           A2-F2(1,J)
IF(DABS(A2).LT.EPS) A2-EPS
EPB-DEXP(A2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Y(1,3)=Y(2,3)
Y(IP1,3)=Y(IMAX,3)
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                           DO 501 J=2, JHAX
              DO 500 I-2, IMAX
                                                                                                             DO 502 J=2,JHAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           DO 130 J-1, JP1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            500 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              300
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         130
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            189
                                                                                                                                                                                                                                                                                                                                                                                                                                                                            501
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444

U

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106 CONTINUE

U U BETA(I)=B(I)-A(I)\*C(I-1)/BETA(I-1)
I GAMMA(I)=(D(I)-A(I)\*GAMMA(I-1))/BETA(I)
V(L)=GAMMA(L)
LAST=L-IF
DO 2 K=1,LAST
I=L-K
2 V(I)=GAMMA(I)-C(I)\*V(I+1)/BETA(I)
RETURN
END

21-A

FLARE APPROXIMATION FOR PARTIALLY PARABOLIC FORMULATION

IFA=2 FOR PARTIALLY PARABOLIC FORMULATION.

IFA=1 FOR ELLIPTIC FORMULATION.

: SUM OF MASS RESIDUALS.

RESEM

: V-VELOCITY AT THE WALL FUNCTION CALCULATION POINT.

: FRICTION VELOCITY.

UTAUA

TNU : EDDY VISCOSITY. SU,SV,SK,SD : SRC TERM FOR U,V,K,E. GEOMETRIC COEFFICIENTS : Bll,B22,512,G11,G12,G12,A11,A22,A12

COMMON/ PRES1/PR0(90,53), PP(90,53), PR(90,53)
COMMON/ PRES2/CU(90,53), CV(90,53), CUX(90,53)
COMMON/ PRES3/CU(90,53), PR(90,53), CUX(90,53)
COMMON/ GEO1/XP(90,53), YP(90,53)
COMMON/ GEO2/XU(90,53), YP(90,53)
COMMON/ GEO2/XU(90,53), YP(90,53)
COMMON/ GEO2/XV(90,53), YP(90,53)
COMMON/ GEO2/XV(90,53), YP(90,53)
COMMON/ GEO2/XV(90), YU3(90), YV4(90)
COMMON/ GEO2/YV(90), YP3(90), YP4(90)
COMMON/ GEO2/YP2(90), YP3(90), YP4(90)
COMMON/ GEO2/YP2(90), YP3(90), YP4(90)
COMMON/ GEO1/FV(90,53), FDY(90,53)
COMMON/ GEO12/FV(90,53), FPY(90,53)
COMMON/ GEO12/FY(90,53), FPY(90,53)
COMMON/ MALL1/FC(90), VSF(90), UTAUA(90)
COMMON/ MALL1/FC(90), VSF(90), UTAUA(90)
COMMON/ MALL1/FC(90), VSF(90), UTAUA(90)
COMMON/ MALL1/FC(90), YSF(90), Y IMPLICIT DOUBLE PRECISION (A-H,0-2) MAIN PROGRAM. COMMON/VEL2/US (90,53) COMMON/VEL3/UH (90,53) COMMON/VEL4/UG (90,53) COMMON/VEL6/VO (90,53) CHARACTER\*10 F2NAME(6) CHARACTER\*10 F3NAME(6) CHARACTER\*10 F4NAME(6) CHARACTER\*10 FINAME(6) COMMON/VEL1/U0(90,53) U

> \* VARIABLES INTERPRETATION.(NEARLY SAME AS FANS-2)

PRESSURE AT PREVIOUS TIME STEP. PRESSURE CORRECTION. PRESSURE EQUATION COEFFICIENTS.

PRESSURE.

PR PR0

VELOCITY. STAR VELOCITY.

U, V US, VS UV, VO DE BE

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TKEO TDSO

TKE 108

PP BCU, BCV

PEUDD VELCCITY.

VELOCITY AT PRESSURE EQUATION.

HASS SRC FOR PRESSURE CORRECTION EQUATION.

HASS SRC FOR PRESSURE CORRECTION EQUATION.

HASS SRC GENERALED BY NON-ORTHOGONALITY OF GRID.

TURBULENT KINETIC ENERGY AT PREVIOUS TIME STEP.

TURBULENT DISSIPATION RATE.

TURBULENT DISSIPATION RATE.

TURBULENT GENERATION TERM.

COEFF OF PRESSURE TERM IN MOMENTUM EQUATION.

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IMAX=84
                                                                                                                                                                                                                                                            IMAX-89
                                                                                                                                                                                                                                                                                   IMAX=84
                                                                                                                                                                                                                                                                                               END IF
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  FINAME(1)/'FA1BDAT'/, FINAME(2)/'FA2BDAT'/, FINAME(4)/'FA4BDAT'/, FINAME(4)/'FA4BDAT'/, FINAME(6)/'FA6BDAT'/
                                                                                                                                                                                                                                                                                 P2NAME(1)/'FA1OUT1'/, F2NAME(2)/'FA2OUT1'/,
P2NAME(3)/'FA3OUT1'/, F2NAME(4)/'FA4OUT1'/,
F2NAME(5)/'FA5OUT1'/, P2NAME(6)/'FA6OUT1'/
                                                                                                                                                                                                                                                                                                          F3NAME(1)/'FA1OUT2'/,F3NAME(2)/'FA2OUT2'/,
F3NAME(3)/'FA3OUT2'/,F3NAME(4)/'FA4OUT2'/,
F3NAME(5)/'FASOUT2'/,F3NAME(6)/'FA6OUT2'/
                                                                                                                                                                                                                                                                                                                                 F4NAME(1)/'FALOUT3'/,F4NAME(2)''FAZOUT3'/,
F4NAME(3)''FASOUT3'/,F4NAME(4)''FAGOUT3'/,
F4NAME(5)''FASOUT3'',F4NAME(6)''FAGOUT3''
                                                                                                                                                                                                                                                                                                           DATA
                                                                                                                                                                                                                                                                                                                                  DATA
                                                                                                                                                                                                                                                            DATA
                                                                                                                                                                                                                                                                                   PATA
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REYNOLDS NUMBERS AND FRICTION VELOCITIES AT THE STARTING POINT OF THE BODY FROM EXPERIMENTAL DATA. (TURBULENT). (TURBULENT). (TURBULENT). WANT ? DINSRDC DINSRDC DINSRDC DINSRDC DINSRDC (TURBULENT) 0000 BODY DO YOU WHAT KIND OF BODY DO YOU TYPE 1 FOR AFTERBODY1 OF TYPE 2 FOR AFTERBODY2 OF TYPE 3 FOR AFTERBODY3 OF TYPE 5 FOR AFTERBODY5 OF DTNDSRDC DTNDSRDC DTNDSRDC DTNDSRDC enternations of the Terminal. OPEN(UNIT=9,FILE=F2NAME(1BODY))
OPEN(UNIT=8,FILE=F3NAME(1BODY))
OPEN(UNIT=7,FILE=F4NAME(1BODY)) 90.00 THEN THEN ELSE IF(IBODY.EQ.2) THEN RE-6800000.D0 AFTERBODY1 AXISYMMETRIC BODIES. 1 AFTERBODYS ELSE IF(IBODY.EQ.3) RE-6000000.D0 ELSE IF(IBODY.EQ.5) RE=9300000.D0 SPECIFY CONSTANTS. THEN READ(\*,\*) IBODY IF(IBODY.EQ.1) 7 RE=6600000.D0 IMAX=84 WRITE(\*,\*)
WRITE(\*,\*)
WRITE(\*,\*) WRITE(\*,\*) IBODY-2 IBODY-3 IBODY-5 I BODY-1 00000

DO 131 J=1,JP1 XU(IP1,J)=XP(IP1,J)

8 P-A

SET UP THE INITIAL CONDITIONS. SET UP THE INLET CONDITION. R-0.5D0\*(¥C[1,J)+YC(1,J-1))
B11C(1,J)=(YC(1,J)+YC(1,J-1))\*R
B11C(1,J)=(YC(1,J)+YC(1,J-1))\*R
B11C(1,J)=(YC(1,J)-YC(1,J-1))\*R
B21C(1,J)=(XC(1,J)-XC(1,J-1))\*R
R-0.5D0\*(YC(1,J)+YC(1-1,J))
B12C(1,J)=(YC(1,J)-YC(1-1,J))\*R
9 B22C(1,J)=(XC(1,J)-XC(1-1,J))\*R YXI=0.5D0\*(YP(I+1,J)-YP(I-1,J))
YET=0.5D0\*(YP(I,J+1)-YP(I,J-1))
XXI=0.5D0\*(XP(I+1,J)-XP(I-1,J)) DO 20 I=1, IP1 VSF(I)=0.D0 DO 20 J=1, JP1 BCU(I,J)=0.D0 BCV(I,J)=0.D0 INU(I,J)=0.D0 A12P(I,J)=A12 A22P(I,J)=A22 AJIP(I,J)=AJI DELTAX-0.006D0 B21P(I,J)=B21 B22P(I,J)=B22 -111 B11P(I,J)=B11 B12P(I,J)=B12 DO 19 I=2, IP1 DO 19 J=2, JP1 PP(I,J)=0.D0 PR(I,J)=0.D0 CALL GEOCOE B22P(I,J) A11P(I,J) 19 20 18 000000 00000 O Ç

64-A

V(I+1,J)=V(I,J) US(I+1,J)=US(I,J) VS(I+1,J)=VS(I,J) VO(I+1,J)=VO(I,J) VO(I+1,J)=VO(I,J) TREO(I+1,J)=TREO(I,J) TREO(I+1,J)=TREO(I,J) TRE(I+1,J)=TRE(I,J) 27 TDS(I+1,J)=TDS(I,J) 26 CONTINUE	C attractor to the cost of Calific Cost of Calific Calculate the Cost of Calific Calculate of the Cost of Calific Calculate of the Calculate of Calific Calculate of the Calcula	C R=1.D0 YXI=YC(I,1)-YC(I-1,1) XXI=XC(I,1)-XC(I-1,1) YET=YP(I,2)-YP(I,1) XET=0.D0 CALL GEOCOE COSA=(B12*XET+B22*VET)/DSQHT(G22*G*A22)	C CALCULATE THE EDDY VISCOSITY. C CARGESPERSESSESSESSESSESSESSESSESSESSESSESSESSE	 ILOSE ILOSE ILOSE ILOSE ALEN=AK*(YP(I,J)-YP(I,J))*COSA ALEN=SQRT(TREO(I,J))*CYP(I,J))*COSA RK=RE*DSQRT(TREO(I,J))*(YP(I,J)-YP(I,J))*COSA TNU(I,J)=CMU*ALEN*DSQRT(TREO(I,J))*(1.Do-DEXP(-AMU*RK)) END IF	ELSE THU(I,J)=CNU*TKEO(I,J)*TKEO(I,J)/TDSO(I,J) END IF 28 CONTINUE	C DO 29 J=4,JP1 IF(TNU(I,J-1).LE.TNU(I,J-2).AND.TNU(I,J-1).LT. 1TNU(I,J) TNU(I,J)=TNU(I,J-1)	C IF(I.EQ.2) THEN DO 30 J=1,Pl 30 TNU(1,J)=TNU(2,J) END IF C IF(I.LT.IWAKE) TNU(I,1)=0.D0 IF(I.GE.IWAKE) TNU(I,1)=TNU(I,2)
C DO 22 J=1,JP1 V(1,J)=V(1,J) VS(1,J)=V(1,J) VS(1,J)=V(1,J) C DO 23 J=1,JP1 C DO 23 J=1,JP1 DO 23 J=1,JP1 CU(1,J)=0,D0	Cv(I,J)=0.Do Cuv(I,J)=0.Do DS(I,J)=0.Do 23 PP(I,J)=0.Do	1F(IT.LT.4) GO TO 24  DO 25 J=1,JP1  VO(1,J)=VO(2,J)  C TEEO(1,J)=TEEO(2,J)  25 CONTINUE  24 CONTINUE	C START SPACE MARCHING FROM UPSTREAM TO DOWN STREAM. C START SPACE MARCHING FROM UPSTREAM TO DOWN STREAM.		C essessessessessessessessessessessessess		VS(I,J)=V(I,J) VO(I,J)=V(I,J) VO(I,J)=V(I,J) TVO(I,J)=TVCO(I-1,J) TVC(I,J)=TVCO(I-1,J) TVC(I,J)=TVCO(I,J) TVC(I,J)=TVCO(I,J) VO(I,J)=TVCO(I,J)

IS-A

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CALCULATE F-A COEFFICIENT FOR V-MONENTUM EQUATION.
                                                                                                                                                                                                                                                                                                                        FY=FVY([,J)
ER=DSQRT(AllV(1,J))
FR=DSQRT(A22V(1,J))
AR=0.5004(REFF*AllV(I,J)*(B11V(I,J)*UU+B21V(I,J)*VV)-FX)
IF(AR:LE.0.D0) AR=0.D0-0.5D0*FX
BR=0.5D0*(REFF*AllV(I,J)*(B12V(I,J)*UU+B22V(I,J)*VV)-FY)
                                                                                                                                                                                                                                                  UU-6.2550*(U0(I,J)+U0(I,J+1)+U0(I-1,J)+U0(I-1,J+U))-TNUX
VV-V(I,J)-2.50*TNUY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          E2(I,J)=REFF*TAUI
D=REFF*VPC(I,J)/(1.D0+D2(I,J)+E2(I,J'. vPC(I,J))
CV(I,J)=D/(YP(I,J+1)-YP(I,J))
BCV(I,J)=B22C(I,J)*CV(I,J)
                                                                                                                                                                              DO 36 J-JAV,JMAX
TNUP-0.5DO*(TNU(I,J+1)+TNU(I,J))
REFF-1.00/(REI+TNUP)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 IF(I.LT.IWAKE) THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     VEB(I,J)=CF(3,1)
VEC(I,J)=CF(3,2)
VET(I,J)=CF(3,3)
IF(IFA.EQ.2) THEN
DZ(I,J)=VMC(I,J)
ELSE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  BCV(I,JP1)=0.D0
BCV(I,JAVM1)=0.D0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    VWB(I,J) = CF(1,1)
VWC(I,J) = CF(1,2)
VWT(I,J) = CF(1,3)
VWC(I,J) = CF(2,1)
VPC(I,J) = CF(2,2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     IF (IFA.EQ. 2) THEN
                       DO 35 J-JAP, JP1
                                                               BCU(IP1, J) =0. DO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               U(I,1)=0.D0
US(I,1)=0.D0
UH(I,1)=0.D0
TKE(I,1)=0.D0
END IF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              US(I,JP1)=1.D0
                                           BCU(1,J)=0.D0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     D2(I,J)=0.D0
END IF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         CALL COEFF2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                COEFF3
                                                                                                                                                                                                                                                                                                          FX=FVX(I,3)
                                                                                                                                                                                                                                                CALL SRCV
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    END IF
                                                               35
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              36
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     E1(I,J)=REFFUTUI

D=REFFUTC(I,J)/(1.D0+D1(I,J)+R1(I,J)*UPC(I,J))

CU(I,J)=D/(XP(I+1,J)-XP(I,J))

CU(I,J)=D=(YP(I,J)-YP(I+1,J)/(XP(I+1,J)-XP(I,J))

CU(I,J)=D=(YP(I,J+1)+YP(I+1,J+1)-YP(I+1,J-1)-YP(I,J-1)))

BCU(I,J)=B11C(I,J)*CU(I,J)
                                                                                                                                           CALCULATE THE PIRST FICTICIOUS V-VELOCITY BY INTERPOLATION.
                                                                                                                         如果我们的有一个,我们的是一个,我们的,我们的,我们的,我们的,我们的人们的,我们的人们的人们的,我们的人们的人们的人们的,我们的人们的人们的人们的人们的人们的人
                                                                                                                                                                                                                                                                                  CALCULATES F-A COEFFICIENTS FOR THE U-MOMENTUM EQUATION.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  FY=FUT(I,J)
ER=DSQRT(AllU(I,J))
FR=DSQRT(AllU(I,J))
AR=0.5Dow(FFFFAJIU(I,J)) + (BllU(I,J) + UU+B2lU(I,J) + VV) - FX)
AR=0.5Dow(FFFFAJIU(I,J)) + (BllU(I,J) + UU+B2lU(I,J) + VV) - FX)
BR=0.5Dow(REFFAJIU(I,J)) + (Bl2U(I,J) + UU+B22U(I,J) + VV) - FY)
DR=2.DO*AR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     UU=U0(I,J)-2.D0*TNUX
VV=0.25D0*(V0(I,J-1)+V0(I+1,J-1)
+V0(I,J)+V0(I+1,J))-TMUY
                                                                                                                                                                                                                                                                                                                                                                                     DO 34 J-JAU,JMAX
TWUP-0.5D0*(TWU(I+1,J)+TWU(I,J))
REFF-1.D0/(REI+TWUP)
                                                                                                                                                                                                    V(I,1)-V(I,2)*YV1(I)/YV2(I)
VO(I,1)-V(I,1)
IF(IT.GT.ITH) GO TO 31
DO 32 J=1,JP1
TMU(I+1,J)=TMU(I,J)
COMTIMUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   CALL COEFF3
END IF
UNB(I,J) = CF(1,1)
UNC(I,J) = CF(1,2)
UNT(I,J) = CF(2,1)
UPC(I,J) = CF(2,2)
UPT(I,J) = CF(2,2)
UEB(I,J) = CF(2,2)
UEC(I,J) = UEC(I,J)
UEC(I,J) = UEC(I,J)
UEC(I,J) = UEC(I,J)
UEC(I,J) = UEC(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         IP(IFA.EQ.2) THEN
CALL COEFF2
ELSE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             D1(1,3)=0.D0
END 1P
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SS-A

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U(I,JF1)=1.D0 UH(I,JF1)=1.D0	C START INNER ITERATION.	DO 6000 ITA-1,ITERA	C CALCULATE THE U-STAR VELOCITY.  C CALCULATE THE U-STAR VELOCITY.  C C CALCULATE THE U-STAR VELOCITY.	DO 45 IUVAL, ITUV DO 46 JAJAU, JHAX AA(11) == IIDR(T 1)	BB(J)=1.D0+D1(I,J)+E1(I,J)*UPC(I,J) CC(J)=-UPT(I,J) 46 DD(J)=-UC(I,J)*US(I+1,J)+UEB(I,J)*US(I+1,J-1) 1 DFFT(I,J)*US(I+1,J)+UEB(I,J)*US(I+1,J-1)	1 + UMB(I.J) = US(I.L.J.L) + UMC(I.J.J) = US(I-1.J.J) 2 + UMB(I.J.J) = US(I.L.J.J.L) + UMT(I.J.J. = US(I.L.J.J.L) 3 + UMB(I.J.J. = US(I.J.J. + USU(I.J.J.))		6 DD(JAU) = DD(JAU) = DA(JAU) * US(I,J-1) - PR(I+1,J-1) DD(JAMX) = DD(JAMY) + US(I,J-MU) DD(JMAX) = DD(JMAX) * US(I,J-MU) DS(JMAX) = DS(JMAX) * US(I,J-MU) CAII ***********************************	DO 47 J-JAU, JHAX 47 US(I,J)=I(J) IF(I,LT,IMAKE) GO TO 45 US(I,1)=(YUSQ(I)*US(I,2)-YU2SQ(I)*US(I,3))	1 / (YU3SQ(I)~YUZSQ(I)) 45 CONTINUE C	C CALCULATE THE V-STAR VELOCITY.	ITUV-3	DO SO IUV-1, ITUV	55	51 DD(J) = VPE(I,J) = VE(I+1,J) + VEB(I,J) = VS(I+1,J-1)	1 +VET[1,J) *VS[1+1,J+1)+VMC[1,J) *VS[1-1,J] 2 +VMB[1,J) *VS[1-1,J-1)+VMT[1,J) *VS[1-1,J+1] 3 +VPC(1,J) *(E2(1,J) *VO[1,J)+SV(1,J))	DO(JAV) =DO(JAV) = (PK(I,J+1) = PK(I,J)) DO(JAV) =DO(JAV) = (JAV) = (JAV) = (JAV)

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Attachmental and the statement of the st
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FR=DSQRT(A22P(I,J))
AR=0.5D0*(REFF*AJIP(I,J)*(B!1P(I,J)*UU+B21P(I,J)*VV)-FX)
IF(AR.LE.0.D0) AR=0.D0-0.5D0*FX
BR=0.5D0*(REFF*AJIP(I,J)*(B12P(I,J)*UU+B22P(I,J)*VV)-FY)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     DO 62 ITK=1,ITKD
DO 63 J=JA,JHAX
AA(J)=-TRPB(I,J)
BB(J)=1.D0+D3(I,J)+(E3(I,J)-SKP(I,J))*TKPC(I,J)
CC(J)=-TKPT(I,J)
CC(J)=-TKPT(I,J)
1 +TKE(I,J)*TKE(I+1,J)+TKPC(I,J)*TKE(I+1,J-1)
1 +TKE(I,J)*TKE(I+1,J+1)+TKMT(I,J)*TKE(I-1,J-1)
2 +TKPC(I,J)*TKE(I-1,J-1)+TKMT(I,J)*TKE(I-1,J-1)
DD(JA)=DD(JA)-AA(JA)*TKE(I,J)*TKE(I,J)*TKE(I-1,J+1)
DD(JAA)=DD(JAAX)*CC(JAAX)*TKE(I,JP1)
CALL TRIDAG(JA,JAAX,AA,BB,CC,DD,T)
DD 64 J=JA,JHAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              TRE(I,JPI)=TKE(I,JMAX)
IF(I.LT.IMAKE) GC TO 62
TRE(I,1)=(VP3SQ(I)*TKE(I,2))
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             E4(I,J)=CEPS*REFF*TAUI
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             IF(I.LE.IWAKE) THEN
                                                                                                                                                                                                                                                                                                                                                                 TDWC(1,2) = CF(1,2)
TDWT(1,3) = CF(1,2)
TDPB(1,3) = CF(2,1)
TDPC(1,3) = CF(2,2)
TDPT(1,3) = CF(2,3)
TDEB(1,3) = CF(3,2)
TDET(1,3) = CF(3,2)
TF(FA.EQ.2) THEN
DF(1,3) = CF(3,3)
EESE
                                                                                                                                                                                                                                                                                                                                              TDWB(I,J)-CF(1,1)
                                                                                                                                                                     IF(IFA.EQ.2)THEN
CALL COEFF2
ELSE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       TKE(1,3)=T(J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                D4(I,J)=0.D0
END IF
                                                                                                                                                                                                                                                                             CALL COEFF3
                                                                                                                                        DR=2. DO*AR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ITKD-3
                                                                                                                                                                                                                                                                                                                END IF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          62
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 000000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             000000
                                                                                                                                                                                                  CALCULATE THE FINITE AMALYTIC COEFFICIENT FOR TURBULENT KINETIC ENERGY EQUATION.
                                                                                                                                                                        FY=FPY(I,J)
ER=DSQRT(A22P(I,J))
FR=DSQRT(A22P(I,J))
FR=DSQRT(A22P(I,J))
FR=DSQRT(A22P(I,J))
FR=DSQRT(A22P(I,J))
FR=DSQRT(A22P(I,J))
FR=DSQRT(A22P(I,J) *(B11P(I,J) *(UU+B21P(I,J) *VV) -FX)
FR=DSQRT(A22P(I,J) *(B12P(I,J) *(U+B22P(I,J) *VV) -FY)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 CALCULATE THE FINITE ANALYTIC COEFFICIENT OF THE TURBULENT DISSIPATION RATE EQUATION.
                                                                                                                                                                                                                                                                                                                                                                                                                                        UU=0.5D0*(U0(I,J)+U0(I-1,J))*CEPK - THUX
VV=0.5D0*(V0(I,J-1)+V0(I,J))*CEPK - THUY
PX=PPX(I,J)
                                   U(1,1) = (YU3SQ(1) * U(1,2) - YU2SQ(1) * U(1,3))
(YU3SQ(1) - YU2SQ(1))
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 UU=0.5D0*(U0(I,J)+U0(I-1,J))*CEPS-TNUX
VV=0.5D0*(V0(I,J-1)+V0(I,J))*CEPS-TNUX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   DO 61 J-JA,JHAX
TNUP-TNU(1,J)
REFF-1.DO/(REI*CEPS+TNUP)
         IF (I.LT.IWAKE) GO TO 6000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     E3(I,J)=CEPK+REFF+TAUI
CONTINUE
                                                                                                                                                                                                                                                                                                                                          DO 60 J-JA,JMAX
TNUP-TNU(I,J)
REFF=1.DO/(REI+TNUP)
CALL SRCK
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ER-DSQRT(Allp(I,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   TKNC (1,3) -CF (1,2)
TKNP (1,3) -CF (1,3)
TKPP (1,3) -CF (2,2)
TKPT (1,3) -CF (2,3)
TKRP (1,3) -CF (2,3)
TKRP (1,3) -CF (3,1)
TKRP (1,3) -CF (3,2)
TKRT (1,3) -CF (3,2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               TK4B(I,J)=CF(1,1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             D3(1,J)=TKWC(1,J)
Else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             IF(IFA.EQ.2)THEN
CALL COEFF2
ELSE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 D3(I,J)=0.D0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               COEFF3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     FX-FPX(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             DR-2. DO * AR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CALL SRCD
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      FY=FPY (I
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               END IF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            END IF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               CALL
                                                                                                           9009
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   9
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RMAX=YC(1,1)
DO 3003 J=1,3P1
RU(1,J)=(YU(1,J)-YU(1,1))/RWAX
RU(1,J)=(YP(1,J)-YP(1,J))/RWAX
RP(1,J)=(YP(1,J)-YP(1,J))/RWAX
RV(1,J)=(YV(1,J)-YV(1,J))/RWAX
3003 WRITE(9,207)RU(1,J), UO(1,J), RV(1,J), YO(1,J), RP(1,J), TKEO(1,J)
, PR(1,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   2222 WRITE(9,3001)
3001 FORMAT(//5%,'RU(I,J)',6%,'VEL U',7%,'RV(I,J)',5%,'VEL V',6%,
1'RP(I,J)',5%,'TURB KE',3%,'PRESSURE'//)
                                                                                                                                                                                                                                                                                                                                                                                                     各种技术的现在分词有效的现在分词有效的现在分词有效的现在分词有效的现在分词的现在分词的现在分词形式的现在分词
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            2098 WRITE(9,2099) UTAUA(1),FC(1)
2099 FORMAT(5X,'UTAU=',E12.4,5X,'FRICTION COEF = ',E12.4)
                                                                                                                                                                                                                          FORMAT(5X, 'NO. OF ITERATION = ', I4, 3X, 'ERRM=', Ell.4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       WRITE(9,2) IT, I, XP(I,1), TAU
: FORMAT(//5X, 'NO. OF ITERATION =', I3, 5X, 'STATION', I3
1,5X,'X =',F8.4,5X,'TAU =',F6.3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  OUTPUT AFTER FINAL ITERATION.
CALCULATE SUM OF MASS RESIDUALS.
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COMMON/VEL9/V(90,53)
COMMON/VEL9/V(90,53)
COMMON/TURBJ/TKE(90,53)
COMMON/TURBJ/TKE(90,53)
COMMON/TURBJ/TKE(90,53)
COMMON/TURBJ/TUS(90,53)
COMMON/TURBJ/TUS(90,53)
COMMON/TURBJ/TUS(90,53)
COMMON/TURBG/TGE(90,53)
COMMON/ST/SV(90,53),SV(90,53),SK(90,53),SD(90,53)
COMMON/ST/SV(90,53),YD(90,53)
COMMON/CONSJ/TUJ,J,IMAX,JMAX,JMAX,JRJ,JAU,JAV,JAP,JA,IFA,IWAKE
COMMON/CONSJ/TUJ,J,IMAX,JMAX,JMAX,JRJ,JAU,JAV,JAP,JA,IFA,IWAKE
COMMON/CONSJ/TV(90,53),YV(90,53)
COMMON/GED3/XV(90,53),YV(90,53)
COMMON/GED4/XV(90,53),YV(90,53)
COMMON/GED4/XV(90,53),YV(90,53)
COMMON/GED4/XV(30,53),YV(90,53)
COMMON/GED4/XV(30,53),YV(90,53)
COMMON/GED4/XV(30,53),YV(90,53)
COMMON/GED4/XV(30,53),YV(30,53)
COMMON/GED4/XV(30,53),YV(30,53)
COMMON/GED4/XV(30,53),YV(30,53)
COMMON/GED4/XV(30,53),YV(30,53)
COMMON/GED4/XV(30,53),YV(30,53)
COMMON/GED4/XV(30,53),YV(30,53)
COMMON/GED4/XV(30,53),YV(30,53)
COMMON/GED4/XV(30,53),YV(30,53)
                                                                                                                                                                                                                                                                                                                                                                                                 ENERGY EQUATION.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               XXI=XU(I,J)-XU(I-1,J)

YXI=YU(I,J)-YU(I-1,J)

XET=0.25D0*(XU(I,J+1)+XU(I-1,J+1)-XU(I,J-1)-XU(I-1,J-1))

YET=0.25D0*(YU(I,J+1)+YU(I-1,J+1)-YU(I,J-1)-YU(I-1,J-1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            YET=YV(I,J)-YV(I,J-1)
XXI=0.25D0*(XV(I+1,J)+XV(I+1,J-1)-XV(I-1,J)-XV(I-1,J-1)
YXI=0.25D0*(YV(I+1,J)+YV(I+1,J-1)-YV(I-1,J)-YV(I-1,J-1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 CALL GEOCCE
DUET=0.25D0*(U(1,J+1)+U(1-1,J+1)-U(1,J-1)-U(I-1,J-1))
DUXI=0.15D0*(U(1,J+1)+U(I-1,J+1)-U(1,J-1)-U(I-1,J-1))
DUXI=1.611*DUXI+B12*DUET)
DUX=AJI*(B11*DUXI+B22*DUET)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CALL GEOCOE

DVET=V([,J)-V(I,J-1)

DVET=V([,J)-V(I+1,J)+V(I+1,J-1)-V(I-1,J)-V(I-1,J-1))

DVX=AJI*(B11*DVXI+B12*DVET)

DVY=AJI*(B21*DVXI+B2*DVET)
                                                                                                                                                                                                                                                                                                                                                                   CALCULATE THE SOURCE FUNCTION FOR TURBULENT KINETIC
SS=0.5D0*Al2*(V0(I+1,J+1)+V0(I-1,J-1)-V0(I+1,J-1)
-V0(I-1,J+1))
                                                                                        R=YV(I,J)
VO=V(I,J)
SV(I,J)=SS+REFF*(TNUX*DUY
-2.DO/3.DO*DKY)-VO/R/R
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      IMPLICIT REAL*8(A-H,O-Z)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  XET=XV(I,3)-XV(I,3-1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            SUBROUTINE SRCK
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    R=YP(I,J)
                                                                                                                                                                                                                                                                              END
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ပပ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          U
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                                                                                                                                                                                                                                                                                                           000000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              DKET=TRE(I,J+1)-TKE(I,J)

DKXI=0.25D0*(TKE(I+1,J)+TKE(I+1,J+1)-TKE(I-1,J)-TKE(I-1,J+1))

TNET=TWU(I,J+1)-TWU(I,J)

TNET=TWU(I,J+1)-TWU(I+1,J)+TWU(I-1,J)-TWU(I-1,J)-TWU(I-1,J+1))

DKY=DJI*(B21*DKXI+B22*DKET)

TWUY=DJI*(B21*TWXI+B22*TWET)

TWUY=DJI*(B11*TWXI+B12*TWET)
                                                                                                                                                                                                                                                                                                                                   COMMON VELA/U (90,53)
COMMON/VELA/V (90,53)
COMMON/VELS/V (90,53)
COMMON/TURBJ/TKE(90,53)
COMMON/TURBJ/TKE(90,53)
COMMON/TURBJ/TKE(90,53)
COMMON/TURBJ/TKE(90,53)
COMMON/TURBJ/TKE(90,53)
COMMON/CONSI/I,J,IMAX,JMAX,IP1,JP1,JAU,JAV,JAP,JA,IFA,IWAKE
COMMON/CONSI/I,J,IMAX,JMAX,IP1,JP1,JAU,JAV,JAP,JA,IFA,IWAKE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 R=YV(I,J)

XXI=0.25D0*(XP(I+1,J)+XP(I+1,J+1)-XP(I-1,J)-XP(I-1,J+1))

XXI=0.25D0*(YP(I+1,J)+YP(I+1,J+1)-YP(I-1,J)-YP(I-1,J+1))

XET=XP(I,J+1)-XP(I,J)
                                                                                                                     CALCULATE THE SOURCE FUNCTION FOR V-MOMENTUM EQUATION.
                                                                                              XET=0.5D0*(XU(I,J+1)+XU(I-1;J+1)-XU(I,J)-XU(I-1,J))
YET=0.5D0*(YU(I,J+1)+YU(I-1,J+1)-YU(I,J)-XU(I-1,J)
XXI=0.5D0*(XU(I,J)+XU(I,J+1)-XU(I-1,J)-XU(I-1,J+1)
XXI=0.5D0*(YU(I,J)+YU(I,J+1)-YU(I-1,J+1)-YU(I-1,J+1)
CALL GEOCOE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            DUET-0.5D0*(U(I,J+1)+U(I-1,J+1)-U(I,J)-U(I-1,J))
DUXI-0.5D0*(U(I,J)+U(I,J+1)-U(I-1,J)-U(I-1,J+1))
DUY-AJI*(B2I*DUXI+B22*DUET)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              COMMON/GED1/XP(90,53), YP(90,53)
COMMON/GED3/XU(90,53), YU(90,53)
COMMON/GED4/XV(90,53), YV(90,53)
COMMON/BODY1/B1, B12, B22
COMMON/BODY2/G11, G12, G22, A11, A12, A22, G, AJI
COMMON/BODY3/XXI, XXI, XET, YET, R
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               XXI=0.5D0*(XV(I+1,J)-XV(I-1,J)

XXI=0.5D0*(YV(I+1,J)-YV(I-1,J)

XET=0.5D0*(XV(I,J+1)-XV(I,J-1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       YET-0.5D0*(YV(I,J+1)-YV(I,J-1))
CALL GEOCOE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               DVET-0.5D0*(V(I,J+1)-V(I,J-1))
DVXI-0.5D0*(V(I+1,J)-V(I-1,J))
DVX-AJI*(B11*DVXI+B12*DVET)
DVY-AJI*(B21*DVXI+B22*DVET)
                                                                                                                                                                                                                                                                                                           IMPLICIT REAL*8(A-H,0-Z)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      YET-YP(I,J+1)-YP(I,J)
CALL GEOCOE
                                                                                                                                                                                                                                                 SRCV
                                                                                                                                                                                                                                              SUBROUTINE
RETURN
                                   END
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R=YP(I,J) XXI=XU(I,J)-XU(I-1,J) XXI=YU(I,J)-YU(I-1,J) XXI=YU(I,J)-YU(I-1,J) XET=0.25D0*(XU(I,J+1)+XU(I-1,J+1)-XU(I,J-1)-XU(I-1,J-1)) YET=0.25D0*(YU(I,J+1)+YU(I-1,J+1)-YU(I,J-1)-YU(I-1,J-1)) CALL GEOCOE DUET=0.25D0*(U(I,J+1)+U(I-1,J+1)-U(I,J-1)-U(I-1,J-1)) DUX=AI*(BIJ*DUXI+BIZ*DUET) CC UND UXI-XI*(BIJ*DUXI+BIZ*DUET) CC UND UXI-XI*(BIJ*DUXI+BIZ*DUET)	XET=XV(I,J)-XV(I,J-1) YET=YV(I,J)-YV(I,J-1) XXI=0.25D0*(XV(I+1,J)+XV(I+1,J-1)-XV(I-1,J)-XV(I-1,J-1)) XXI=0.25D0*(XV(I+1,J)+YV(I+1,J-1)-YV(I-1,J)-YV(I-1,J-1)) XXI=0.25D0*(XV(I+1,J)+YV(I+1,J-1)-YV(I-1,J)-YV(I-1,J-1)) DVXI=0.25D0*(V(I,J-1) DVXI=0.25D0*(V(I+1,J)+V(I+1,J-1)-V(I-1,J)-V(I-1,J-1)) DVXI=AJI*(B21*DVXI+B12*DVET)	XXI=0.5D0*(XP(I+1,J)-XP(I-1,J))  XXI=0.5D0*(YP(I+1,J)-YP(I-1,J))  XXT=0.5D0*(XP(I,J+1)-XP(I,J-1))  XET=0.5D0*(XP(I,J+1)-XP(I,J-1))  YET=0.5D0*(YP(I,J+1)-YP(I,J-1))  TWEF=0.5D0*(TDS(I,J+1)-TDS(I,J-1))  TWEF=0.5D0*(TDS(I,J-1)-TDS(I,J-1))  DEXI=0.5D0*(TDS(I+1,J)-TNU(I,J-1))  DEXI=0.5D0*(TDS(I+1,J)-TNU(I-1,J))  TWXI=0.5D0*(TBX(I+1,J)-TNU(I-1,J))  DEXI=0.5D0*(RSI*TWXI+B22*DEET)  TWY=AJI*(RSI*TWXI+B22*DEET)  TWY=AJI*(RSI*TWXI+B22*DEET)  TWY=AJI*(RSI*TWXI+B22*TWET)  TWY=AJI*(RSI*TWXI+B22*TWET)  C  TRUX=AJI*(RSI*TWXI+B12*TWET)  C  TRUX=AJI*(RSI*TWXI+B12*TWET)  C  TRUX=AJI*(RSI*TWXI+B12*TWET)  C  TRUX=AJI*(RSI*TWXI+B12*TWET)	R=YP(1,J) VO=0.5D0*(V(I,J)+V(I,J-1)) C TGE(I,J)=TNU(I,J)*(2.D0*DUX*DUX+2.D0*DVY*DVY+ 1 ADK=TDS(I,J)/TKE(I,J) SDP(I,J)=ADK*CEPS*REFF*CEPS2 SD(I,J)=SS+CEPS*REFF*CEPS1*TGE(I,J)*TKE(I,J) C RETURN END	C ALCULATE FINITE ANALYTIC COEFFICIENT OF TRANSPORT C CALCULATE FINITE ANALYTIC COEFFICIENT OF TRANSPORT C CALCULATE FINITE ANALYTIC COEFFICIENT OF TRANSPORT C EQUATIONS FOR PARTIALLY PARABOLIC CASE. (3-POINT) C SUBROUTINE COEFF2 C IMPLICIT DOUBLE PRECISION (A-H,O-Z) COMMON/COEF7/CF(3,3) COMMON/FA1/AR,BR,BR,FR COMMON/FA1/AR,BR,BR,FR COMMON/FA1/AR,BR,BR,FR
C XXI=0.5D0*(XP(I+1,J)-XP(I-1,J)) YXI=0.5D0*(XP(I+1,J)-XP(I-1,J)) XET=0.5D0*(XP(I,J+1)-XP(I,J-1)) YET=0.5D0*(YP(I,J+1)-YP(I,J-1)) CALL GECCOE DKET=0.5D0*(TKE(I,J+1)-TKE(I,J-1)) TNET=0.5D0*(TKE(I,J+1)-TKE(I,J-1)) DKXI=0.5D0*(TKE(I+1,J)-TKE(I,J-1)) DXXI=0.5D0*(TKE(I+1,J)-TKE(I-1,J)) DXX=AJI*(B11*DKXI+B12*DKET)	DKY=AJI (	TGE(I,J)=TNU(I,J)=(2.D0=DDX*DDX+2.D0=DY*PDX+  C ADK=TDS(I,J)-ADK*CEPF*REF  SK(I,J)=SA+CEPK*REFF*TGE(I,J)  C RETURN  END  C AARAGAARARARARARARARARARARARARARARARARA	IMPLICIT REAL*8(A-H,O-Z)  COMMON/VEL5/U(90,53)  COMMON/TURB1/TKE(90,53)  COMMON/TURB3/TXE0(90,53)  COMMON/TURB4/TDS0(90,53)  COMMON/TURB4/TDS0(90,53)  COMMON/TURB5/TMU(90,53)  COMMON/TURB6/TGE(90,53)  COMMON/TURB6/TGE(90,53)  COMMON/TURB6/TGE(90,53)  COMMON/STLA/SWP(90,53),SW(90,53),SM(90,53)	COMMON/CONSI/I, J, IMAX, JMAX, IPI, JPI, JAU, JAV, JAP, JA, IFA, IWAKE COMMON/CONSG/REFF COMMON/CONSG/REFF COMMON/GEO1/XP(90, 53), YP(90, 53) COMMON/GEO1/XP(90, 53), YV(90, 53) COMMON/GEO3/XV(90, 53), YV(90, 53) COMMON/GEO4/XP(90, 53), YV(90, 53) COMMON/BODYI/B11, B12, B21, B22 COMMON/BODYI/B11, B12, B21, B22 COMMON/BODYI/B11, B12, B21, B22 COMMON/BODYI/SYXI, XXI, XET, YET, R COMMON/BUDYI/TNUX, TNUY C

```
EPBKI=1.DO/EPBK
TANNB=(EPBK-EPBKI)/(EPBK+EPBKI)
CF(2,3)=EPBKI/(EPBK+EPBK)
CF(2,2)=TANNB/(2.DO*BRO)
CF(2,1)=EPBK/(EPBK1+EPBK)
GO TO 2
                                                DBK-DMIN1 (DABS (BK), FMAX)
BK-DSIGN (DBK, BK)
                                                                                                                                                                                                 CF(2,1)=0.5D0
CF(2,2)=0.5D0/FR/FR
CF(2,3)=0.5D0
CONTINUE
                                                                                                                                                                                                                                                               CF(1,1)=0.00
CF(1,2)=CF(2,2)*DR
CF(1,3)=0.00
CF(3,1)=0.00
CF(3,2)=0.00
CF(3,3)=0.00
                   HY-1. DO/FR
BR-BR/FR
                                  BK-BR+HY
```

```
SUBROUTINE TRIDAG(IF, L, A, B, C, D, V)
IMPLICIT DOUBLE PRECISION (A-H, O-Z)
DIMENSION A(53), B(53), C(53), D(53), V(53), BETA(53), GANMA(53)
BETA(1F) = B(IF)
GANMA(IF) = D(IF)/BETA(IF)
SUBROUTINE TRIDAG TO SOLVE ALGEBRAIC EQUATIONS SIMULTANEOUSLY FOR EACH ROW OR COLUMN
                                                                                                                                                                                                                                                                                                                                         DO 1 I-IFP1, L
```

```
BETA(I) = B(I) - A(I) + C(I-I) / BETA(I-I) \\ GAMMA(I) = (D(I) - A(I) + GAMMA(I-I) ) / BETA(I) \\ V(L) - GAMMA(L)
                                                                 V(I)=GAMMA(I)-C(I)+V(I+1)/BETA(I)
RETURN
                                   LAST-L-IF
DO 2 K-1, LAST
                                                          1-L-K
                                                                                                       0000000
```

```
CALCULATE THE FINITE ANALYTIC COEFFICIENT FOR CONVECTIVE-
DIFFUSION PROBLEM --- ELLIPTIC CASE ( 9 POINT FORMULA.)
                                                                                                                                         SUBROUTINE COEFF3
IMPLICIT DOUBLE PRECISION (A-H,0-Z)
COMMON/COEF7/CF(3,3)
```

```
IF (DABS (AR) . LT. EPE) AR=DSIGN (EPE, AR)
IF (DABS (BR) . LT. EPE) BR=DSIGN (EPE, BR)
COMMON/FA1/AR, BR, DR, ER, FR
                                                                                                                                                                                                                                                                                                                                                            IF(DAH.GT.EMAX) IM=1
IF(DBK.GT.EMAX) JM=2
MT=IM+JM+1
GO TO (1,2,3,4), MT
                                                    PI=3.1415926535897D0
                                                                                                                                                                                        FR2=FR*FR
AB2=AR*AR+BR*BR
                                                                                                                                                                                                                                                                   DAH=DABS(AH)
DBK=DABS(BK)
AH2=AH*AH
BK2=BK*BK
                                       MAX-20. DO
                                                                                EPE=1.0-5
                                                                                                         BR-BR/FR
HX=1./ER
HY=1./FR
                                                                                                                                                                         ER2=ER*ER
                                                                                                                                                                                                                               AK=AR+HY
BH=BR+HX
                                                                                            AR-AR/ER
                                                                                                                                                                                                                  AH=AR+HX
                                                                                                                                                                                                                                                          BK-BR*HY
                                                                   C1=1.D0
                                                                                                                                                                                                                                                                                                                                       IM=0
             υ
                                                                                                                                                                                                                                                                                                                         U
```

EPAH-DEXP(AH)
EPBK-DEXP(BK)
EPAHI-1./EPBK
EPAHI-1./EPBK
COSHA-0.5\*(EPAH\*EPAHI)
COSHB-0.5\*(EPBK+EPBKI)
COTHA-2.\*COSHB-(EPBK-EPBKI)
COTHA-2.\*COSHB-(EPBK-EPBKI)
ACTHB-AK\*COTHA
BHCTHB-BH\*COTHB IF(HX.GT.HY) GO TO 11 EX:=0. DO 10 M=1,MAX ZA=(M=0.5)\*PI ZA2=ZA\*ZA

O

10 EX2=EX2-PWR\*ZA/((AB+1./AB)\*(AH2+ZA2)\*(AH2+ZA2))
9 PA=B.\*AH\*COTHA\*COSHA\*COSHB\*EX2
PB=1.+BHCTHB/AKCTHA\*(PA-1.)
CF(2,2)=0.5\*HX/(AR\*COTHA)\*(1.-PA)
GO TO 100 DABK-DSQRT(AB2+ZA2\*ER2)\*HY IF(DABK.GT.100.) GO TO 9 AB=DEXP(DABK)

DO 12 M-1, MAX 2A-(M-0.5) \*PI 7

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09-A

(F(DABS(BR).LT.EPE) GO TO 1

	Z	IF(AKCTHA.GT.BHCTHB) GO TO 32
	PAR PAR	EY2=0.
	Dabh-dsgrt (ab2+za2*fr2) *HX	FY2=0.
	IF(MABH.GT.100.) GO TO 19	ZA=(II-0.5)*PI
77	EX==EX3 - FMR*EX/(AB+1./AB)*(BK2+ZA2)*(BK2+ZA2))	ZA2-ZA*ZA
67	*	PWR=~PWR
	PA=1.+AKCTHA/5.iCTHB@(PB=1.)	PZ=PWR*ZA/((BK2+ZA2)*(BK2+ZA2)) FX3-FX3-FX
	CF(2,2)=0.5*HY/(BR*COTHB)*(1Pb)	DABH=DSORT (AB2+ZA2*FR2)*HX
		AB-1.
~	EPBK-DEXP(BK)	IF(DABH.GT.100) GO TO 30
	EPBKI=1./EPBK	EPABH=DEXP(DABH)
	BK+EPBKI)	
	PBKI)	30 EY2=EY2-PZ*AB
	COTHA=DSIGN(C1, AR)	PB=1EY2/FY2
	AKCTHA=AK*COTHA	
	BHCTHB=BH*COTHB	CF(2,2)=0.5*HY/(BK*COTHB)*(1PB)
	TEXAMEN TO DESCRIPTION OF THE PROPERTY OF THE	12 EX2=0.
	MATERIAL OF THE PROPERTY OF TH	ZA=(II-0.5) *PI
	DO 20 II=1, MAX	ZA2=ZA*ZA
	ZA=(II-0.5)*PI	PWRPWR
	ZA2=ZA*ZA	DABK=DBK-DSQRT (AB2+ZA2*ER2) *HY
	PWR=:PWR	IF(DABS(DABK).GT.100.) GO TO 39
	((AH2+2A2) * (AH2+2A2))	
		33 EX2=EX2=PWK=ZA=AB/((AHZ+ZAZ)*(AHZ+ZAZ))
	DSQKT (ABZ+ZAZ=EKZ) *HI	
	TECHNIC OF ACT OF	CF(2,2)=0.54HY/(BR4COTHB)+(1,-PB)
	If (UMBN: GILOU)	GO TO 100
	AB-1COSHB (EPABK)	
20	EX3=EX2-PZ+AB	4 DAK-DABS(AK)
	PA=1EX2/FX2	DBH=DABS (BH)
		COTHA = DSIGN(CI, AR)
	CF(2,2)=0.5*HY/(BR*COTHB)*(1PB)	COTRB=DSIGN(C1, BK)
5	40 TO TOO	3
•	D. 2-1 T=1 MAV	PR=1DBH/DAK
	23 = 1 1 - 1,114.	CF(2,2)=0,5*HX/(AR*COTHA)
	ZA2=ZA=Z	GO TO 100
	O	
	*HX	41 PB=0.
	11F (DASS (DASH), GT.100.) GO TO 29	PA=1DAK/DBH CE(2.2)-0.5+UV/(BD+COTHB)
ç	AD-UEKK (ANABA) 823-823-823-823-828 (ABM34-883) (ABM34	Cr(2,2)=0.5-ni/ (px=Coing)
3 6		100 OmlPA-PB
•		
	CF(2,2)=0.5+HV(BR*COTHB)*(1,-PB)	TANHB=1./COTHB
		BE=0.5*(1TANHA)
		BW=0.5*(1.+TANHA)
~	EPAH-DEXF(AH)	BN=0.5*(1TANHB)
	COSHARD 44/EDAN+EDAH)	CF(1.1) **BS**B**O
	COTHA 2 . COSHA ( EPAH I)	CF(3,1)=BS+BE+Q
	COTHB-DSIGN(C1, BR)	
	AKCTHA*AK*COTHA	CF(3,3) -BN+BE+Q
	BHCTHB=BH+COTHB	CF(2,1)=BS*PA
		40+Ma1 \C C/60

19-A

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PR(I,1)=((YP(I,3)-YP(I,1))*PR(I,2)-(YP(I,2)-YP(I,1))
*PR(I,3))/(YP(I,3)-YP(I,2))
       BB(J)=BCV(I,J)+BCV(I-1,J)+BCV(I,J)+BCV(I,J-1)
CC(J)=-BCV(I,J)
100 DD(J)=BCV(I,J)*PR(I+1,J)+BCV(I-1,J)*PR(I-1,J)
1 DD(J)=BCV(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   DO 700 I=1,IP1
DO 700 J=1,JP1
PR(I,J)=PRO(I,J)+RFP*(PR(I,J)-PRO(I,J))
                                                                                                                                                                                          CALL TRIDAG (JAP, JMAX, AA, BB, CC, DD, T)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       DO 999 J=1,JP1
999 PR(IP1,J)=PR(IMAX,J)
                                                                                                                                                                                                                                                         DO 200 J-JAP, JMAX
                                                                                                                                                                                                                                                                                                    200 PR(I,J)-T(J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          500 CONTINUE
600 CONTINUE
400 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             700
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Ü
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          U
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           IMPLICIT REAL-8 (A-H,O-Z)

COMMON PRES1/PRO(90,53), PP(90,53), PR(90,53)

COMMON/PRES1/BCU(90,53), BCV(90,53), DC (90,63)

COMMON/WASS1/DH(90,53), DC (90,53), DF (90,53)

COMMON/WASS1/DH(90,53), DC (53), DD (53), DD (53), DC (90,63), DC (90,63), DC (90,63), DC (90,53), 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ontendentendentendentendentendentendentendentendentendentenden
CALCULATE THE GEOMETRIC CONSTANTS.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     B22=XXI:R
G11=XXI:XXI+YXI:YXI
G12=XYI:YYETXETXXX
G12=XXI:YYETXXX:XXET
G12=XXI:YYETXX:XXET
G12=XXI:YYEYETXX:XXET
G12:XX:YYEYETXX:XXET
G12:XX:YYEYEX
A11=G12:R*R
A12=G1:G11:R*R
A12=G1:G12:R*R
A11=DSGRT(G1)
                                                                                                                                                                                                                                                                                                                                                                                                   IMPLICIT REAL*8(A-H,O-Z)
COMMON/BODY1/B11,B12,B21,B22
COMMON/BODY2/G11,G12,G22,A11,A12,A22,G,AJ1
COMMON/BODY3/XXI,YXI,XET,YET,R
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              DO 400 ITERG=1,10
DO 600 II=2,IMAX
I=IMAX+2-II
DO 500 ITER=1,ITERP
DO 100 J=JAP,JMAX
AA(3)=-BCV(I,J-1)
                                                                                                                                                                                                                                                                                                                                   SUBROUTINE GEOCOE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        DO 300 I=1,IP1
DO 300 J=1,JP1
PRO(I,J)=PR(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               SUBROUTINE PRESS
CF(1,2)=BW*PB
CF(3,2)=BE*PB
RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             B12=-YXI*R
B21=-XET*R
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          B11-YET-R
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               RFP-0.1D0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ITERP-5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              300
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## Computer Code for Chapter-VII

- 1. Full Body Calculation
- 1-1) Computer Program for the Generation of Body Shape and X-Coordinates
- 1-2) Geometric Data Files
   (Generated by Program 1-1)
- 1-3) Computer Program for the Generation of Boundary-Fitted Coordinates
- 1-4) Computer Program for Input Data for Flow calculation
- 1-5) Computer Program for Flow Calculation by Finite Volume Method

```
WRITE(*,*) 'TYPE 8 FOR 10% THICK ARC AIRFOIL'
WRITE(*,*) 'TYPE 9 FOR 5% THICK ARC AIRFOIL'
                                                                                                                                                                                                                                                                        GRID IN THE FRONT BODY REGION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   X-DIRECTIONAL MAXIMUM NUMBER OF GRID.
                                                                                                                                                                                                                                         X-DIRECTIONAL GRID SPECIFICATION,
                                                                                                                                                                                                                                                                                                                                                                                                THE WAKE REGION
                                                                                                                                                                                                                                                                                                                                                                                                                                                             STARTING POINT OF BODY FRONT
                                                                                                                                                                                                         TRAILING EDGE OF THE BODY.
                                                                                                                            IF(IBODY.EQ.4) GO TO 999
                                                                                                                                                                                                                                                                                                                                    GRID ON THE BODY
                                                                                                                                                                                         GENERATE X-COORDINATES.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           DXBODY=1./FLOAT(M2)
                                                               READ(*,*) IBODY
                                                                                                                                                                                                                                                                                                                                                                                              GRID IN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 IMAX=H1+H2+H3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        DXF(1)-DXBODY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       DO 40 I=2,M1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                IP1=IMAX+1
IM1=IMAX-1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           *********
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      MB=M1+M2+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          BODY FRONT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            X(MB)=1.
                                                                                                                                                                                                                                                                      NUM. OF
                                                                                                                                                                                                                                                                                                                                    NUM. OF
                                                                                                                                                                                                                                                                                                                                                                                              NUM. OF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              X (MA) =0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            MA-M1+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     IMA=HA
IMB=HB
                                                                                                                                                                                                                                                                                                                                                                 M2=100
                                                                                                                                                                                                                                                                                                     M1=20
                                                                                                                                                                                                                                                                                                                                                                                                                              M3=30
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                  * AXISYMMETRIC AND TWO-DIMENSIONAL BODIES.
                              NUMERICAL GENERATION OF BODY SHAPES AND X - COORDINATES OF AXISYMMETRIC AND TWO DIMENSIONAL BODIES FOR LAMINAR AND TURBULENT FLOW CALCULATION.
                                                                                                                                                                                                                                                                                                                                                                                                            IBODY=1; AFTERBODY1 OF DTNDSRDC (TURBULENT).
IBODY=2; AFTERBODY2 OF DTNDSRDC (TURBULENT).
IBODY=3; AFTERBODY5 OF DTNDSRDC (TURBULENT).
IBODY=5; AFTERBODY5 OF DTNDSRDC (TURBULENT).
IBODY=6; 6 TO 1 RE-MODIFIED SPHEROID (TURBULENT).
IBODY=7; F57 BODY (TURBULENT).
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        WHAT KIND OF BODY DO YOU WANT ?'
TYPE 1 FOR AFTERBODY OF DINSRDC'
TYPE 2 FOR AFTERBODYS OF DINSRDC'
TYPE 5 FOR AFTERBODYS OF DINSRDC'
TYPE 5 FOR AFTERBODYS OF DINSRDC'
TYPE 6 FOR 6 TO 1 RE-MODIFIED SPHEROID'
TYPE 7 FOR F57 BODY'
                                                                                                                         IMPLICIT REAL*8(A-H,O-Z)
CHARACTER*7 FNAME(10)
COMBON/ABA/X(200), RX(200)
COMBON/ABC/DDY[200), DXM(200)
DATA FNAME(1)/'A1BODY'/,FNAME(2)/'A2BODY'/,FNAME(4)/'A4BODY'/,FNAME(4)/'A4BODY'/,FNAME(4)/'A4BODY'/,FNAME(4)/'A4BODY'/,FNAME(4)/'A4BODY'/,FNAME(4)/'A4BODY'/,FNAME(4)/'A4BODY'/,FNAME(6)/'A4BODY'/,FNAME(6)/'A4BODY'/,FNAME(6)/'A4BODY'/,FNAME(6)/'A4BODY'/,FNAME(6)/'A4BODY'/
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ; 10% THICK ARC AIRFOIL (LAMINAR).
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    IBODY=10 ; FLAT-PLATE (TURBULENT). IBODY=11 ; FLAT-PLATE (LAMINAR).
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             *********************
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           READ BODY TYPE FROM THE TERMINAL.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ****************
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         TWO-DIMENSIONAL BODIES
                                                                                                                                                                                                                                                                                                                                                                 AXIS INDIETRIC BODIES.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 PI-3.141592654D0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      WRITE(*,*)
WRITE(*,*)
WRITE(*,*)
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WRITE(*,*)
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       I BODY = 8
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        IBODY=9
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ELSE IF(X(I).LT.1.DO) THEN  WRITE(*,*) 'AFTERBODY1'  WRITE(*,*) X(I)  READ(*,*) X1,X1,X2,Y2  RX(I)=Y1+(Y2-Y1)/(X2-X1)*(X(I)-X1)	C ELSE RX(I)=0.DO END IF	110	C GENERATE AFTERBODY2. C GRASSESSESSES	ELSE IF(IBODY.EQ.2) THEN  C XARC=0.3D0  RMAX=0.0456D0  RADIUS=1.D0/(2.D0*RMAX)*(RMAX**2+XARC**2)		ELSE IF(X(1).LE.O./952)THEN RX(I) "RMAX ELSE IF(X(I).LT.1.DO) THEN C	WRITE(*,*) 'AFTERBODY2' WRITE(*,*) X(I) READ(*,*) X1,X1,X2,Y2 RX(I)=Y1+(Y2-Y1)/(X2-X1)*(X(I)-X1) C	ELSE RX(I)=0.DO END IF C 120 CONTINUE	C statementations C CENERATE AFTERBODY3.	ELSE IF(IBODY.EQ.3) THEN  RMAX=0.0456  XARC=0.3D0  RADIUS=1.D0/(2.D0*RMAX)*(RMAX**2+XARC**2)  C	DO 130 1=1,IP1 IF(X(I).LE.0.DO) THEN RX(I)=0.DO ELSE IF(X(I).LE.0.3DO) THEN RX(I)=RMAX-RADIUS+DSQRT(RADIUS**2-(X(I)-XARC)**2) ELSE IF(X(I).LE.0.864811) THEN
IP(I.LE.5) THEN RATIO-1. ELSE RATIO-1.3 END IF	40 DXF(I)-DXF(I-1)*RATIO DO 50 I-1.M1	50 X(MA-I)-X(MA-I+1)-DXF(I)	ON THE BODY.	60 X(MA+I)-DXBODY+X(MA+I-1) Assessanssan ON THE WAKE.	DXM(1)=DXBODY  DO 61 I=2,M3  IF(I.LE.10) THEN	RATIO-1.3 RATIO-1.3	61 DXW(I)-DXW(I-1)*RATIO DO 70 I-1,H3 70 X(MB+I)=X(MB+I-1)+DXW(I)	_	GENERATE AFTERBOY1.  ***********************************		IF(X(I).LE.O.DO) THEN RX(I)=0.DO RLSE IF(X(I).LE.O.3DO) THEN RX(I)=RMAX-RADIUS+DSQRT(RADIUS+>2-(X(I)-XARC)+>2) RX(I)=RMAX-RADIUS+DSQRT(RADIUS+>2-(X(I)-XARC)+>2) RX(I)=RMAX

.50 CONTINUE	errerrerrerrerrerrerrerrerrerrerrerrerr	ELSE IF(IBODY.EQ.6) THEN	ALENGTH = 164. ARADIUSX = 76.	AKALUSI=12.5 AXCEN=82. AXI=11.	AXT=153.	XLENGTH=1. XRX=ARADIUSX/ALENGTH	XRY=ARADIUSY/ALENGTH XCEN=AXCEN/ALENGTH	XIN=AXI/ALENGTH XTN=AXT/ALENGTH	SLOPE=4.459/11.	[d] [=1 09t 00	(1) X-CX (1)	IT(AT.LI.U.) THEN RX(I)=0.D0	ELSE IF(XT.LE.XIN) THEN RX(I)=SLOPE*XT	ELSE IF(XI.LE.XIN) THEN RX(I)=XRV+DSOBT(1.DG-(XT/XBX-XCBN/XBX)++0)	ELSE IF(XI.E.1.) THEN RX(I)=SLOPE*(1.Do-XI)	ELSE RX(I)=0.	END IF 160 CONTINUE		GENERATE FOT BODY.	ELSE IF(IBODY.EQ.7) THEN	2446	AN-1./(2.*4.2735)	DO 170 I=1, IMAX	XT=X(I) IF(XT.LT.0.) THEN	RX(I)=0.D0 FISH IF(XI LE XM) THEN	AKINININININININININININININININININININ	RX(I)=RM*DSQRT(SUMI) ELSE IF(XT.LE.1.DO) THEN	
150	(x(I)-0.9771)	(0.9811-0.9791)*(X(I)-0.9791) C	+(X(I)-0.9831)	*(X(I)-0.9851)	*(X(I)-0.9871)	*(X(I)-0.9881)	*(X(I)-0.9901)	*(X(I)-0.9920)	(0.9960-0.9940)*(X(I)-0.9940)	.9980-0.9960)*(X(I)-0.9960)	.0000-0.9980)*(X(I)-0.9980)		13 CX			THEN EJ	160 CC	00	υυ	U	v	IUS**2-(X(I)-XARC)**2)	9					
RX(I)=RMAX ELSE IP(X(I).LE.0.977137) THEN BY(Y)=0.07886-0.0106716-0006/	RA(1)-0.023000-0.0190730-2000 RISE IF(X(1)-LE.0.9791) THEN RX(1)-0.0062+(0.0059-0.0062)/ RISE IF (X(1)-LE.0.9811) THEN	ELSE IF(X(I).LE.0.9831) THEN	RX(I)-0:0036*(0:0031-0:0036) RX(I)-0:0051+(0:0050-0:0051) RX(I)-0:0051+(0:0050-0:0051)	ELSE IF(X(1)-LE-U-9871) INEN RX(1)=0.0050+(0.0048-0.0050), ELSE IF(X(1)-LE-0.9681) THEN	RX(I)=0.0048+(0.0046- RLSE IF(X(I).LE.0.990	RX(I)=0.0046+(0.0043- ELSE IF (X(I).LE.0.99	ELSE IF(X(I).LE.0.9940) THEN	RX(I)=0.0040+(0.0036-0.0040)/ ELSE IF(X(I).LE.0.9960) THEN	RX(I)=0.0036+(0.0028-0.0036), ELSE IF(X(I).LE.0.9980) THEN	RX(I)=0.0028+(0.0019-0.0028)/(0.8158 IF(X(I).IT.0.9999999) THEN	RX(I)=0.0000+(0.0000-	RX(I)=0.	END IF		GENERATE AFTERBODYS.	ELSE IF(IBODY.EQ.5) 1		XARC=0.3D0 RMAX=0.0480D0	KADIOSHI. DO/ (Z. DOHNAK) # (KMAX*#Z+XAKC*#Z)	DO 150 I=1, IP1 IF(X(I).LE.0.DO) THEN	RX(I)=0.D0 ELSE IF(X(I).LE.0.3D0) THEN	RX(I) =RMAX-RADIUS+DSQRT (RAD	RX(I)-RMAX	ELSE IF(X(I).LT.1.DO) THEN	WRITE(*,*) 'AFTERBOD'S WRITE(*.*) X(I)	READ(+,+) X1,X1,X2,X2 RX(I)-Y1+(Y2-Y1)/(X2-X1)+(X(I)-X1)	ELSE	RX(I)=0.D0 END IF

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RX(I)=AN1+DSQRT(AN2*AN2~(XT-0.5)**2)
END IF
                                                                                                                                                                                                                                                         RX(I)+AN1+DSQRT(AN2*AN2-(XT-0.5)**2)
END IF
                                                                                                                                                                                                   DO 180 1=1, IP1
XT=X(I)
IF(XT.LE.O.DO.OR.XT.GE.1.DO) THEN
RIX(I)=0.DO
                                                                                                                                                                                                                                                                                                                                                                                                                   XT=X(I)
IF(XT:LE.O.DO.OR.XT.GE.1.DO) THEN
RX(I)=O.DO
                                                                                              GENERATE 10% THICK ARC AIRFOIL.
                                                                                                                                                                                                                                                                                                GENERATE S& THICK ARC AIRFOIL.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   OPEN(UNIT-7, FILE-FNAME(1BODY))
WRITE(7,1111)(X(I),I=1,IP1)
WRITE(7,1111)(RX(I),I=1,IP1)
WRITE(5013.6)
CLOSE(7)
                                                                                                                                                           AM=0.1
AN1=1./2./AH*(AH*AM=0.25)
AN2=1./2./AM*(AM*AH+0.25)
                                                                                                                                                                                                                                                                                                                                                              AM=0.05
AN1=1./2./AM*(AM*AM=0.25)
AN2=1./2./AM*(AM*AM+0.25)
                                                                                                                                       ELSE IF(IRODY.EQ.8) THEN
                                                                                                                                                                                                                                                                                                                                          ELSE IF (IBODY. EQ. 9) THEN
1 +0.17730*AK2**2
RX(I)=RM*DSQRT(SUM2)
ELSE
                                                                                                                                                                                                                                                                                                                                                                                                         DO 190 I=1, IMAX
                                         RX(I)=0.
END IF
CONTINUE
                                                                                                                                                                                                                                                                            CONTINUE
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EF-00-0.360150E+00-0.278577E+00-0.21
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EF-01.0.500000E-01.0.0630000E-01.0.50
EF-01.0.500000E-01.0.0630000E+00.0.10
EF-01.0.500000E-01.0.070
EF-00.0.110000E+00.0.120000E+00.0.13
EF-00.0.230000E+00.0.120000E+00.0.13
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EF-00.0.3510FE+01.0.354014E+01.0.48 0.000000E+00 0.000000E+00 0.000000E+00 0.166601E-01 0.394251E-01 0.384251E-01 0.456000E-01 0.0000000E+00 0.0000000E+00 0.0000000E+00 0.0000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.141589E-01 0.371957E-01 0.45500E-01 0.456000E-01 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 .222472E+01-0
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"a2body"

file

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.200000E-01-0.100000E-01 0.000000E+00 0.10 .400000E-01 0.500000E-01 0.60000E-01 0.20	0.120000E+00	0.180000E+00	0.240000E+00	0.300000E+00	.150000E+00 0.160000E+00 0.3	0.420000E+00	0.540000E+00	0.600000E+00	0.660000E+00	0.720000E+00	0.780000E+00	0.840000E+00	0.900000E+00	0.960000E+00	. INTOCOE+O1 O. INTOCOE+O1 O. I	0.1180418+01	0.165405E+01	.327472E+01 0.394014E+01 0.4		0.000000E+00	00000008+00 0.0000008+00 0.00	0.0000000000000000000000000000000000000	0.166603E-01	0.294251E-01	0.384434E-01	.431/USE-UI 0.438156E-UI 0.4/ .455505E-OI 0.4%6000E-UI 0.4/	0.456000E-01	0.456000E-01		0.456000E-01	.456000E-01	0.456000E-01 0.	456000E-01 0.456000E-01 0.4	0.367762E-01 0.	0.842924E-02	0.00000E+00	0.000000E+00	0.000000E+00 0.000000E+00 0.00	0.000000E+00		t ortoractoret ortoraset	-u,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	-0.101870E+00-0.7990U0E-01-0.630000E-01-0.500000E-01-0.400000E-	-0.200000E-01-0.100000E-01 0.000000E+00 0.100000E-01

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IBODY=3 IBODY=5 IBODY=6 I BODY=7

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IBODY=8

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DO 10 J=4,JP1 IF(J.LE.6) THEN	ELSE C IF(IBODY.EQ.6.OR.IBODY.EQ.7) THEN	RATIO=1.20 ELSE RATIO=1.30 END IF C END IF	10 DY1(J) *DY1(J-1) *RATIO	ELSE C · FOR LAMINAR FLOW CALCULATION.	_	DY1(1) = 0.  DY1(2) = DYWALL  DY1(3) = DY1(2)	C DO 20 J=4,JP1 RATIO=1.25 20 DY1(J)=DY1(J-1)*RATIO	END IF	C C GRID NUMBER OF CENTER OF BODY.		THUELTHAY (IND-TRA) = 0.5 C Y (IMC, 1) = RX (IMC)	DO 82 J=2,JP1 82 Y(IMC,J)=Y(IMC,J-1)+DY1(J) C	C GENERATE INITIAL GRID IN THE WHOLE DOMAIN.		DO 90 J=1,NRP 90 FR(J)=(Y(IMC,J)-RX(IMC))/(DELTA-RX(IMC))	DO 91 I=1, IP1 Y(I, 1)=RX(I) Y(I, NRP)=DELTA 91 CONTINUE	C DO 750 I=1,IP1 DO 751 J=2,NRP 751 Y(I,J)=Y(I,1)+FR(J)*(DELTA-Y(I,1))	
IMA=ML-1 IMB=MT+1	**************************************	OPEN(UNIT=7, FILE=FINAME(IBODY)) READ(7,1111)(X(I),I=1,IP1) READ(7,1111)(RX(I),I=1,IP1) I FORMAT(6D13.6) CLOSE(7)	MODIFY THE LEADING EDGE AND TRAILING EDGE.	RX(NL)=1.D0/3.D0*RX(NL+1) RX(NT)=1.D0/3.D0*RX(NT-1)	OPEN(UNIT=10, FILE=F2NAME(IBODY))	SOME CONSTANTS AND RELAXATION FACTOR.	PI=3.141592653589793D0 EPS=0.001 RF=1.8	MAXIMUM NUMBER OF ITERATIONS.	ITMAX-200	NUMBER OF GRID IN Y-DIRECTION.	JOHAN-1 JOHAN-JHAX+1 JOHAN-JHAX-1	NUMBER OF GRID IN Y-DIRECTION WHERE CRID IS ORTHOGONAL.	NRP=JHAX-5	SENERATE Y-DIRECTIONAL GRID AT THE CENTER OF BODY.		. 1. OR. IBODY. EQ. 2. OR. . 5. OR. IBODY. EQ. 6. OR	FFLOS=40.50 DY1(1)=0. DY1(2)=YPLUS/RE/UTAU	

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SY=0.5*Al2(I,J)*(Y(I+1,J+1)+Y(I-1,J-1)-Y(I+1,J-1)-Y(I-1,J+1))
AY(J)=-2.*Al2(I,J)*EFB*A2/(EPB-1./EPB)
BY(J)=-2.*Al1(I,J)*Al*(EPA+1./EPA)/(EPA-1./EPA)
1 +2.*Al2(I,J)*Al*(EPA+1./EPB)/(EPB-1./EPB)
CY(J)=-2.*Al2(I,J)*Al*(EPB+1./EPB)/(EPB-1./EPB)
DY(J)=-2.*Al2(I,J)*Al/(EPA-1./EPB)
2 +Y(I+1,J)/EPA)*SY
502 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       PRINT 999, IT, DRMAX
999 FORMAT(5X, 'NO. OF ITERATION = ', I5, 5X, 'DRMAX=', D12.4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      SPECIFY BOUNDARY CONDITIONS.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            PRINT OUTPUT IN EACH ITERATION PROCESS.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               WRITE(10,189) IT, DRMAX
FORMAT(5X,'IT=',IS,5X,'DRMAX=',D12.4)
                                                                                                                                                                                                                                                                                                                                       DY (JMAX) = DY (JMAX) - CY (JMAX) +Y (I, JP1)
                                                                                                                                                                                                                                                                                                                                                                         CALL TRIDAG(2, JMAX, AY, BY, CY, DY, TY)
                                                                                                                                                                                                                                                                                                                                                                                                                              YDIFF-DABS(TY(J)-Y(I,J))
IF (YDIFF.CT.DRMAX) DRMAX-YDIFF
Y(I,J)-Y(I,J)+RF*(TY(J)-Y(I,J))
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           SPECIFY THE BOUNDARY CONDITIONS
                                                                                                            IF(DABS(A2).LT.EPS) A2 EPS
EPB DEXP(A2)
                IF(DABS(A1).LT.EPS) A1*EPS
EPA*DEXP(A1)
                                                                                                                                                                                                                                                                                                                     DY (2) -DY (2) -AY (2) +Y (I, 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Y(1,J)=Y(2,J)
Y(IP1,J)=Y(IMAX,J)
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                F1(1)=F1(2)
F1(IP1)=F1(IMAX)
                                                                                                                                                                                                                                                                                                                                                                                                            DO 501 J=2,JMAX
                                                                          DO 502 J=2, JMAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               DO 130 J=1,JP1
                                                                                              A2=F2(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       500 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   CONTINUE
A1=F1(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  189
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   300
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    501
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      U
                                                                                                                                                                                                                                                                                                                                                                  DO 110 J=2,JMAX

DO 110 I=2,IMAX

F2(I,J)=(F2(IMC,J)*(RD(IMB)-RD(I))+F2(IP1,J)*(RD(I)-RD(IMC)))

1 /{RD(IMB}-RD[IMC))

IF(I.GT.IMB) F2(I,J)=F2(IP1,J)

110 CONTINUE
                                                                                                                                                                                                                                                           107 F2(IP1,J)=(Y(IMB,J+1)+Y(IMB,J-1)-2.*X(IMB,J))
1 /(Y(IMB,J+1) -Y(IMB,J-1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            297 F1(I) = (X(I+1) + X(I-1) - 2 \cdot *X(I)) / (X(I+1) - X(I-1))
                                                                                                                                                                                                        F2(IMC, J) = (Y(IMC, J+1) +Y(IMC, J-1) -2. *Y(IMC, J))
/(Y(IMC, J+1) -Y(IMC, J-1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 START ITERATION PROCESS FOR GRID GENERATION.
                                                                                                                                                    F2(1,J)=(Y(1,J+1)+Y(1,J-1)-2.*Y(1,J))
/(Y(1,J+1)-Y(1,J-1))
                                    Specify THE GRID CONTROL FUNCTIONS.
                                                                          WRITE(10,2005) (Y(IMC,J),J=1,JP)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       YET=0.5*(Y(I,J+1)-Y(I,J-1))
G11=XXI*XXI+YXI*XXI
G22=XET*XET+YET*YET
G12=XXI*XET+YXI*YET
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      XXI=0.5*(X(I+1)-1(I-1))
YXI=0.5*(Y(I+1,J)-Y(I-1,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       G=(G11*G22-G12*G12)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            DO 300 IT=1,ITMAX
                                                                                                                                                                                                                                                                                                                                       RD(I)-DELTA-RX(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     AJ(I,J)=DSQRT(G)
All(I,J)=G22/G
A22(I,J)=G11/G
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            A12(I,J)=-G12/G
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        DO 297 I=2, IMAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  DO 100 I-2, IMAX
DO 100 J-2, JMAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    DO 500 I=2, IMAX
                                                                                                                DO 107 J-2, JHAX
                                                                                                                                                                                                                                                                                                                     DO 108 I-1, IMAX
   750 Y(I,J)-Y(IMC,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  DRMAX-0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               100
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SUBROUTINE TRIDAG(IF, L, A, B, C, D, V)
IMPLICIT REAL*8(A-H, O-Z)
DIMENSION A(10), B(70), C(70), D(70), V(70), BETA(70), GAMMA(70)
BETA(IF) = B(IF)
GAMMA(IF) = D(IF)/BETA(IF)
                                                                                                                                                                                                                                                                                                                                                             SAVE DATA FOR CALCULATION
                                                                                                                                             PRINT OUTPUT AFTER ITERATION PROCESS
                                                       REARRANGE DATA
                                             OPEN(UNIT=11,FILE=F3NAME(IBODY))
WRITE(11,2009)((XC(I,J),I=1,IP1),J=1,JP1)
WRITE(11,2009)((YC(I,J),I=1,IP1),J=1,JP1)
CLOSE(11)
                                                                                                                                                                                         DO 302 I=1,IP1
WRITE(10,601) I,X(I)
FORMAT(5X,'STATION',IS,5X,'X =',F8.4)
WRITE(10,2005)(Y(I,J),J=1,JP1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             V(I) =GAMMA(I) -C(I) *V(I+1)/BETA(I)
RETURN
                                                                                                                                                                                                                                                                                            DO 250 J=1,JP1
250 WRITE(10,2005)(Y(I,J),I=1,IP1)
2005 FORMAT(4D14.6)
                                                                                                                                                                                                                                             WRITE(10,2007)(X(I),I=1,IP1)
2007 FORMAT(6F12.8)
C
DO 301 J=1,JP1
F2(1,J)=F2(2,J)
F2(IP1,J)=F2(IMAX,J)
                                                                                        DO 123 I=1, IP1
DO 123 J=1,JP1
YC(I,J)=Y(I,J)
XC(I,J)=X(I)
                                                                                                                                                                                                                                                                                                                                         CLOSE (10)
                                                                                                                                                                                                                                       302 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             STOP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        END
                       301
                                                                                                                          123
                                                                                                                                                                                                                  601
                                                                                                                                                                                                                                                                                                                                                                                                                                            2009
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AXISYMMETRIC AND TWO-DIMENSIONAL BODIES.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  IBODY-1; AFTERBODY1 OF DTNDSRDC (TURBULENT).
IBODY-2; AFTERBODY2 OF DTNDSRDC (TURBULENT).
IBODY-3; AFTERBODY3 OF DTNDSRDC (TURBULENT).
IBODY-5; AFTERBODY5 OF DTNDSRDC (TURBULENT).
IBODY-6; 6 TO 1 RE-MODIFIED SPHEROID (TURBULENT).
IBODY-7; F57 BODY (TURBULENT).
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       1 10% THICK ARC AIRFOIL (LAMINAR).
1 5% THICK ARC AIRFOIL (LAMINAR).
                                                                                                                                                                                                                                                                       FSNAME (1) / 'Aldat' /, FSNAME (2) / 'A2DAT' /, FSNAME (3) / 'A3DAT' /, FSNAME (4) / 'A6DAT' /, FSNAME (5) / 'A6DAT' /, FSNAME (6) / 'A6DAT' /, FSNAME (8) / 'A6DAT' /, FSNAME (9) / 'A0DAT' /, FSNAME (9) / 'A0DAT' /, FSNAME (10) / 'A0DAT' /, FSNAME (10) / 'A0DAT' /, FSNAME (10) / 'A0DAT' /
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   IBODY-10 , FLAT-PLATE (TURBULENT).
IBODY-11 ; FLAT-PLATE (LAMINAR).
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             TWO-DIMENSIONAL BODIES.
                                                                                                                                                                     IMPLICIT REAL*8(A-H,O-Z)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        AXISYMMETRIC BODIES.
                                                                                                                                                                                                                          CHARACTER*7 FSNAME(10)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            I BODY=8
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      I BODY=9
                                                                                                                                                                                                                                                                            DATA
```

LEADING EDGE OF THE BODY ( I-M1 ). STARTING CALCULATION POINT OF THE WAKE ( I-M2 ).

NUMBER OF GRID POINTS IN X AND Y-DIRECTION.

IMAX=151

JMAX=36

0000

ELSE IF(IBODY.EQ.6) THEN RENUM=1300000.D0 ELSE IF(IBODY.EQ.7) THEN RENUM=1200000.D0

END IF

000

ELSE IF(IBODY.EQ.3) THEN RENUM=6000000.D0 ELSE IF(IBODY.EQ.5) THEN RENUM=9300000.D0

ELSE IF(IBODY.EQ.2) THEN (F(IBODY.EQ.1) THEN REYNOLDS NUMBERS

RENUM-6600000. DO RENUM-6800000. DO

READ(\*,\*) IBODY

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LAMINAR (IFLOW=1) OR TURBULENT FLOW (IFLOW=2).

IFLOW=2

M2=122

000

```
TURBULENT INTENSITY AND LENGTH SCALE
         2-DIMENSIONAL BODY (ICORD-1)
                                                                                          TUSCALE=0.001D0
                                                                                                                                                                                      URFVIS=0.8D0
URFPR=0.5
                                                                                                                                                 URFV-0.7D0
URFK-0.8D0
                                                                                                                                                                            URFD-0.8D0
                                                                              TURBIN-0.5
                                                                                                                                        URFU=0.7D0
                                                                                                                                                                                                                                                ITMAX=500
                                 ICORD-2
                                                                                                                                                                                                                                                             NINER-3
ບບບ
                                             000
                                                                                                       000
                                                                                                                                                                                                               ບບບ
                                                                                                     YPE 1 FOR AFTERBODY DO YOU WANT ?'
YPE 2 FOR AFTERBODY OF DINSRC'
'PE 3 FOR AFTERBODY OF DINSRC'
'PE 5 FOR AFTERBODY OF DINSRC'
'E 6 FOR 6 TO 1 RE-MODIFIED SPHEROID'
'E 7 FOR F57 BODY'
' @ FOR 10% THICK ARC ATTACH
                                                                                                                                                    *******************
                                                                                                                                                              READ BODY TYPE FROM THE TERMINAL.
```

TYPE TYPE TYPE TYPE TYPE TYPE

WRITE(\*,\*)
WRITE(\*,\*)
WRITE(\*,\*)
WRITE(\*,\*)

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WRITE(\*,\*) WRITE(\*,\*)

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WRITE(\*, \*)

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MAXIMUM ITERATION (ITMAX) AND INNER ITERATION (NINER).
UNDER-RELAXATION FACTORS
                                                                                                                                                                                                                                                                             NUMBER OF SWEEPS.
                                                                                                                                                                                                                            ITOUT-100
                                                                                                                                                                                                                                                000
```

OR AXISYMMETRIC BODY (ICORD=2).

NSWPU-5
NSWPV-5
NSWPW-5
NSWPW-5
NSWPW-5
NSWPW-5
NSWPW-5
NSWPW-5
NSWPW-6
C SAVE DATA FOR THE FLOW CALCULATION.
C WRITE(12,1) IMAX,JMAX,M1,M2
1 FORMAT(415)
2 FORMAT(215)
2 FORMAT(215)
C WRITE(12,3) REWUM,TURBIN,TUSCALE
C WRITE(12,4) ITMAX,NINER,ITOUT
4 FORMAT(315)
C WRITE(12,5) URFU,URFK,URFD,URFVIS,URFPR
5 FORMAT(677.3)
C WRITE(12,5) NSWPU,NSWPW,NSWPK,NSWPD
C CLOSE(12)
C CLOSE(12)
STOP
END

)

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PROGRAM HAWKEYE

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                                                                                                                                                                                                                                                                                                                                                             化非常有效的 医克克特氏 医克克特氏 医克克特氏 医克克特氏 医克克特氏 医克克特氏 医克克特氏 医克克特氏 医克克特氏病
                                                                                                                                                                                                        READ(12,5) URFU, URFV, URFK, URFD, URFVIS, URFPR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   PRED=CAPPA*CAPPA/(C2-C1)/(CMU**0.5D0)
                                                                                                                                                                                                                                                          READ(12,6) NSWPU, NSWPV, NSWPK, NSWPD
                                                                                                  READ(12,3) RENUM, TURBIN, TUSCALE FORMAT(3E12.4)
                                                                                                                                                    READ(12,4) ITMAX,NINER,ITOUT
FORMAT(315)
READ(12,1) IMAX,JMAX,M1,M2
FORMAT(415)
                                                  READ(12,2) IFLOW, ICORD FORMAT(215)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       NUMBER OF ITERATIONS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              TURBULENT CONSTANTS.
                                                                                                                                                                                                                                                                                                                                                                                                GEOMETRIC CONSTANTS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     NITER-O
MAXIT-NITER+ITMAX
ITPR-1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           FLUID PROPERTIES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           VISCOS=1./RENUM
                                                                                                                                                                                                                          FORMAT (6F7.3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            PRANDT=0.9D0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                CAPPA=0.4187
ELOG=9.793
                                                                                                                                                                                                                                                                                                                                                                                                                                                JP1=JMAX+1
JPP1=JMAX+2
IM1=IMAX-1
                                                                                                                                                                                                                                                                             FORMAT (415)
                                                                                                                                                                                                                                                                                                                                                                                                                                 IP1-IMAX+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  JM1=JMAX-1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   M2M1=M2-1
M2P1=M2+1
M1M1=M1-1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            DENSIT-1.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     MIPI=MI+1
                                                                                                                                                                                                                                                                                                            CLOSE(12)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             CMU=0.09
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                C1-1.44
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   C2=1.92
                                                                                                                                                                                                                          S
                                                                                                                                                                                                                                                                             ø
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          000
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                                                                                      U
                                                                                                                                                                                                                                                                                             U
                                                     A MAIN PROGRAM
                                                                                                                                                      * AXISYMMETRIC AND TWO-DIMENSIONAL BODIES.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      在我也是我的现在分词,我们的我们的,我们的是我们的,我们的我们的,我们的我们的,我们的我们的,我们的我们的,我们的我们的,我们的我们的,我们的我们的,我们的我们的
                                                                                                                                         AT KIND OF BODY DO YOU WANT ?'
PE 1 FOR AFTERBODY1 OF DTHSRDC'
PE 2 FOR AFTERBODY2 OF DTHSRDC'
PE 5 FOR AFTERBODY3 OF DTHSRDC'
PE 5 FOR AFTERBODY3 OF DTHSRDC'
PE 6 FOR 6 TO 1 RE-MODIFIED SPHEROID'
PE 7 FOR F97 BODY'
PE 9 FOR 10% THICK ARC AIRFOIL'
                                                                                                                                                                                                                                                            [BODY=1 ; AFTERBODY1 OF DTNSRDC (TURBULENT).

[BODY=2 ; AFTERBODY2 OF DTNSRDC (TURBULENT).

[BODY=3 ; AFTERBODY3 OF DTNSRDC (TURBULENT).

[BODY=5 ; AFTERBODY5 OF DTNSRDC (TURBULENT).

[BODY=6 ; 6 TO 1 RE-MODIFIED SPHEROID (TURBULENT).

[BODY=7 ; F57 BODY (TURBULENT).
```

1 108 THICK ARC AIRFOIL (LAMINAR).

I BODY=8 I BODY=9

\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\* TWO-DIMENSIONAL BODIES

AXISYMMETRIC BODIES.

IBODY=10 ; FLAT-PLATE (TURBULENT). IBODY=11 ; FLAT-PLATE (LAMINAR).

READ BODY TYPE FROM THE TERMINAL.

. TYPE . TYPE . TYPE . TYPE . TYPE . TYPE

WRITE(\*,\*)
WRITE(\*,\*)
WRITE(\*,\*)

WRITE(\*, \*)

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WRITE(\*,\*) WRITE(\*,\*) WRITE(\*,\*)

WRITE(\*,\*)

\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\* READ INPUT DATA FROM FILE (FSNAME)

0 0 0 0 0

READ(\*,\*) IBODY

9 L - Y

DATA

FSNAME(1)/'A1DAT'/,FSNAME(2)/'A2DAT'/, FSNAME(3)/'A1DAT'/,FSNAME(4)/'A6DAT'/, FSNAME(5)/'A5DAT'/,FSNAME(6)/'A6DAT'/, FSNAME(7)/'A7DAT'/,FSNAME(10)/'A0DAT'/, FSNAME(9)/'A9DAT'/,FSNAME(10)/'A0DAT'/

OPEN (UNIT-12, FILE-F5NAME (IBODY))

```
XE(1,J) = 0.5* (XC(1,J) + XC(1,J-1))

XN(1,J) = 0.5* (XC(1,J) + XC(1-1,J))

XR(1,J) = 0.25* (XC(1,J) + XC(1,J-1) + XC(1-1,J) + XC(1-1,J-1))

YE(1,J) = 0.5* (YC(1,J) + YC(1,J-1))

YR(1,J) = 0.5* (YC(1,J) + YC(1-1,J))

YR(1,J) = 0.25* (YC(1,J) + YC(1,J-1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   XC(IP1,J)=XC(IMAX,J)+0.5*(XC(IMAX,J)-XC(IMAX-1,J))
XE(IP1,J)=XC(IP1,J)
XR(IP1,J)=XC(IP1,J)
XR(IP1,J)=XC(IP1,J)
YC(IP1,J)=YC(IMAX,J)
YC(IP1,J)=YC(IMAX,J)
YE(IP1,J)=YE(IMAX,J)
XR(IP1,J)=YE(IMAX,J)
XR(IP1,J)=YE(IMAX,J)
XR(IP1,J)=YE(IMAX,J)
                                                                                                    XE(I,1)=XC(I,1)
XN(I,1)=0.5*(XC(I,1)+XC(I-1,1))
XP(I,1)=0.5*(XC(I,1)+XC(I-1,1))
YE(1,J)=0.5*(YC(1,J)+YC(1,J-1))
YN(1,J)=YC(1,J)
YP(1,J)=0.5*(YC(1,J)+YC(1,J-1))
                                                                                                                                                                                         YN(I,1)=0.5*(YC(I,1)+YC(I-1,1))
YP(I,1)=0.5*(YC(I,1)+YC(I-1,1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       RADIUS FOR AXISYMMETRIC BODY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          DO 117 I=1, IP1
DO 117 J=1, JP1
IF(ICORD.EQ.1) THEN
R(I,J)=1.D0
ELSE IF(ICORD.EQ.2) THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              YE2(I)-YE(I,2)-YE(I,1)
YE3(I)-YE(I,3)-YE(I,1)
YN2(I)-YN(I,2)-YN(I,1)
YN3(I)-YN(I,3)-YN(I,1)
YP2(I)-YP(I,2)-YP(I,1)
YP3(I)-YP(I,3)-YP(I,1)
                                                                                                                                                                                                                                                                                                                                                                                                                     DO 113 I=2,IMAX

XC(I,JP1)=XC(I,JMAX)

XE(I,JP1)=XE(I,JMAX)

XN(I,JP1)=XN(I,JMAX)

XP(I,JP1)=XN(I,JMAX)

YC(I,JP1)=YC(I,JP1)

YE(I,JP1)=YR(I,JP1)

YN(I,JP1)=YN(I,JP1)

113 YP(I,JP1)=YN(I,JP1)
                                                                                    DO 112 I=2, IMAX
                                                                                                                                                                                                                                                      DO 112 J-2, JMAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   R(I,J)=YC(I,J)
END IF
CONTINUE
                                                                                                                                                                    YE(I,1)=YC(I,1)
YN(I,1)=0.5*(YC
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  DO 115 J=1,JP1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              IdI'1=I 911 00
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              116
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                117
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            O
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    u u u
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                                                                                                                                                                                                                                                                                                                                                                                                    ပ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  XE, YE---- EAST CELL SURFACE CALCULATION POINT (UE, VE).
XN, YN----- NORTH CELL SURFACE CALCULATION POINT (UN, VN).
XP, YP---- CELL CENTER CALCULATION POINT (PR, PP, AKE, ADS).
XC, YC---- CELL CONTROL VOLUME.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     XC(1,JP1)=XC(1,JHAX)
YC(1,JP1)=YC(1,JHAX)+(YC(1,JHAX)-YC(1,JHAX-1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              OPEN(UNIT=11,FILE-FINAME(IBODY))
READ(11,2006)((XC(I,J),I=1,IHAX),J=1,JHAX)
READ(11,2006)((YC(I,J),I=1,IHAX),J=1,JHAX)
CLOSE(11)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    OFFSET OF NUMERICAL GRID.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    OPEN(UNIT-8, FILE-F2NAME(IBODY))
OPEN(UNIT-7, FILE-F3NAME(IBODY))
OPEN(UNIT-9, FILE-F4NAME(IBODY))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       XC(1,J)=0.5*(XC(1,J)+XC(2,J))
YC(1,J)=0.5*(YC(1,J)+YC(2,J))
                                                                                                                                                  TEIN=1.5D0*(TURBIN/100.D0)**2
AIAMDA=TUSCALE*ALENGTH
EDIN=CHU*TEIN**1.5/ALAMDA
                                                                                                                                                                                                                                                                                             OPEN FILES FOR OUTPUT
                                                                                                                                                                                                                                                      PI=3.141592653589793D0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       XE(1,1)=XC(1,1)
XN(1,1)=XC(1,1)
XP(1,1)=XC(1,1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           XE(1,J)=XC(1,J)
XN(1,J)=XC(1,J)
XP(1,J)=XC(1,J)
                                                                 INLET CONDITIONS.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       DO 110 J=1,JMAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           YE(1,1)=YC(1,1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         YP(1,1)=YC(1,1)
YP(1,1)=YC(1,1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         DO 111 J=2,JP1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           FORMAT (6D13.6)
                                                                                                            ALENGTH-1. DO
                                                                                                                                                                                                                                        GREAT-1.030
      PRED=1.3
PRTE=1.D0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  110
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C PRESSURE, PRESSURE CORRECTION FIELD.	C PR(I,J)=0.D0 PRO(I,J)=0.D0 PP(I,J)=0.D0	C KINETIC ENERGY AND DISSIPATION RATE.	AKE(I,J)=0.D0 ADS(I,J)=0.D0	C DENSITY AND VISCOSITY	DEN(I,J)=DENSIT VIS(I,J)=VISCOS	C COEFFICIENTS OF PRESSURE TERM IN C HOMENTUM EQUATIONS.	CXUE(I,J)=0.D0 CYUE(I,J)=0.D0 CXVE(I,J)=0.D0 CXVE(I,J)=0.D0	C CXVIN (1, 3) = 0.00	CXVN(I,J)=0.D0 CXVN(I,J)=0.D0 CYVN(I,J)=0.D0	QXUE(1,J)=0.D0 QXVE(1,J)=0.D0 QXVI(1,J)=0.D0		C COEFFICIENTS OF PRESSURE AND C PRESSURE CORRECTION EQUATION.	BCU(I,J) = 0.D0 BCV(I,J) = 0.D0		C FOR VELOCITY, UE AND VE.		SCVE(I,V)=0.D0 SPVE(I,V)=0.D0	C FOR VELOCITY, UN AND VN.	SCUN(I,J)=0.D0 SPUN(I,J)=0.D0		C FOR KINETIC ENERGY, AKE.	SCK(I,J)=0.D0 SPK(I,J)=0.D0
VOLUME SIZE OF EACH CONTROL VOLUME CELL.	DO 118 1-2, JP1 DO 118 J-2, JP1 IF(ICORD.EQ.1) THEN	VOL(I,J)=0.5*((XC(I,J)-XC(I-1,J))*(YC(I-1,J)-YC(I,J-1)) -(XC(I-1,J)-XC(I,J))*(YC(I,J)-YC(I-1,J-1))	ELSE IF(ICORD.EQ.2) THEN VOL(I,J)=1.DO/6.DO* 1 ((XC(I,J-1)-XC(I,J))	Z m(YC(I,U-I)mmd+YC(I,U)mmZ+YC(I,U-I)mYC(I,U)) 3 + (XC(I,U)-XC(I-I,U)) 5 + (XC(I,U)-XC(I-I,U))	+ (xc(1-1,3) -*2+Yc(1-1,3-1)) + (xc(1-1,3) -*2+Yc(1-1,3-1))	<pre>/ + (XC(I-1,J-1) **2+YC(I,J-1) 8 * (YC(I-1,J-1) **2+YC(I,J-1) **2+YC(I-1,J-1) *YC(I,J-1)))</pre>	.18 CONTINUE DO 119 J=1,JP1 .19 VOL(1,J)=0.D0	DO 120 I-1,IP1 (20 VOL(I,1)-0.D0	standsbetsbetsbetsbetsbets SET VARIABLES TO ZERO.	destretes destretes destretes de la	orace deals from	TAUN(I)=1. DO	DO 14 J=1,JP1	CARTESIAN ( OR CYLINDRICAL ) VELOCITY COMPONENTS.	UE(I,J)=0.D0	VA(I,J)=0.00	PSEUDO-VELOCITY COMPONENTS.	UHE(I,J)=0.D0	UN (I,J) = 0. DO	CONTRAVARIANT VELOCITY COMPONENTS.	UUE(1,J)=0.D0	UCN (I,I) = 0. DO  VVN (I,J) = 0. DO

```
DO 202 J=2,JP1
202 UUE(1,J)=DEN(1,J)*0.5*(R(1,J)+R(1,J-1))*(YC(1,J)-YC(1,J-1))
1 *UE(1,J)=0.
                                                                                                                                                                                                                                                                                       DO 201 J=2,JMAX

ARDEN=DEN(1,J)*0.5*(R(1,J)+R(1,J-1))*(YC(1,J)-YC(1,J-1))

XHONIN=XMONIN+ARDEN*UE(1,J)*UE(1,J)

ARDENT-ARDENT+ARDEN

FLOWIN=FLOWIN+ARDEN*UE(1,J)

UMEAN=FLOWIN/ARDENT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  RETURN POINT OF ITERATION.
                                                                                                                                                                                                   COMPUTE INLET MEAN VELOCITY, MASS FLUX AND MOMENTUM FLUX.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                COMPUTE INLET CONTRAVARIANT VELOCITY.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         DO 19 J=1,JP1
DO 21 I=1,IP1
SPF(I,J)=0.DO
1 PP(I,J)=0.DO
1F(NITER.LT.4) GO TO 19
VE(1,J)=VE(2,J)
VN(1,J)=VN(2,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      INITIAL GUESS FOR YPLUS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  VVN(1,J)=VVN(2,J)
AKE(1,J)=AKE(2,J)
ADS(1,J)=ADS(2,J)
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           DO 205 I=2, IMAX
205 YPLUSN(I)=11.D0
                  AKE(1,J)=TEIN
ADS(1,J)=EDIN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         4000 NITER-NITER+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     RESAK-0.
RESAD-0.
RESIM-0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        RESUE-0.
RESVE-0.
RESUN-0.
                                                                                                    20 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             RESVN=0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      5
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                                                                                                                                                                                                                                                             FOR PRESSURE AND PRESSURE CORRECTION EQUATION.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   OPEN(UNIT-11, FILE-'FVINPUT')
DO 16 I-1,IP1
DO 16 J-1,JP1
DO 16 J-1,JP1
16 READ(11,2008) UE(I,J), VE(I,J), UN(I,J), VN(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            INITIAL PROFILES FROM FILE FVINDUT
IF AVAILABLE
                                                                               FOR DISSIPATION RATE, ADS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ITM=1
IF(ITM.EQ.1) GO TO 15
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        INLET CONDITIONS
                                                                                                                                    SCD(1,J)=0.D0
SPD(1,J)=0.D0
SUDD(1,J)=0.D0
SPDD(1,J)=0.D0
SUKD(1,3)=0.D0
SPKD(1,3)=0.D0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    2008 FORMAT (7E12.4)
                                                                                                                                                                                                                                                                                                                          SPP(I,J)=0.D0
SPR(I,J)=0.D0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           UE(1,3)=UIN
VE(1,3)=0.DO
UN(1,3)=UIN
VN(1,3)=0.DO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        DO 20 J-1,JP1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ARDEN=0.D0
ARDENT=0.D0
XMONIN=0.D0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 UHE(1,3)-UIN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              UHN (1,3) =UIN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 VVE(1,3)=0.
VVN(1,3)=0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       PLOWIN-0. DO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         CLOSE(11)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         15 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                         14 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                      0000000
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IF(ADS(I,J).EQ.0.D0) GO TO 241

STARTING POINT OF INNER ITERATION. VIS(I,J)=CMU\*DEN(I,J)\*AKE(I,J)\*AKE(I,J)/ADS(I,J) +VISCOS 242 VIS(I,J)=URFVIS\*VIS(I,J)+(1.D0-URFVIS)\*VISOLD

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VISS=VIS(I,J)
VIEE=0.25D0*(VIS(I,J)+VIS(I,J+1)+VIS(I+1,J+1)+VIS(I+1,J))
VIEH=0.25D0*(VIS(I-1,J)+VIS(I-1,J+1)+VIS(I,J+1)+VIS(I,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     DESS=DEN(I,J)
DEEE=0.25*(DEN(I,J)+DEN(I,J+1)+DEN(I+1,J+1)+DEN(I+1,J))
DEWN=0.25*(DEN(I-1,J)+DEN(I-1,J+1)+DEN(I,J+1)+DEN(I,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               AKEE-0.25*(AKE(1,3)+AKE(1,3+1)+AKE(1+1,3+1)+AKE(1+1,3)
AKWW-0.25*(AKE(1-1,3)+AKE(1-1,3+1)+AKE(1,3+1)+AKE(1,3))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  COMPUTE COEFFICIENTS OF SOURCE TERM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                            UNN=0.5*(UE(I,J+1)+UE(I-1,J+1)

VNN=0.5*(UE(I,J)+UN(I,J+1)

USS=0.5*(UE(I,J)+UE(I-1,J)

VSS=0.5*(UE(I,J)+UE(I,J+1)

UEE=0.5*(UE(I,J)+UE(I,J+1)

VEE=0.5*(UE(I,J)+UE(I,J+1)

UWW=0.5*(UE(I-1,J)+UE(I-1,J+1))

UWW=0.5*(UE(I-1,J)+UE(I-1,J+1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              FW=0.5*(UUE(I-1,J)+UUE(I-1,J+1))
B22S=XE(I,J)-XE(I-1,J)
D21S=RS*RS*(B11S*B21S+B12S*B22S)
D22S=RS*RS*(B21S*B21S+B22S*B22S)
VOLS=VOL(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          COMPUTE DIFFUSION COEFFICIENTS
                                                                                                                                                                                B12P=(YC(1,J+1)-YP(1,J)
B12P=(XP(1,J+1)-XP(1,J))
B22P=(YC(1,J)-YC(1-1,J))
B22P=XC(1,J)-XC(1-1,J)
VOLP=0.5*(VOL(1,J)+VOL(1,J+1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         FN=0.5*(VVN(I,J)+VVN(I,J+1))
FS=0.5*(VVN(I,J)+VVN(I,J-1))
FE=0.5*(UUE(I,J)+UUE(I,J+1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             COMPUTE CONVECTION MASS FLUX
                                                                                                                                                                                                                                                                                                                                                                                                                                       COMPUTE CELL SURFACE VALUES
                                                                                                                                                                                                                                                                                                                        IF(J.EQ.2) THEN
VOLP=VOL(I,2)+0.5*VOL(I,3)
                                                                                                                                                              RP=0.5*(R(I,J)+R(I-1,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       DS=VISS*D22S/VOLS
DE=VIEE*D11E/VOLE
DW=VIWW*D11W/VOLW
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      DN=VINN*D22N/VOLN
                                                                                                                    FOR CENTER POINT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 DENN-DEN(I,J+1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       AKNN-AKE(I,J+1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   (I+f'I)SIN=NNIN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             AKSS=AKE(I,J)
                                                                                                                                                                                                                                                                                                                                                                     END IF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ပပ
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                                                                                                                                                                                                                                                                                                  O
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         B21W=-(YN(I,J)-YN(I-1,J))
B22W=XN(I,J)-XN(I-1,J)
D11W=KN*(B11W*B11W*B12W*B12W)
D12W=RN*(B11W*B11W*B12W*B2ZW)
VOLM=C.25*(VOL(I-1,J)+VOL(I-1,J+1)+VOL(I,J)+VOL(I,J+1))
                                                                                                                                                                                                                                                    D11E-RE*RE*(B11E*B11E+B12E*B12E)
D12E-RE*RE*(B11E*B21E+B12E*B22E)
VOLE-0.25*(VOL(1+1,J)+VOL(1+1,J+1)+VOL(1,J)+VOL(1,J+1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   VOLM=0.25*(VOL(I-1,2)+VOL(I-1,3)+VOL(I,2)+VOL(I,3))
+0.25*(VOL(I-1,2)+VOL(I,2))
                                                                                                                                                                                                                                                                                                                                                                  VOLE-0.25*(VOL(I+1,2)+VOL(I+1,3)+VOL(I,2)+VOL(I,3))
+0.25*(VOL(I+1,2)+VOL(I,2))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         RN=0.25*(R(I-1,J)+R(I-1,J+1)+R(I,J)+R(I,J+1))
B11N=YN(I,J+1)-YN(I,J)
B12N=-(XN(I,J+1)-XN(I,J))
B21N=-(YE(I,J+1)-YE(I-1,J+1))
B22N=XE(I,J+1)-XE(I-1,J+1)
B22N=XE(I,J+1)-XE(I-1,J+1)
D21N=RW-RW+(B11N*B21N*B22N)
D22N=RN+RW+(B21N*B21N+B22N*B22N)
VOLN=VOL(I,J+1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           RS=0.25*(R(I-1,J)+R(I-1,J-1)+R(I,J)+R(I,J-1))
B11S=YN(I,J)-YN(I,J-1)
B12S=-(XN(I,J)-XN(I,J-1))
P21S=-(YE(I,J)-YE(I-1,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   FOR NORTH CONTROL VOLUME SURFACE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    FOR SOUTH CONTROL VOLUME SURFACE
                                                                                                                                                                                                                                                                                                                                                                                                                                                             POR WEST CONTROL VOLUME SURFACE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    RW-R(I-1,J)
Bliw-YE(I-1,J+1)-YE(I-1,J)
Bliw--(XE(I-1,J+1)-XE(I-1,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   BliW=YE(I-1,3)-YE(I-1,1)
Bl2W=-(XE(I-1,3)-XE(I-1,1))
      RE-R(I,J)
BllE-YE(I,J+1)-YE(I,J)
BllZE-(XE(I,J+1)-XE(I,J))
BllE-(YR(T+1,J)-YN(I,J))
BllE-(XR(I+1,J)-XN(I,J))
                                                                                                                                                              BllE=YE(I,3)-YE(I,1)
Bl2E=-(XE(I,3)-XE(I,1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               IF(J.EQ.2) THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               IF(J.EQ.2) THEN
                                                                                                                                             IF(J.EQ.2) THEN
                                                                                                                                                                                                                                                                                                                                                   IP(J.EQ.2) THEN
                                                                                                                                                                                                          END IF
                                                                                                                                                                                                                                                                                                                                                                                                            END IF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             END IF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             END IF
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SMP=FN-FS+FE-FW

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APVN(I,J)=ANN(I,J)+ASN(I,J)+AEN(I,J)+AWN(I,J)-SPVN(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      FINAL COEFF ASSEMBLY AND RESIDUAL SOURCE FOR UN
                                                                                                        化化化物 化化化物 医医克拉氏病 化化化物 化化化物 化化化物 化化化物 化化化物 化化化物 医阿拉特氏病
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        CALCULATE THE COEFFICIENTS AND SOURCE TERMS FOR
                                                                                                                                                                                                                                                                                                                                                                                      SORVOL-GREAT*VOLP
IF(-SPVN(1,J).GT.O.5*SORVOL) RESOR=RESOR/SORVOL
RESVN-RESVN+DABS(RESOR)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    RE=0.25*(R(I+1,J)+R(I+1,J-1)+R(I,J-1)+R(I,J))
B11E=YN(I+1,J)-YN(I+1,J-1)
B12E=-(XN(I+1,J)-XN(I+1,J-1))
B21E=-(XK(I+1,J)-YE(I,J))
D11E=-XE(I+1,J)-XE(I,J)
D11E=-RE+RE+(B11E+B12E+B12E)
D12E=-RE+RE+(B11E+B12E+B12E+B2E)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     RW=0.25*(R(I,J)+R(I,J-1)+R(I-1,J-1)+R(I-1,J))
B11W=YN(I,J)-YN(I,J-1)
                                                                                                                                                                                                                                       RESOR-ANN(I,J)*VN(I,J+1)+ASN(I,J)*VN(I,J-1)
+AEN(I,J)*VN(I+1,J)+AWN(I,J)*VN(I-1,J)
-APVN(I,J)*VN(I,J)+SCVN(I,J)
+CXVN(I,J)*0.25*(PR(I-1,J+1)+PR(I-1,J)
-PR(I+1,J+1)-PR(I+1,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          SCVN(1,J)=SCVN(1,J)
+(1.D0-URFV)/URFV*APVN(1,J)*VN(1,J)
         SCUN(1,3)=SCUN(1,3)
+(1.D0-URFU)/URFU*APUN(1,3)*UN(1,3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         FOR WEST CONTROL VOLUME SURFACE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        FOR EAST CONTROL VOLUME SURFACE
                                                                                                                                                                                                                                                                                                                                                         VOLP=0.5*(VOL(I,J)+VOL(I,J+1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         EAST CELL SURFACE VELOCITIES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          COMPUTE GEOMETRIC CONSTANTS
                                                                                                                                                                                                                                                                                                                                                                                                                                                            UNDER-RELAXATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         DO 280 J-2, JMAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           VOLE=VOL(I+1,J)
                                                                                                                                                                            DO 384 J=2, JWAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          CONTINUE
                                                             383 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            384
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        APUN(I,J)=ANN(I,J)+ASN(I,J)+AEN(I,J)+AWN(I,J)-SPUN(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           IF(-SPUN(I,J).GT.0.5*SORVOL) RESOR-RESOR/SORVOL
FESUN-RESUN+DABS(RESOR)
                                                                                                                                          SCUN(I,2)=SCUN(I,2)+TMULT*ANEAM*AN1*AN2*VN(I,2)
SCVN(I,2)=SCVN(I,2)+TMULT*AREAM*AN1*AN2*UN(I,2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       RESOR=ANN(I,J) *UN(I,J+1) +ASN(I,J) *UN(I,J-1)

+AEN(I,J) *UN(I+1,J) +AMN(I,J)

-AEUN(I,J) *UN(I,J)

+CXUN(I,J) *0.25*(PR(I-1,J+1) +PR(I-1,J)

+CYUN(I,J) *(PR(I-1,J+1) +PR(I+1,J))

+CYUN(I,J) *(PR(I,J) -PR(I,J+1)
                                                                                                                                                                                                                                              ALONG THE BOTTOM WALL AND SYMMETRY LINE.
                                                                                           SPUN(I,2)=SPUN(I,2)-THULT*AREAW*AN2*AN2
SPUN(I,2)=SPUN(I,2)-THULT*AREAW*AN1*AN1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            VOLP=0.5*(VOL(I,J)+VOL(I,J+1))
                                                             IF(IFLOW.Eg.1) TMULT-VISCOS/YW
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              TOP FREE STREAM BOUNDARY.
                                LAMINAR FLOW CALCULATION.
                                                                                                                                                                                                                                                                                                                                                                                                                                          IF(I.EQ.IMAX) THEN
DO 381 J=2,JHAX
AEN(IMAX,J)=0.DO
END IF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            SORVOL-GREAT * VOLP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           UNDER-RELAXATION
                                                                                                                                                                                                                                                                                                                                                                                              OUTLET CONDITION
                                                                                                                                                                                                                                                                                                                                                                                                                ************
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           DO 383 J-2, JMAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            UN(I, JP1)=1.D0
                                                                                                                                                                                                               ASN(I,2)=0.00
                                                                                                                                                                                                                                                                                                                                ASN(1,2)=0.D0
                                                                                                                                                                                                                                                                                                                                                              END IF
END IF
                                                                                                                                                                                                                                                                                                 ELSE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                               381
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DESS=0.25*(DEN(I,J)+DEN(I,J-1)+DEN(I+1,J)+DEN(I+1,J-1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                COEFFICIENTS OF PRESSURE TERM IN MOMENTUM EQUATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              DUDX-RP*(B11P*(UEE-UWW)+B21P*(UNN-USS))/VOLP
DVDX-RP*(B11P*(VEE-VWW)+B21P*(VNN-VSS))/VOLP
DKDX-RP*(B11P*(AKEE-AKWW)+B21P*(AKNN-AKSS))/VOLP
DVIDX-RP*(B11P*(VIEE-VIWW)+B21P*(VINN-VISS))/VOLP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           DUDY-RP*(B12P*(UEE-UWW)+B22P*(UNN-USS))/VOLP
DVDY-RP*(B12P*(VEE-VWW)+B22P*(VNN-VSS))/VOLP
DKDY-RP*(B12P*(AKEE-AKWW)+B22P*(AKNN-AKSS))/VOLP
DVIDY-RP*(B12P*(VIEE-VIWW)+B22P*(VINN-VISS))/VOLP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ANE (I, 3) = DMAX1 (DABS (0.5D0*FN), DN) -0.5D0*FN ASE (I, 3) = DMAX1 (DABS (0.5D0*FS), DS) +0.5D0*FS AEE (I, 3) = DMAX1 (DABS (0.5D0*FE), DE) -0.5D0*FE AWE (I, 3) = DMAX1 (DABS (0.5D0*FW), DW) +0.5D0*FW
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    COMPUTE DERIVATIVE VALUES FOR SOURCE TERMS.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                DVEDEE=0.25*(VE(1+1,3-1)-UE(1,3-1))
DVEDEE=0.25*(VE(1+1,3-1)-VE(1,3+1)
DUEDEW=0.25*(UE(1-1,3+1)-VE(1,3+1)
-UE(1-1,3-1)-UE(1,3+1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               DVEDEW=0.25*(VE(I-1,J+1)+VE(I,J+1)
-VE(I-1,J-1)-VE(I,J-1)
DUEDKN=0.25*(UE(I+1,J+1)+UE(I+1,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 -UE(I-1,J+1)-UE(I-1,J))
                                                                                                                                                                                                                                                                                                                                                                                                      COMPUTE COEFFICIENTS OF SOURCE TERM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            DUEDEE=0.25*(UE(I+1,J+1)+UE(I,J+1)
                                                                                                                                FN=0.5*(VVN(I,3)+VVN(I+1,3;)
FS=0.5*(VVN(I,3-1)+VVN(I+1,3-1))
FE=0.5*(UUE(I,3)+UUE(I+1,3))
FW=0.5*(UUE(I,3)+UUE(I-1,3))
                                                                                                                                                                                                                                                COMPUTE DIFFUSION COEFFICIENTS
                                                                                       COMPUTE CONVECTION MASS FLUX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ASSEMBLE MAIN COEFFICIENTS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     CXUE(I,J)=RP+B11P
CYUE(I,J)=RP+B21P
CXVE(I,J)=RP+B12P
CYVE(I,J)=RP+B22P
                                                                                                                                                                                                                                                                                                                                                                                                                                                                      CP=DMAX1 (0.D0, SMP)
                                                                                                                                                                                                                                                                                         DN-VINN*D22N/VOLN
                                                                                                                                                                                                                                                                                                             DS-VISS+D22S/VOLS
DE-VIEE*D11E/VOLE
                                                                                                                                                                                                                                                                                                                                                           DW-VIWW*D11W/VOLW
                                                                                                                                                                                                                                                                                                                                                                                                                                                  SMP-FN-FS+FE-FW
                   DEEE-DEN(I+1,J)
                                             DEWW-DEN(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           CPO=CP
                                                                                                                                                                                                                                                                                                                                                                                   000
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             VINN=0.25D0*(VIS(I,J)+VIS(I,J+1)+VIS(I+1,J)+VIS(I+1,J+1))
VISS=0.25D0*(VIS(I,J)+VIS(I,J-1)+VIS(I+1,J)+VIS(I+1,J-1))
VIEE=VIS(I+1,J)
                                                                                                                                                                                           RN=R(I,J)
B11N=YE(I,J+1)-YE(I,J)
B12N=-(XE(I,J+1)-XE(I,J))
B21N=-(YE(I,J+1,J)-XH(I,J))
B22N=XH(I+1,J)-XH(I,J)
D21N=RN*RN*(B11N*B21N+B12N*B22N)
D22N=RN*RN*(B21N-B21N+B22N+B22N)
VOLN=0.25*(VOL(I,J)+VOL(I,J+1)+VOL(I+1,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      VOLS=0.25*(VOL(I,J-1)+VOL(I,J)+VOL(I+1,J)+VOL(I+1,J-1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  AKNN-0.25*(AKE(I,J)+AKE(I,J+1)+AKE(I+1,J+1)+AKE(I+1,J))
AKSS-0.25*(AKE(I,J-1)+AKE(I,J)+AKE(I+1,J)+AKE(I+1,J-1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               DENN=0.25*(DEN(I,J)+DRN(I,J+1)+DEN(I+1,J)+DEN(I+1,J+1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 VNN=0.5*(VN(I,J)+VN(I+1,J)

USS=0.5*(UE(I,J)+UE(I,J-1))

VSS=0.5*(UE(I,J)+UE(I+1,J-1))

UEE=0.5*(UE(I,J)+UE(I+1,J))

UNN=0.5*(UE(I,J)+UE(I+1,J-1))

UNN=0.5*(UE(I,J)+UE(I-1,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     B228-XN(I+1,J-1)-XN(I,J-1)
D21S-RS*RS*(B11S*B21S+B12S*B22S)
D22S-RS*RS*(B21S*B21S+B22S*B22S)
                   B21N=-(VE(I,J)-YE(I-1,J))
B22N=XE(I,J)-XE(I-1,J)
D11N=RN*RN*(B11N*B11N*B12N*B12H)
D12N=RN*RN*(B11N*B12N*B12H)
                                                                                                                                                      NORTH CONTROL VOLUME SURFACE
                                                                                                                                                                                                                                                                                                                                                                                                    FOR SOUTH CONTROL VOLUME SURFACE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               B11P=YC(I,J)-YC(I,J-1)

B12P=-(XC(I,J)-XC(I,J-1))

B21P=-(YP(I+1,J)-YP(I,J))

B22P=XF(I+1,J)-YP(I,J)

VOLP=0.5*(VOL(I,J)+VOL(I+1,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                   B11S=YE(I,J)-YE(I,J-1)
B12S=-(XE(I,J)-XE(I,J-1))
B21S=-(YN(I+1,J-1)-YN(I,J-1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  COMPUTE CELL SURPACE VALUES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  UNN=0.5*(UE(I,J)+UE(I,J+1))
  012W=-(XN(I,J)-XN(I,J-I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              RP=0.5+(R(I,J)+R(I,J-1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CENTER POINT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                AKEE-AKE(I+1,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     VIWN-VIS(I, J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        AKWW-AKE(I,J)
                                                                                                          VOLM-VOL(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                              RS=R(I,J-1)
                                                                                                                                                      FOR
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DIN=(XE(I,2)-XE(I,1))**2+(YE(I,2)-YE(I,1))**2
DIW=(XP(I+1,1)-XP(I,1))**2+(YP(I+1,1)-YP(I,1))**2
DISN=DSQRT(DIN)
                                                                                                                                                                                                                                                                                                                                                                   TMULT=DENUE*CDTERM*SQRTK*CAPPA/DLOG(ELOG*YPLUSA)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          S..E(I,2)=SPUE(I,2)-TMULT*AREAWAN2*AN2
SPUE(I,2)=SPUE(I,2)+TMULT*AREAWAN1*AN2
SCUE(I,2)=SCUE(I,2)+TMULT*AREAWAN1*AN2*VE(I,2)
SCUE(I,2)=SCUE(I,2)+TMULT*AREAWAN1*AN2*VE(I,2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ALONG THE BOTTOM WALL AND SYMMETRY LINE.
                                                                                                                                                                                                                                          SQRTK-DSQRT(0.5*(AKE(1,2)+AKE(1+1,2)))
DENUE-0.5D0*(DEN(1,2)+DEN(1+1,2))
YPLUSA-CDTERM*SQRTK*YW/VISCOS
                                                                                                                                                                                                                                                                                                                                                                                                                                                          IF(IFLOW.EQ.1) TMULT=VISCOS/YW
                                                                                                                                    AN1=-(YP(I+1,1)-YP(I,1))/DISW
AN2=(XP(I+1,1)-XP(I,1))/DISW
                                IF(I.GE.M1.AND.I.LT.M2) THEN
                                                                                                                                                                                                                                                                                                               IF(YPLUSA.LE.11.63D0) THEN TMULT=VISCOS/YW
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   TOP FREE STREAM BOUNDARY.
                                                                                                                                                                                                                                                                                                                                                                                                                        LAMINAR FLOW CALCULATION.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              IF(I.EQ.IMAX) THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             DO 281 J=2,JMAX
AEE(IMAX,J)=0.DO
END IF
                                                                                                                                                                                            AREAW=DISW*R(I,1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            DUTLET CONDITION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ***********
                                                                                                                      DISW-DSQRT (DIW)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         UE(I,JP1)=1.D0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ASE(1,2)=0.D0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ASE(I,2)=0.D0
                                                                                                                                                                                                                              WW=DISN*AN2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          END IF
                                                                                                                                                                                                                                                                                                                                                                                       END IF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ELSE
                                                                                                                                                                                                                                                                                                                                                     ELSE
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               IF(ICORD.EQ.2) THEN
SPVE(I,J)=SPVE(I,J)
-0.5*(VIS(I,J)+VIS(I+1,J))*VOLP/RP/RP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ALONG THE BOTTOM WALL- BY WALL FUNCTION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 SORCUE-DVIDX * DUDX + DVIDY * DVDX-2./3.*DKDX
SORCVE-DVIDX * DUDY + DVIDY * DVDY-2./3.*DKDY
   DVEDKN=0.25*(VE(I+1,J+1)+VE(I+1,J)

VE(I-1,J+1)+VE(I+1,J)

DVEDKS=0.25*(VE(I+1,J+1)+VE(I+1,J)

-UE(I-1,J+1)-UE(I-1,J+1)

DVEDKS=0.25*(VE(I+1,J-1)+VE(I+1,J)

-VE(I-1,J-1)+VE(I+1,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  SCUE(I,J) =CPO*UE(I,J) +SORCUE*VOLP+S 3UE
SCVE(I,J) =CPO*VE(I,J) +SORCVE*VOLP+SBVE
                                                                                                                             SOURCE FUNCTION BY NON-ORTHOGONALITY.
                                                                                                                                                                                                                                                                                                                                                                                                                             SBUE-SBUEE-SBUEW+SBUEN-SBUES
SBVE-SBVEW+SBVEN-SBVES
                                                                                                                                                                             SBVEE-VIEE *D12E/VOLE*DVEOEE
SBUEW-VIWW*D12W/VOLW*DVEDEW
SBVEW-VIWW*D12W/VOLW*DVEDEW
SBUEN-VIWW*D2IN/VOLW*BVEDEW
SBVEN-VINN*D2IN/VOLW*BVEDKW
                                                                                                                                                                                                                                                                                                                                                          SBUES=VISS*D21S/VOLS*DUEDKS
SBVES=VISS*D21S/VOLS*DVEDKS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       IF(IFLOW.EQ.1) THEN
SCUE(I,J)=CPO*UE(I,J)+SBUE
SCVE(I,J)=CPO*VE(I,J)+SBVE
END IF
                                                                                                                                                                 SBUEE-VIEE+D12E/VOLE+DUEDEE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    COMPUTE SOURCE FUNCTIONS
                                                                                                                                                                                                                                                                                     IF(J.EQ.2) THEN
SBUES=0.DO
SBVES=0.DO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               CDTERM=CMU*0.25
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               SPUE(I,J)=-CP
SPVE(I,J)=-CP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    END IF
                                                                                                                                                                                                                                                                                                                                                                                                END IF
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DO 386 J-ANI(I,J)
AA(J)=ASN(I,J)
AA(J)=ASN(I,J)
CC(J)=-ANN(I,J)
5 DD(J)=AEN(I,J) *UN(I+1,J) *AWN(I,J) *VN(I-1,J) *VON(I,J)
1 +CXUN(I,J) *0.25*(PR(I-1,J+1) +PR(I-1,J)
PR(I+1,J+1) *VON(I,J) *VON(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          DD(J)=AEN(I,J)*VN(I+1,J)+AWN(I,J)*VN(I-1,J)+SCVN(I,J)
+CXVN(I,J)*0.25*(PR(I-1,J+1)+PR(I-1,J)
-PR(I+1,J+1)-PR(I+1,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 SOLUTION OF DIFFERENCE EQUATIONS FOR VN.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             VN(I,JP1)=VN(I,JMAX)*(R(I,JMAX)+R(I-1,JMAX+1))
/(R(I,JMAX+1)+R(I-1,JMAX+1))
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C CALCULATE THE PRESSURE-CORRECTION FIELD C 1TPP=15 C DO 482 J=1,JP1 PP(1-1,J)=0. 482 PP(1+1,J)=0. C NO 483 ITER=1,ITPP CALL PRESU(PP,SPP,I,0) 483 CONTINUE C	C CORRECT THE VELOCITY FIELD. C CORRECT THE VELOCITY FIELD. C CORRECT THE VELOCITY FIELD. C CORRECT CONTRAVARIANT VELOCITIES. C CORRECT CONTRAVARIANT VELOCITIES. C DO 170 J=2,JMAX 170 VVN(I,J)=VVN(I,J)+BCV(I,J)*(PP(I,J)-PP(I,J+1)) VVN(I,JP1)=VVN(I,J)+BCV(I,J)*(PP(I,J)-PP(I+1,J+1)) C DO 171 J=2,JMAX 171 UUE(I,J)=UUE(I,J)+BCU(I,J)*(PP(I,J)-PP(I+1,J+1)) UUE(I,J)=UUE(I,J)=UUE(I,J)+BCN(I+1,JP1)) 1 *0.5D0*(BN(I,J+JP1))	UUE(I,1)=0.00  C CALCULATE THE OTHER CONTRAVARIANT VELOCITIES C BY INTEPOLATION. C DO 172 J=2,JMAX VVE(I,J)=0.25*(VVM(I,J)+VVM(I+1,J)+VVM(I+1,J-1)) 172 UUN(I,J)=0.25*(VUE(I,J)+UUE(I-1,J)+UUE(I-1,J+1) C C CALCULATE CORRECTED CARTESIAN VELOCITY COMPONENTS C USING THE CORRECTED CONTRAVELOCITES.	C FOR NORTH CONTROL VOLUME SURFACE C VELOCITY COMPONENTS, UN AND VN. C DO 174 J=2,JHAX DENN=0.5*(DEN[I,J]+DEN[I,J+1]) RN=0.5*(DEN[I,J)+R[I-J,J) B11N=-YP[I,J+1]-YP[I,J) B12N=-(XP[I,J+1]-YP[I,J) B12N=-(XP[I,J+1]-YP[I,J) B21N=-(XP[I,J)-XP[I,J)) B22N=-(XP[I,J)-XP[I,J)) B22N=-(XP[I,J)-XP[I,J)) B22N=-(YP[I,J)-XP[I,J)) B22N=-XP[I,J)-XP[I,J) D1VN=DENN*RN*(B11N*B22N-B12N*B21N) UN(I,J)=-(B21N*UUN(I,J)-B11N*VVN(I,J))/DIVN C C
FS=DESS=RS=(B21S=UN(I,J-1)+B22S=VN(I,J-1)) FE=DEEE=RE=(B11E=UE(I,J)+B12E=VE(I,J)) FW=DEWN=RN=(B11N=UE(I-1,J)+B12WaVE(I-1,J)) C SMP=FN-FS+FE-FW C SMP=FN-FS+FE-FW C COMPUTE CONTRAVARIANT VELOCITY COMPONENTS C UUE(I,J)=FR VVN(I,J)=FR C COMPUTE SUM OF ABSOLUTE MASS SOURCE	C COMPUTE COEFFICIENTS OF PRESSURE C COMPUTE COEFFICIENTS OF PRESSURE C AND PRESSURE CORRECTION. C QXUE(I,J)=URFV*RE*BllE/APUE(I,J) QXVE(I,J)=URFV*RE*BllE/APUE(I,J) QXVI(I,J)=URFV*RH*BllN/APUN(I,J) QYUN(I,J)=URFV*RH*BllN/APUN(I,J) C BCU(I,J)=DERE*RE*(BllE*QXUE(I,J)+BllE*QXVE(I,J)) C BCU(I,J)=DERH*RH*(BllN*QYUN(I,J)+BllN*QYUN(I,J)) C C C CONTINUE	CONSIDER THE BOUNDARY CONDITIONS FOR  CONSIDER THE BOUNDARY CONDITIONS FOR  C THE PRESSURE CORRECTION EQUATION.  ***********************************	C VVN(I,JP1) = VVN(I,JMAX) UUE(I,JP1) = 0.5D0*(BEN(I,JP1) + DEN(I+1,JP1))  1

UN(I,JP1)=1.Do	C DO 489 J=1,JP1
<pre>IF(I.LE.M1.OR.I.GE.M2) THEN UN(I,1)=(YN3SQ*UN(I,2)-YN2SQ*UN(I,3))</pre>	C UE(IP1,J)=UE(IMAX,J) VE(IP1,J)=VE(IMAX,J) UUE(IP1,J)=UUE(IMAX,J) VVE(IP1,J)=VVE(IMAX,J)
VN(I,JP1)=VVN(I,JP1)/(0.5*(R(I,JP1)+R(I-1,JP1))) /(XC(I,JP1)=XC(I-1,JP1)) /(DEN(I,JP1)	UUN(IP1,J)=UUN(IMAX,J) VVN(IP1,J)=VVN(IMAX,J) UN(IP1,J)=UN(IMAX,J) 489 VN(IP1,J)=VN(IMAX,J)
VM(1,1)=U. FOR EAST CONTROL VOLUME SURFACE VELOCITY COMPONENTS, UE AND VE.	C UE(IP1,1)=UE(IP1,2) UN(IP1,1)=UN(IP1,2) C END IF
DO 173 J=2,JMAX DENE=0.5*(DEN(I,J)+DEN(I+1,J)) RE=0.5*(R[I,J)+R[I,J=1)) Blie=vC(I,J)-vC(I,J-l) Blie=vC(I,J)-xC(I,J-l)	C hattertentatestentatestentatestentatestentatestentatestentates C RETURN POINT OF INNER ITERATION. C STATESTESTENTATESTENTATESTENTATESTENTATESTENTATESTENTATESTENTATESTENTATESTENTATESTENTATESTENTATESTENTATESTENTATESTEN
B21E=-(YP(I+1,J)-YP(I,J)) B22E=XP(I+1,J)-YP(I,J)) D1VE-DENE«RE«(B11E»B22E-B12E*B21E) D1VE(I,J)=(B22E*UUE(I,J)-B12E*VVE(I,J))/DIVE VE(I,J)=-(B21E*UUE(I,J)-B11E*VVE(I,J))/DIVE	C terrestrates to the PSEUDO-VELOCITY AND THE CALCULATE THE PSEUDO-VELOCITY AND THE ASSOCIATED MASS SOURCE C ASSOCIATED WASS SOURCE C ASSOCIATED WASS COURCE C ASSOCIATED TO THE TERRESTRATE TO THE TERREST
UE(I,JP1)=1.DO IF(I.LT.M1.OR.I.GE.M2) THEN	C CALCULATE PSEUDO-VELOCITIES. C DO 490 J=2,JMAX
UE(I,1)=(YE3SQ*UE(I,2)-YE2SQ*UE(I,3)) /(YE3SQ-YE2SQ) UE(I,1)=0.	C IF(J.EQ.2) THEN PRUVHE=0.5*(PR[I,1)+PR(I+1,1)) 1
VE(I,JP1)=0.25*(VN(I,JP1)+VN(I,JMAX)+VN(I+1,JP1)+VN(I+1,JMAX)) VE(I,1)=0.	PRUVHE=0.25*(PR(I,J-1)+PR(I+1,J-1) 1 -PR(I,J+1)-PA(I+1,J+1)
ARTER CONDITION PROPERTY OF THE STATE OF THE	UHE(I,J)=(ANE(I,J)*VE(I,J+1)+ASE(I,J)*VE(I,J-1) 1 +AEE(I,J)*VE(I+1,J)+AME(I,J)*VE(I-1,J) 2 +SCVE(I,J)/(APVE(I,J)/URFV) 3 +CYVE(I,J)/(APVE(I,J)/URFV)*PRUVHE
IF(I.EQ.IMAX) THEN ARDENT=0.DO	490 UHE(I,J)= 1 2 2
FIGN=0.DO FIGN=0.DO FCV=0.5*(R[IMAX,J)+R(IMAX,J-1)) ARDEN=DEN(IMAX,J)*RCV*(YC(IMAX,J)-YC(IMAX,J-1)) ARDENT=ARDEN+RDENT FLOW-FLOW+ARDEN*UE(IMAX,J)	C DO 491 J=2,JHAX  DO 491 J=2,JHAX  DO 491 J=2,JHAX  UHN(I,J)=(ANN(I,J)=UN(I,J+1)+ASN(I,J)=UN(I,J-1)  I +AEN(I,J)=(NN(I,J)+ANN(I,J)+UN(I-1,J)  2 +SEN(I,J)>(APUN(I,J)/UNFU)  3 +CXUN(I,J)/(APUN(I,J)/UNFU)  4 +0.25=(PR(I-1,J+1)+PR(I-1,J)  5 +PR(I+1,J+1)+PR(I-1,J)
UINC=(FLOMIN-FLOM)/ARDENT	C 491 VHV(I,J)=(ANN(I,J)*VN(I,J)+ASN(I,J)*VN(I,J-1)

SMP=FN-FS+FE-FW	SPR(I,J)=SMP	C 493 CONTINUE		IF(IFLOW.EQ.1) GO TO 688	CALCULATE THE COEFFICIENTS AND SOURCE FUNCTIONS		C 6555555555555555555555555555555555555	C DO 580 J≈2,JMAX	C COMPUTE GEOMETRIC CONSTANTS	C FOR EAST CONTROL VOLUME SURFACE		B11E=YC(I,J)-YC(I,J-1) B12E=-(XC(I,J)-XC(I,J-1)) B21E=-(XC(I+1,J)-YP(I,J) B22E=XP(I+1,J)-XP(I,J)	D11E=RE*RE*(#11E=#11E+#12E*#12E) D12E=RE*RE*(#11E*#21E+#12E*#22E)	VOLE=0.5*(VOL(1,J)+VOL(1+1,J))  C FOR WEST CONTROL VOLUME SURFACE		B12W=-(XC(I-1,J)-XC(I-1,J-1)) B21W=-(YC(I,J)-YE(I-1,J)) B22W=XP(I,J)-XP(I-1,J) D11W=WRW*(B11W*B12W*B12W)		C FOR NORTH CONTROL VOLUME SURFACE C	RN=0.5 + (R(1, J) + R(1-1, J)) $B11N = YP(1, J) + YP(1, J)$ $B12N = (XP(1, J+1) - XP(1, J))$	B21N=-(YC(I,J)-YC(I-1,J)) B22N=XC(I,J)-XC(I-1,J) D21N=RN*RN*(B11N*B21N+B12N*B22N) D22N=RN*RN*(B21N*B21N+B12N*B22N)	C FOR SOUTH CONTROL VOLUME SURFACE	
1 +AEN(I,J)*VN(I+1,J)*AMN(I,J)*VN(I-1,J) 2 +SCVN(I,J))/(APVN(I,J)/URFV)		5	VHN (I, 1) -VN (I, 1)		IF(I.EQ.2) THEN DO 492 J=2,JHAX	OHE(1,J)=UE(1,J) 492 VHE(1,J)=VE(1,J)		CALCULATE MASS-SOURCE OF PRESSURE EQUATION.	DO 493 J=2, JMAX	COMPUTE GEOMETRIC CONSTANTS	FOR EAST CONTROL VOLUME SURFACE	RE=0.5*(R(I,J)+R(I,J-1)) B11E=YC(I,J)-YC(I,J-1) B12E=-(XC(I,J)-XC(I,J-1))	FOR WEST CONTROL VOLUME SURFACE	RW=0.5*(R(I-1,J)+R(I-1,J-1)) B11W=YC(I-1,J)-YC(I-1,J-1) B12W=-(XC(I-1,J)-XC(I-1,J-1))	FOR NORTH CONTROL VOLUME SURFACE	RN=0.5*(R(I-1,J)+R(I,J)) B21N=-(YC(I,J)-YC(I-1,J)) B22N=XC(I,J)-XC(I-1,J)	FOR SOUTH CONTROL VOLUME SURFACE	RS=0.5 + (R(I-1,J-1) + R(I,J-1)) RJS=-(V(I,J-1) + V(V(I-1,J-1))	COMPUTE FACE DENSITIES.	DENN=0.5D0*(DEN(I,J)+DEN(I,J+1)) DESS=0.5D0*(DEN(I,J)+DEN(I,J-1)) DERE=0.5D0*(DEN(I,J)+DEN(I+1,J)) DEWW=0.5D0*(DEN(I,J)+DEN(I-1,J))	COMPUTE CONVECTION MASS FLUX.	FN=DENN*RN*(B21N*UHN(I,J)+B22N*VHN(I,J)) FS=DESS*RS*(B21S*UHN(I,J-1)+B22S*VHN(I,J-1)) FE=DEEE*RE*(B11E*UHE(I,J)+B12E*VHE(I,J))

	C COMPUTE DIFFUSION COEFFICIENTS  DN=VINND=D22N/VOLN  DS=VISSD=D22S/VOLS  DB=VIEED*D11E/VOLE  DM=VIWMD=D11M/VOLM  C AND(I,J)=DMAX1(DABS(0.5D0*FN), DN)-0.5D0*FN  ASD(I,J)=DMAX1(DABS(0.5D0*FE), DS)-0.5D0*FN  ASD(I,J)=DMAX1(DABS(0.5D0*FE), DS)-0.5D0*FN  AND(I,J)=DMAX1(DABS(0.5D0*FW), DW)+0.5D0*FW	C COMPUTE DERIVATIVE VALUES FOR SOURCE TERMS. C DUDX=RP+(B11P+(UEE-UWW)+B21P+(UNN-USS))/VOLP DVDX=RP+(B11P+(VEE-UWW)+B21P+(VNN-USS))/VOLP DVDY=RP+(B12P+(UEE-UWW)+B22P+(VNN-USS))/VOLP C DAKEDEE=0.25*(AKE(I+1,J+1)+AKE(I,J+1)	DADSDEE=0.25*(ADS(I+1,J-1)-AKE(I,J-1))  DADSDEE=0.25*(ADS(I+1,J-1)-ADS(I,J-1))  DAREDEW=0.25*(ARE(I-1,J-1)-ADS(I,J-1))  DADSDEW=0.25*(ARE(I-1,J-1)-ARE(I,J-1))  DADSDEW=0.25*(ARE(I-1,J-1)-ARE(I,J-1))  DAREDKN=0.25*(ARE(I+1,J+1)+ARE(I+1,J))  DADSDRN=0.25*(ARE(I+1,J+1)-ARE(I-1,J))  DADSDRS=0.25*(ARE(I+1,J+1)-ADS(I-1,J))  DADSDRS=0.25*(ARE(I+1,J-1)+ARE(I+1,J))  DADSDRS=0.25*(ADS(I+1,J-1)+ARE(I-1,J))  DADSDRS=0.25*(ADS(I+1,J-1)+ARE(I-1,J))  DADSDRS=0.25*(ADS(I+1,J-1)+ARE(I-1,J))	C SOURCE FUNCTION BY NON-ORTHOGONALITY. C SBAKEE-VIEE*D12E/VOLE*DAKEDEE SBADSE-VIED*D12E/VOLE*DAKEDEE SBADSE-VIED*D12E/VOLE*DAKEDEW SBADSE-VIEW*D12E/VOLM*DASDEW SBANSH-VIWM*D12E/VOLM*DASDEW SBAKEN-VIWM*D12N/VOLM*DASDEW SBAKEN-VINN*D21N/VOLM*DASDEW SBAKEN-VINND*D21N/VOLM*DASDEW SBAKEN-VINND*D21N/VOLM*DASDEW SBAKES-O.DO SBAKES-O.DO
D21S=RS*RS*(B11S*B21S+B12S*B22S) D22S=RS*RS*RS*(B11S*B21S+B22S*B22S) D22S=RS*RS*RS*(B21S*B21S+B22S*B22S) VOLS=0.5*(VOL(I,J-1)+VOL(I,J)) C FOR CENTER POINT C RP=0.25*(R(I,J)+R(I-1,J)+R(I-1,J-1)+R(I,J-1)) B11P=VN(I,J)-YN(I,J-1) B12P=-(YR(I,J)-XN(I,J-1)) B21P=-(YR(I,J)-XR(I-1,J)) B22P=-XR(I,J)-XR(I-1,J) C C C C C RP=0.25*(R(I,J)-XR(I-1,J))	COMPUTE CELL SURFACE VALUES C UNN-0.25*(UE(I-1,J)+UE(I-1,J+1)+UE(I,J)+UE(I,J+1)) VNN-VN(I,J) USS-0.25*(UE(I-1,J-1)+UE(I-1,J)+UE(I,J-1)+UE(I,J)) VSS-VN(I,J-1) UEE-UE(I,J-1) UEE-UE(I,J-1) VEE-UE(I,J-1) VMM-UE(I-1,J)+VN(I,J-1)+VN(I+1,J-1)) VMM-0.25*(VN(I-1,J)+VN(I-1,J-1)+VN(I,J-1))	IF(J.EQ.2) THEN USS=0.5*(UE(I-1,1)+UE(I,1))  END IF  VINN=0.5*(VIS(I,J)+VIS(I,J+1))/PRTE VISS=0.5*(VIS(I,J)+VIS(I,J-1))/PRTE VIES=0.5*(VIS(I,J)+VIS(I+1,J))/PRTE VINN=0.5*(VIS(I,J)+VIS(I+1,J))/PRTE	DENN=0.5*(DEN(I,J)+DEN(I,J+1)) DESS=0.5*(DEN(I,J)+DEN(I,J-1)) DERE=0.5*(DEN(I,J)+DEN(I+1,J)) DEWH=0.5*(DEN(I,J)+DEN(I-1,J)) C COMPUTE CONVECTION MASS FLUX. C FN=VVN(I,J) FS=VVN(I,J-1) FW=UUE(I,J) C COMPUTE DIFFUSION COEFFICIENTS	C DN=VINN*D22N/VOLN DS=VISS*D22S/VOLS DE=VISE*D11E/VOLE DM=VINN*D11M/VOLM C COMPUTE COEFFICIENTS OF SOURCE TERM C SMP=FN-FS+FE-FW C CPC-CP C ASSEMBLE MAIN COEFFICIENTS

RP=0.25*(R(I,2)+R(I-1,2)+R(I-1,1)+R(I,1)) B11P=YN(I,2)-YN(I,1) B12P=-(XN(I,2)-XN(I,1)) B21P=-(XP(I,2)-YE(I,1)) B22P=-(XE(I,2)-YE(I-1,2)) B22P=XE(I,2)-XE(I-1,2)	DIN=(XP(I,2)-XP(I,1))**2+(YP(I,2)-YP(I,1))**2 DIW=(XC(I,1)-XC(I-1,1))**2+(YC(I,1)-YC(I-1,1))**2 DISN=DSQRT(DIN) DISW=DSQRT(DIW) ANI=-(YC(I,1)-YC(I-1,1))/DISW ANZ=(XC(I,1)-YC(I-1,1))/DISW	AREAW=DISW+0.5+(R(I,1)+R(I-1,1))  YW=DISN+AN2  UP=0.5+(UE(I,2)+UE(I-1,2))  VP=0.5+(VN(I,2)+VN(I,1))  UAVG=AN2+UP-AN1+VP  DENU=DEN(I,2)  SQRTK=DSQRT(AKE(I,2))  YPLUSN(I)=DENU+SQRTK+COTERN+YW/VISCOS	IF(YPLUSN(I).LE.11.63D0) THFN TMULT=VISCOS/YW TAUN(I)=TMULT=VISCOS/YW DITERM=DEN(I,2)*(CMU**0.75D))*SQRTK*YPLUSN(I)/YW ELSE TMULT=DENU*CDTERM*SQRTK*CAPPA/DLOG(ELOG*YPLUSN(I)) TAUN(I)=TMULT=UANG DITERM=DEN(I,2)*(CMUL*0.75D0)*SQRTK  1 = *DLOG(ELOG*YPLUSN(I))/(CAPPA*VW) END IF	UNN=0.25*(UE(I-1,2)+UE(I-1,3)+UE(I,2)+UE(I,3)) USS=0.5*(UE(I-1,1)+UE(I,1)) UE=UE(I,2) UNN=UE(I-1,2) VNN=VN(I,2) VSS=VN(I,1) VE=0.25*(VN(I,2)+VN(I+1,2)+VN(I,1)+VN(I+1,1)) VMM=0.25*(VN(I,2)+VN(I-1,2)+VN(I,1)+VN(I-1,1))	DUDX=RP*(B11P*(UEE-UWM)+B21P*(UNN-USS))/VOLP DVDX=RP*(B11P*(VEE-VWW)+B21P*(VNN-VSS))/VOLP DUDY=RP*(B12P*(UEE-UWW)+B22P*(UNN-USS))/VOLP DVDY=RP*(B12P*(VEE-VWW)+B22P*(VNN-VSS))/VOLP	GENCOU-TAUN(I)**2/(DENU*CDTERM*SQRTK*CAPPA*YW) GENRES-VIS(I,2)*(2.DO*(DUDX*DUDX+DVDY*DVDY)) GEN(I,2)=GENCOU +GENRES	IF(ICORD.EQ.2) THEN GEN(I,2)=GEN(I,2)+VIS(I,2)*0.5*(VN(I,2)+VN(I,1))**2/RP/RP END IF
ELSE SBAKES-VISS*D21S/VOLS*DAKEDKS SBADSS-VISSD*D21S/VOLS*DADSDKS END 1F C SBAKE-SBAKEW+SBAKEW-SBAKES SBADSS-SBADSE-SBAKEW+SBAKEW-SBAKES		GEN(I,3)=VIS(I,J)*(2.D0*(DUDX*DUDX+DVDY*DVDY)  1	О <u>г</u> р 'AKE(1,J) «VOLР	SCD(I,J)=CPO+ADS(I,J)+SBADS SUDO(I,J)=SCD(I,J) SCD(I,J)=SCD(I,J) 1 +DEN(I,J)=CP SPD(I,J)=-CP SPD(I,J)=-CP SPD(I,J)=SPD(I,J) SPD(I,J)=SPD(I,J) SPD(I,J)=SPD(I,J)	580 CONTINUE  ***********************************	(WALL FUNCTION AND SYMMETRY CONDITIONS)  ***********************************	C ALONG THE BOTTOM WALL - WALL FUNCTION C ************************************

ပ		582 AED(IMAX,J)=0.DO END IF	U O	C stituble coeff ASSEMBLY AND RESIDUAL SOURCE FOR AKE C stituble coeff ASSEMBLY AND RESIDUAL SOURCE FOR AKE	С DO 583 J=2,JMAX	APK(1,J)=ANK(1,J)+ASK(1,J)+AEK(1,J)+AWK(1,J)-SPK(1,J) RESOR=ANK(1,J)*AKE(1,J+1)+ASK(1,J)*AKE(1,J-1) 1 +AEK(1,J)*AKE(1+1,J)+AWK(1,J)*AKE(1-1,J) 2 -APK(1,J)*AKE(1,J)+SCK(1,J)	C VOLP-VOL(1,3)	SORVOL-GREAT*VOLP IF(-SPK(I,J).GT.0.5*SORVOL) RESOR-RESOR/SORVOL RESAK-RESAK+DABS(RESOR)	C UNDER-RELAXATION	APK(I,J)=APK(I,J)/URFK SCK(I,J)=SCK(I,J)+(1.D0-URFK)*APK(I,J)*AKE(I,J)	583	C SOLUTION OF DIFFERENCE EQUATIONS FOR AKE C shipped and the transmission of DIFFERENCE CONTINUE FOR AKE C shipped and the transmission of the tra		BB(J)=APK(I,J) CC(J)=-ANK(I,J)	505 DD(J)=AEK(I,J)*AKE(I+1,J)+AWK(I,J)*AKE(I-1,J) 1 +SCK(I,J) C	DD(2)=DD(2)=AA(2)*AKE(1,1) DD(JMAX)=DD(JMAX)-CC(JMAX)*AKE(1,JMAX+1)	CALL TRIDAG(2, JMAX, AA, BB, CC, DD, T)	DO 586 J=2,JMAX S86 AKE(I,J)=T(J)	C AKE(I,JMAX+1)=AKE(I,JMAX) C	IF(I.LE.M1.0 AKE(I,1)=(YP	1 /(YP3SQ-YP2SQ) ELSE AKE(I,1)=0.
CA NIMEILL EMENDI ECONITOR	SCK(I,2)=GEN(I,2)*VOLP+SUKD(I,2) SPK(I,2)=-DITERM*VOLP+SPKD(I,2)	ASK(I,2)=0.D0	FOR DISSIPATION RATE EQUATION.	TERM=(CMU**0.75D0)/(CAPPA*YW) SCD(I,2)=GREAT*TERM*AKE(I,2)**1.5 SPD(I,2)=-GREAT	ALONG THE SYMMETRY AXIS	ELSE RP=0.25*(R(I,2)+R(I-1,2)+R(I-1,1)+R(I,1)) R)) D=VW/T 0) VW/T 1	B12P=-(XKI,Z)-xXI, B12P=-(YKI,Z)-YK(I,Z) B21P=-(YKI,Z)-YK(I,Z)	_	USS=0.5*(UE(I-1,1)+UE(I,1)) UEE=UE(1,2)	UWW-UE(I-1,2) VNN-VN(I,2)	VSS=VN(I,1) VEE-0.25*(VN(I,2)+VN(I+1,2)+VN(I,1)+VN(I+1,1) VMM+0.25*(VN(I,2)+VN(I=1,3)+VN(I,1)+VN(I=1,1)	DUDX=RP*(B11P*(UEE-UWW)+B21P*(UNN-USS))/VOLP DVDX=RP*(B11P*(VEE-VWW)+B21P*(VNN-VSS))/VOLP	DUDY=RP*(B12P*(UEE-UWW)+B22P*(UNN-USS))/VOLP DVDY=RP*(B12P*(VEE-VWW)+B22P*(VNN-VSS))/VOLP '	GEN(I,2)=VIS(I,2)*(2.D0*(DUDX*DUD::+DVDY*DVDY)+(DVDX+DUDY)**2)	IF(ICORD.EQ.2) THEN GEN(I,2)=GEN(I,2)+VIS(I,2)+0.5*(VN(I,2)+VN(I,1))**2/RP/RP	AND IN	SCK(I,2)=SUKD(I,2)+GEN(I,2)*VOLP SCD(I,2)=SUDD(I,2)	1 +DEN(I,2) *C1*GEN(I,2) *ADS(I,2) *VOLP/AKE(I,2)	ASK(I,2)=0.D0 ASD(I,2)=0.D0	END IF	ALONG THE OUTLET.

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FOR KINETIC ENERGY EQUATION

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IF(I.EQ.IMAX) THEN υO

END IF

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OUTPUT AFTER CALCULATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        WRITE(8,12)NITER,1,XP(1,1),URFU
12 FORMAT(//5X,'NO. OF ITERATION "',13,5X,'STATION',13
1,5X,'X =',F8.4,5X,'U-RF =',F6.3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    OUTPUT FOR EACH ITERATION
                                                                                               5555
5555
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                                                                                                                                                     WRITE(8,4111) NITER
FORMAT(/5x,'NO. OF ITERATION =',15,
15x,'WALL OR CENTERLINE PRESSURE')
WRITE(8,2009)(PR(1,1),1=2,1MAX)
                                                                                                                                                                                                                      FORMAT(/5X,'FRICTION VELOCITY')
WRITE(8,2009)(UTAU(I),I=MIP1,H2M1)
                                                                                                                                                                                                                                                       WRITE(8,4113)
FORMAT(/5X,'CENTERLINE VELOCITY')
WRITE(8,2009)(UE(1,1),1-M2,IMAX)
                                                                                                                                                                                                                                                                                                                                                                             ខ្ពុខ្ព
                                                    ITPRINT MAXIT - ITOUT
IF (NITER. LE. ITPRINT) GO TO 6666
                                                                                                                                                                                                                                                                                                                                                                              888
                                                                                                                                                                                                                                                                                                                                                                                                                                               IF (NITER.GE.MAXIT) GO TO 702
                                                                                                                                                                                                                                                                                                                                                       DO 4999 I=1,IP1
DO 4999 J=1,JP1
IF(DABS(PE(I,J)).GT.10.DD)
IF(DABS(UE(I,J)).GT.10.DD)
IF(DABS(UN(I,J)).GT.10.DD)
                                                                                                                                                                                                                                                                                                                                   CHECK FOR OVERFLOW.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      IN 3333 I=1, IP1
                                                                                                                                                                                                             WRITE(8,4112)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     GO TO 4000
                                                                                                                                                                                                                                                                                                              CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                               CONTINUE
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SELECT NUMBER OF ITERATION FOR OUTPUT

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IMPLICIT DOUBLE PRECISION (A-H,O-2)
PARAMETER(JD=45)
DIMENSION A(JD), B(JD), C(JD), D(JD), BETA(JD), GAMMA(JD)
                                                                                                                                                                                                                                                                                                                                                                                                 SUBROUTINE PRESU(P, DHS, I, M)
IMPLICIT DOUBLE PRECISION (A-H, O-Z)
PARAMETER(ID=152, JD=45)
DIMENSION P(ID, JD)
DIMENSION DHS(ID, JD)
COMMON/PRESS/BCU(ID, JD), CC(JD), DD(JD)
COMMON/AAA/AA(JD), BB(JD), CC(JD), DD(JD), T(JD)
COMMON/CONSI/IMAX, JMAX, IPI, JPI, JPPI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    DO 660 J=2,JMAX
AA(J)=-BCV(I,J-1)
BB(J)=BCU(I,J,J)*M+BCU(I,J)+BCV(I,J-1)
1 +BCV(I,J)
CC(J)=-BCV(I,J)
660 DD(J)=BCU(I,J)*P(I+1,J)+BCU(I-1,J)*P(I-1,J)
                                                                                                                                                           DO 1 I=IFP1,L
BETA(I)=B(I)-A(I)*C(I-1)/BETA(I-1)
GAMMA(I)=(D(I)-A(I)*GAMMA(I-1))/BETA(I)
V(L)=GAMMA(L)
                                                                                                                                                                                                                                                                                                     V(I) = GAMMA(I) - C(I) * V(I+1) / BETA(I)
RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         CALL TRIDAG(2, JMAX, AA, BB, CC, DD, T)
                                                                                                                    GAMMA(IF) -D(IF) / BETA(IF)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               DO 671 J=2,JMAX
                                                                                                  BETA(IF) =B(IF)
                                                                                                                                                                                                                                                                 DO 2 K-1, LAST
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    671 P(1,J) "T(J)
                                                                                                                                                                                                                                            LAST=L-IF
                                                                                                                                           IFP1-IF+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            RETURN
                                                                                                                                                                                                                                                                                 I=L-K
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             O
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 169 WRITE(11,2008) UE(1,3), VE(1,3), UN(1,3), VN(1,3)
1 AKE(1,3), ABS(1,3), PR(1,3)
                                                                                                                                     3001 FORMAT(//5X, 'Y-CORD', 6X, 'VEL U', 7X, 'VEL V', 6X, l'TURB KE', 5X, 'EFF VISC', 3X, 'PRESSURE'//)
                                   2098 WRITE(8,2099) UTAU(I),CFS(I)
2099 FORMAT(5X,'UTAU=',El2.4,5X,'TAUW=',El2.4)
                                                                                                                                                                                              DO 3003 J=1,JP1
3003 WRITE(8,2007) YP(I,J),UE(I,J),VN(I,J)
1 ,AKE(I,J),VIS(I,J),PR(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             DO 5001 I=1,IP1
DO 5001 J=1,JP1
5001 WRITE(7,2005)UE(1,J),VN(I,J),PR(I,J)
1 ,AKE(I,J),ADS(I,J),VIS(I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            WRITE(7,2009) (PR(I,1),I=2,IMAX)
WRITE(7,2009) (UE(I,1),I=M2,IMAX)
WRITE(7,2009) (UTAU(I),I=M1P1,M2M1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  SUBROUTINE TRIDAG(IF, L, A, B, C, D, V)
                                                                                                                                                                                                                                                                                                                                                                                                                                              SAVE DATA FOR ANOTHER CALCULATION
IF(I.LE.M1.OR.I.GE.M2) GO TO 2222
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       OPEN(UNIT-11,FILE-'FVINPUT')
DO 169 I-1,IP1
DO 169 J-1,JP1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         SAVE DATA FOR PLOTTING.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               2005 FORMAT(6E12.4)
2009 FORMAT(6E12.4)
                                                                                                                                                                                                                                                                                                                      2117 FORMAT(4E12.4)
2007 FORMAT(6E12.4)
                                                                                                2222 WRITE(8,3001)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  IF NECESSARY
                                                                                                                                                                                                                                                                                                                                                                                                       GO TO 5555
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        CLOSE(11)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     CLOSE(7)
CLOSE(8)
CLOSE(9)
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C
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